

# ONION-SKIN METHOD (OSM) ANALYSIS OF DIII-D EDGE MEASUREMENTS

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# ABSTRACT

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- OSM analysis provides, in principle, a method for identifying the 2-D edge “fields” of  $n_e$ ,  $T_e$ ,  $T_i$ , etc, which is the prerequisite for analyzing the physics processes occurring in the edge, including impurity behavior
- In order to further test this method, an OSM analysis of an extensive edge database for an L-mode DIII-D discharge has been carried out, the first part of which is reported here
- Consistency of OSM results with Langmuir probe,  $D_{\alpha}$ , and edge Thomson scattering measurements encourages further development of the method

# OBJECTIVE

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## What's wanted:

The 2-D “fields” of the primary quantities  $n_e$ ,  $T_e$ ,  $T_i$ ,  $v_{||}$ ,  $V$  throughout the SOL and divertor

## What we've got:

- Measurements here and there of some of these quantities, e.g. from probes, Thomson
- Measurements of some secondary quantities, e.g. poloidal distribution of  $D_\alpha$

## The Task:

Piece the 2-D fields together from this limited database

One Method: **Onion-Skin Method, OSM, Analysis**

# ORGANIZATION OF THIS POSTER

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- 1<sup>st</sup> column: Abstract etc.
- 2<sup>nd</sup> column: OSM description
- 3<sup>rd</sup> column: the DIII-D shot
- 4<sup>th</sup>, 5<sup>th</sup> columns: comparisons of OSM results with measurements

# ONION-SKIN METHOD, OSM, ANALYSIS

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- Solve the 1-D, **along-B**, plasma conservation equations using **across-B** boundary conditions from experiment, e.g.  $I_{\text{sat}}^+$  and  $T_e$  across targets from Langmuir probes to produce a **2-D solution**
- The plasma solver is iterated with a 2-D neutral code, **EIRENE**, to provide the particle, momentum and power terms associated with hydrogen recycle
- **$D_{\perp}^{\text{SOL}}$  and  $\chi_{\perp}^{\text{SOL}}$**  : **not required as input**. The cross-field information is implicitly contained in the cross-field boundary conditions. In fact, they can be **extracted** from OSM analysis ( $\Rightarrow$  “Edge TRANSP”)

Comparing Standard **2-D FLUID AND OSM**, First the . . .  
**STANDARD 2-D FLUID EQUATIONS, e.g. UEDGE**

(Cylindrical geometry for illustration; use actual curvilinear, toroidal grid)

**Solve for  $r$  and  $s_{||}$  directions simultaneously:**

**1. Particles**

$$\frac{\partial}{\partial s_{||}} (\mathbf{n}v_{||}) = S_p^{\text{neut}}(\mathbf{r}, s_{||}) + S_{p\perp}$$

where:  $S_{p\perp} = \frac{1}{r} \frac{\partial}{\partial r} (r\Gamma_r)$  and  $\mathbf{n}v_r \equiv \Gamma_r = -\mathbf{D}_{\perp} \frac{\partial \mathbf{n}}{\partial r} - \mathbf{n}v_{\text{pinch}}$

**2. Momentum**

$$\frac{\partial}{\partial s_{||}} (\mathbf{p}_i + \mathbf{p}_e + \mathbf{m}_i \mathbf{n}v_{||}^2 + \pi_i) = S_{\text{mom}}^{\text{neut}}(\mathbf{r}, s_{||}) + S_{\text{mom}\perp}$$

where:  $S_{\text{mom}\perp} = \frac{1}{r} \frac{\partial}{\partial r} r [\mathbf{m}_i v_{||} \Gamma_r] + \frac{1}{r} \frac{\partial}{\partial r} \left[ r \eta_{\perp} \frac{\partial v_{||}}{\partial r} \right]$

**3. Ion Energy**

$$\frac{\partial}{\partial s_{||}} \left[ \left( \frac{5}{2} \mathbf{p}_i + \frac{1}{2} \mathbf{m}_i \mathbf{n}v_{||}^2 + \pi_i \right) v_{||} - \kappa_{oi} \mathbf{T}_i^{5/2} \frac{\partial \mathbf{T}_i}{\partial s_{||}} \right] = + \mathbf{e} \mathbf{n} v_{||} \mathbf{E}_{||} + \mathbf{Q}_{\text{eq}} + \mathbf{Q}_{\text{Ei}}^{\text{neut}}(\mathbf{r}, s_{||}) + S_{\text{Ei}\perp}$$

where:  $S_{\text{Ei}\perp} = \frac{1}{r} \frac{\partial}{\partial r} r \left[ \mathbf{n} \chi_{\perp}^i \frac{\partial (k\mathbf{T}_i)}{\partial r} + \left( \frac{5}{2} k\mathbf{T}_i + \frac{1}{2} \mathbf{m}_i v_{||}^2 \right) \Gamma_r \right]$

**4. Electron Energy**

$$\frac{\partial}{\partial s_{||}} \left[ \frac{5}{2} \mathbf{p}_e v_{||} - \kappa_{oe} \mathbf{T}_e^{5/2} \frac{\partial \mathbf{T}_e}{\partial s_{||}} \right] = - \mathbf{e} \mathbf{n} v_{||} \mathbf{E}_{||} - \mathbf{Q}_{\text{eq}} + \mathbf{Q}_R + \mathbf{Q}_{\text{Ee}}^{\text{neut}} + S_{\text{Ee}\perp}$$

where:  $S_{\text{Ee}\perp} = \frac{1}{r} \frac{\partial}{\partial r} r \left[ \frac{5}{2} k\mathbf{T}_e \Gamma_r + \mathbf{n} \chi_{\perp}^e \frac{\partial (k\mathbf{T}_e)}{\partial r} \right]$

# next, the . . . “ONION-SKIN” METHOD OSM EQUATIONS

**PARALLEL — AND  $S^{\text{neut}}$  —TERMS are the same as in 2-D fluid models**

*Apply to each flux-tube individually:*

**1. Particles:** 
$$\frac{d}{ds_{\parallel}} (n v_{\parallel}) = S_p^{\text{neut}}(r, s_{\parallel}) + S_{p\perp}$$

$\int_0^L S_{p\perp}$  KNOWN from particle balance. Spatial variation of  $S_{p\perp}$  to be SPECIFIED

**2. Momentum:** 
$$\frac{d}{ds_{\parallel}} (p_i + p_e + m_i n v_{\parallel}^2 + \pi_i) = S_{\text{mom}}^{\text{neut}}(r, s_{\parallel}) + S_{\text{mom}\perp}$$

$\int_0^L S_{\text{mom}\perp}$  KNOWN from particle balance. Spatial variation of  $S_{\text{mom}\perp}$  to be SPECIFIED

**3. Ion Energy:** 
$$\frac{d}{ds_{\parallel}} \left[ \left( \frac{5}{2} p_i + \frac{1}{2} m_i n v_{\parallel}^2 + \pi_i \right) v_{\parallel} - \kappa_{oi} T_i^{5/2} \frac{dT_i}{ds_{\parallel}} \right] = + e n v_{\parallel} E_{\parallel} + Q_{\text{eq}} + Q_{\text{Ei}}^{\text{neut}}(r, s_{\parallel}) + S_{\text{Ei}\perp}$$

$\int_0^L S_{\text{Ei}\perp}$  KNOWN from particle balance. Spatial variation of  $S_{\text{Ei}\perp}$  to be SPECIFIED

**4. Electron Energy:** 
$$\frac{d}{ds_{\parallel}} \left[ \frac{5}{2} p_e v_{\parallel} - \kappa_{oe} T_e^{5/2} \frac{dT_e}{ds_{\parallel}} \right] = - e n v_{\parallel} E_{\parallel} - Q_{\text{eq}} + Q_R + Q_{\text{Ee}}^{\text{neut}} + S_{\text{Ee}\perp}$$

$\int_0^L S_{\text{Ee}\perp}$  KNOWN from particle balance. Spatial variation of  $S_{\text{Ee}\perp}$  to be SPECIFIED

# OSM OPTIONS FOR SPECIFYING $S_{p\perp}$ , $S_{mom\perp}$ , $Q_{Ei\perp}$ , $Q_{Ee\perp}$

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- To mimic the standard diffusive assumption use:

$$S_{p\perp} = \text{constant} \times (\partial^2 n / \partial r^2) \quad \text{etc.}$$

where  $\partial^2 n / \partial r^2$  is known from **iteration**, thus one can **extract** the constant, i.e. extract

$$D_{\perp}^{\text{SOL}}, \chi_{\perp}^{\text{SOL}}$$

- Or simply use  $S_{p\perp} = \text{constant}$ , or  $\propto n$ , or  $\propto \partial n / \partial r$ ,

after all, we don't actually know if cross-field transport is diffusive,  
and if diffusive, we don't know if  $D_{\perp}^{\text{SOL}}$ ,  $\chi_{\perp}^{\text{SOL}}$  are spatially constant, etc.

## GOOD NEWS:

The solutions are often insensitive to the *spatial distribution* of  $S_{p\perp}$ ,  $S_{mom\perp}$ ,  $Q_{Ei\perp}$ ,  $Q_{Ee\perp}$ , particularly when the boundary conditions are imposed at the downstream, *target end*

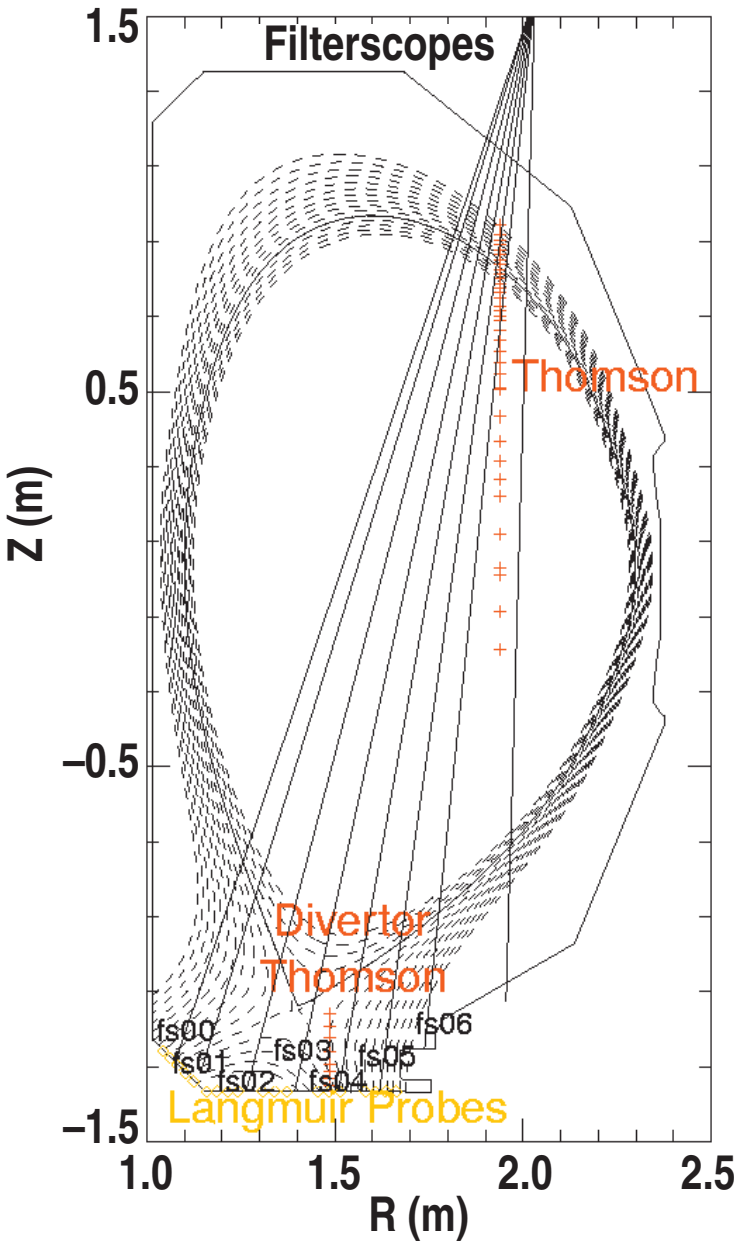


# OSM ANALYSIS OF A DIII-D L-MODE DISCHARGE

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- **DIII-D shot no. 86575:** lower single null, L-mode,  $P_{NB} = 0.85$  MW,  $n_{e0} = 2.1 \times 10^{19}$  m<sup>-3</sup>
- **Divertor Thomson Scattering, DTS,** measured  $n_e$  and  $T_e$  along  $R = 1.49$  m X-point was swept to map out the divertor plasma
- **An array of Langmuir Probes** built into the divertor targets measured  $T_e$  and  $I_{sat}^+$  across the targets
- **The poloidal distribution of  $D_\alpha$  light** across the divertor measured by a calibrated “filterscope”
- **An Upsteam Thomson Scattering System** measured  $n_e$  and  $T_e$  across the SOL and main plasma

# MAGNETIC EQUILIBRIUM FOR SHOT 86575 AT 1650 ms SHOWING LOCATION OF EDGE DIAGNOSTICS



# EFIT

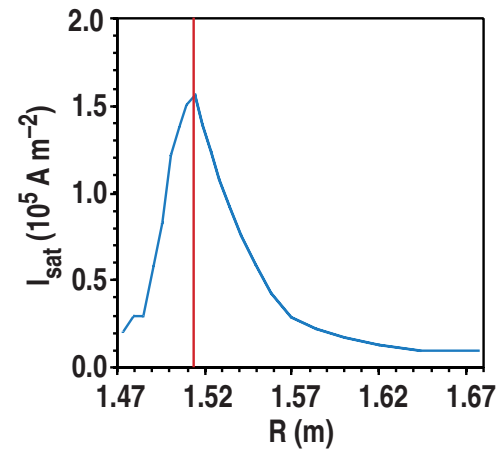
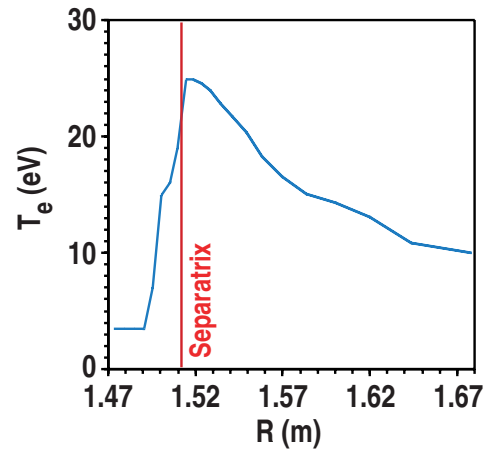
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- OSM analysis depends centrally on the validity of the **computational grid**
- Grid is generated from **EFIT** analysis, e.g. of magnetic pickup coil data
- EFIT **uncertainties** are  $\sim 1$  cm, e.g. in locating separatrix
- This is same order as **SOL radial scale lengths**
- Experimental data were therefore **shifted** relative to the computational grid by up to  $\sim 1$  cm, to see if this would give a match between the OSM-calculated and measured values of  $n_e$ ,  $T_e$ , etc. e.g. from Divertor and Upstream Thomson

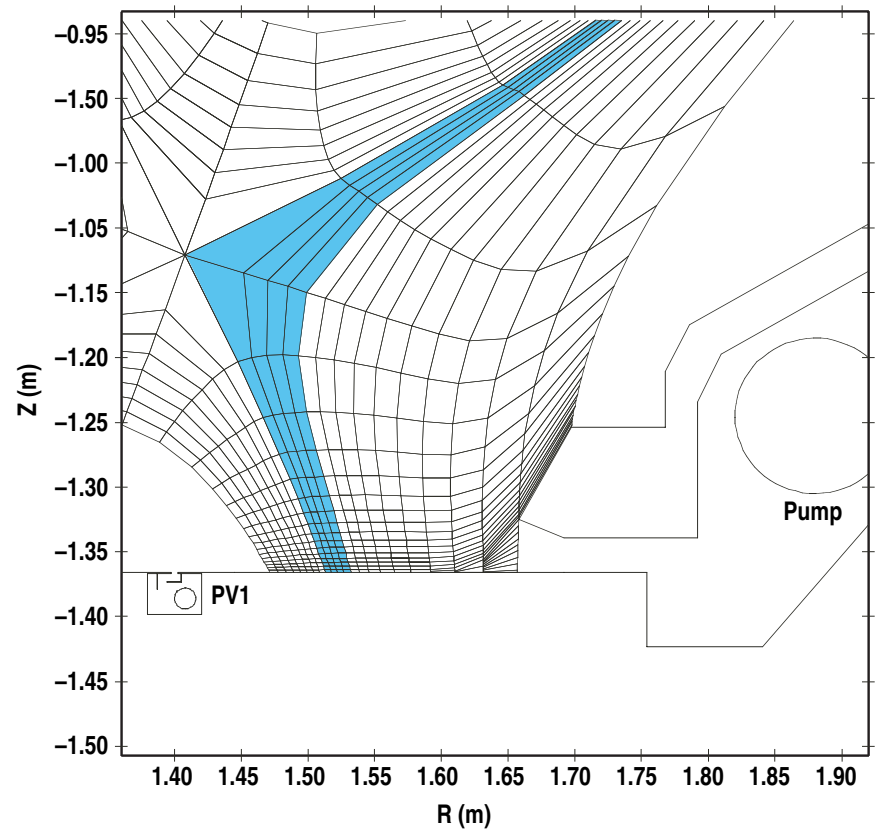
# UEDGE CODE ANALYSIS

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- A first-cut, multifluid UEDGE analysis (Gary Porter) was also carried out for this shot/time
- Input:  $\chi_{\perp e}^{\text{SOL}} = \chi_{\perp i}^{\text{SOL}} = 2.5 \text{ m}^2/\text{s}$ ,  $D_{\perp}^{\text{SOL}} = 0.625 \text{ m}^2/\text{s}$
- Input: recycling coefficient at the walls and targets of unity
- Input: carbon physical and chemical sputtering from the Toronto database (Davis and Haasz, 1996 PSI)
- Input: plasma density was set to match the experimental value upstream near the separatrix

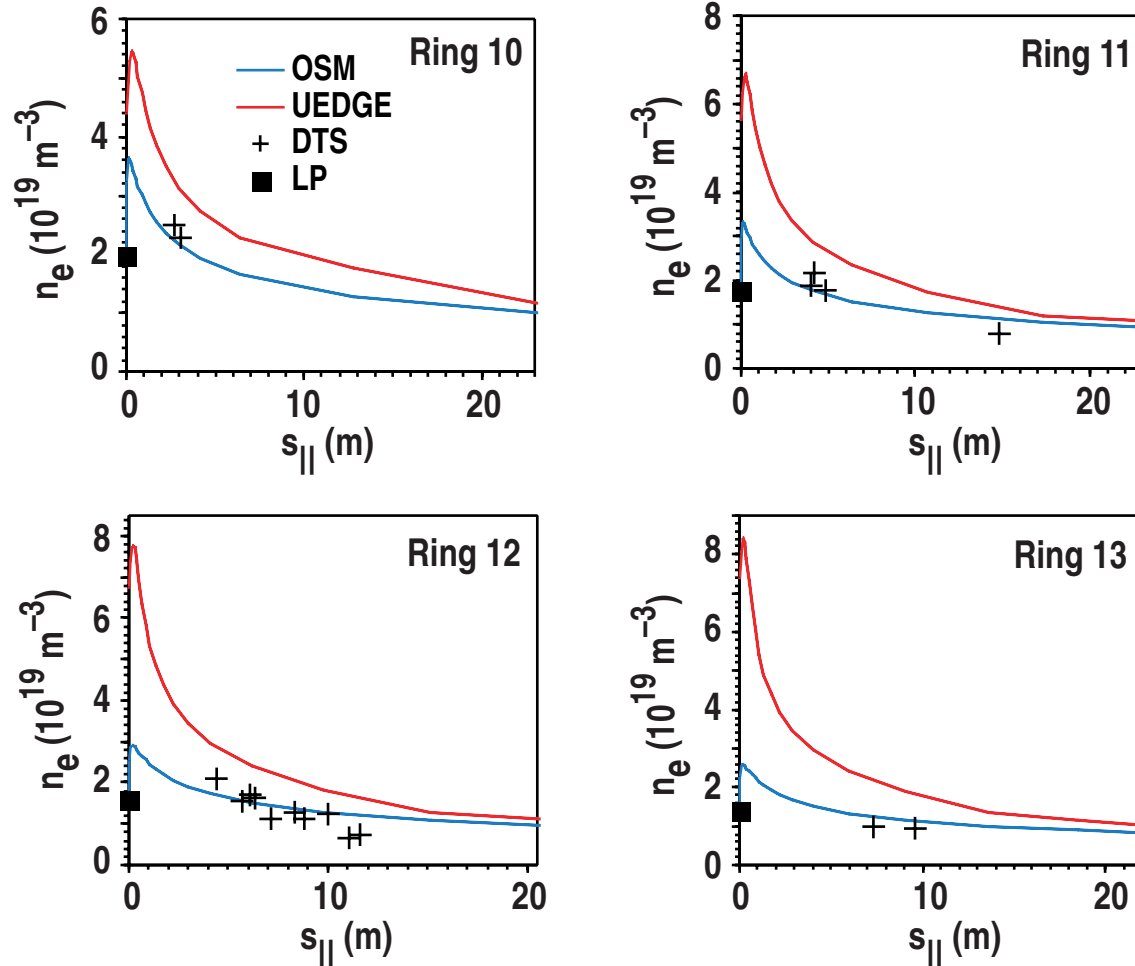


## $I_{\text{sat}}^+$ and $T_e$ from Target Langmuir Probes



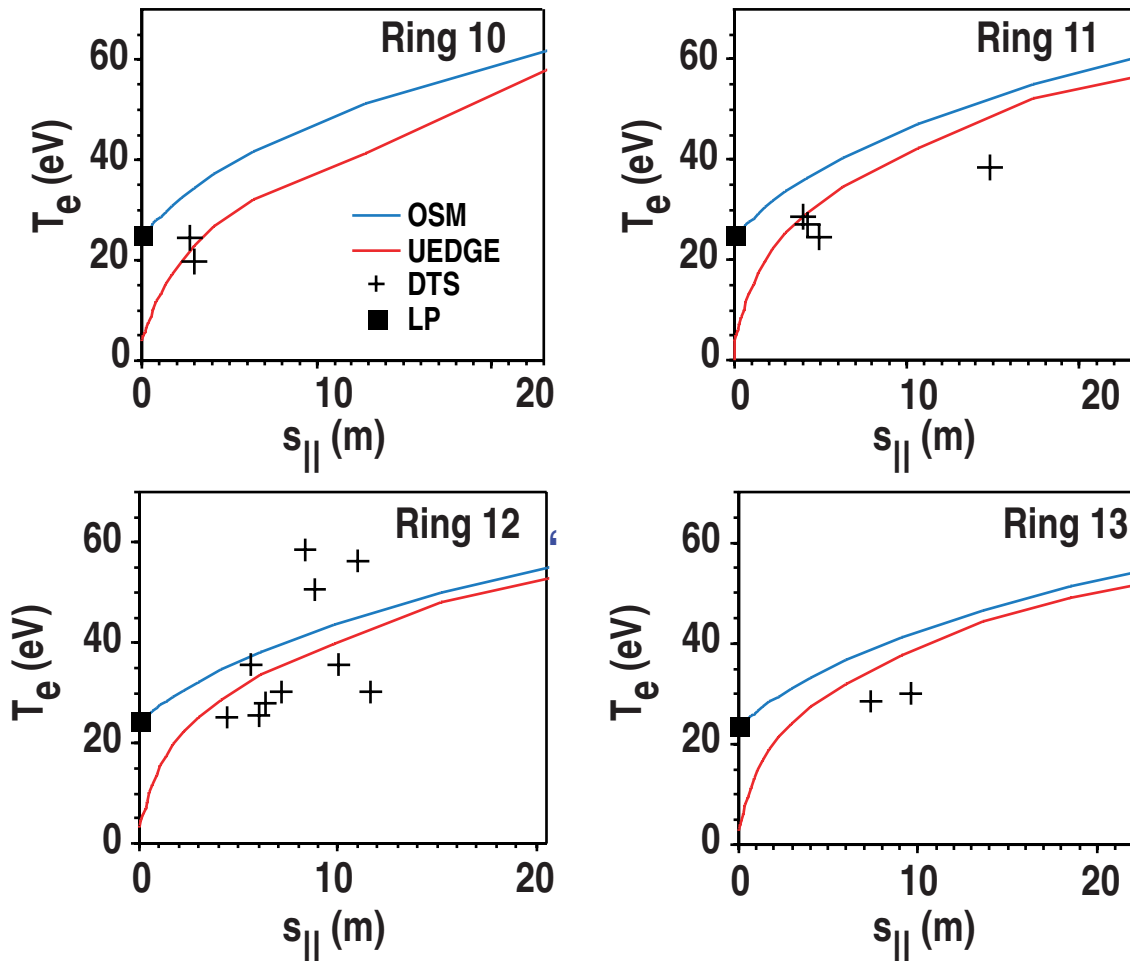
## Computational Grid

# COMPARISON OF OSM AND DIVERTOR THOMSON $n_e$



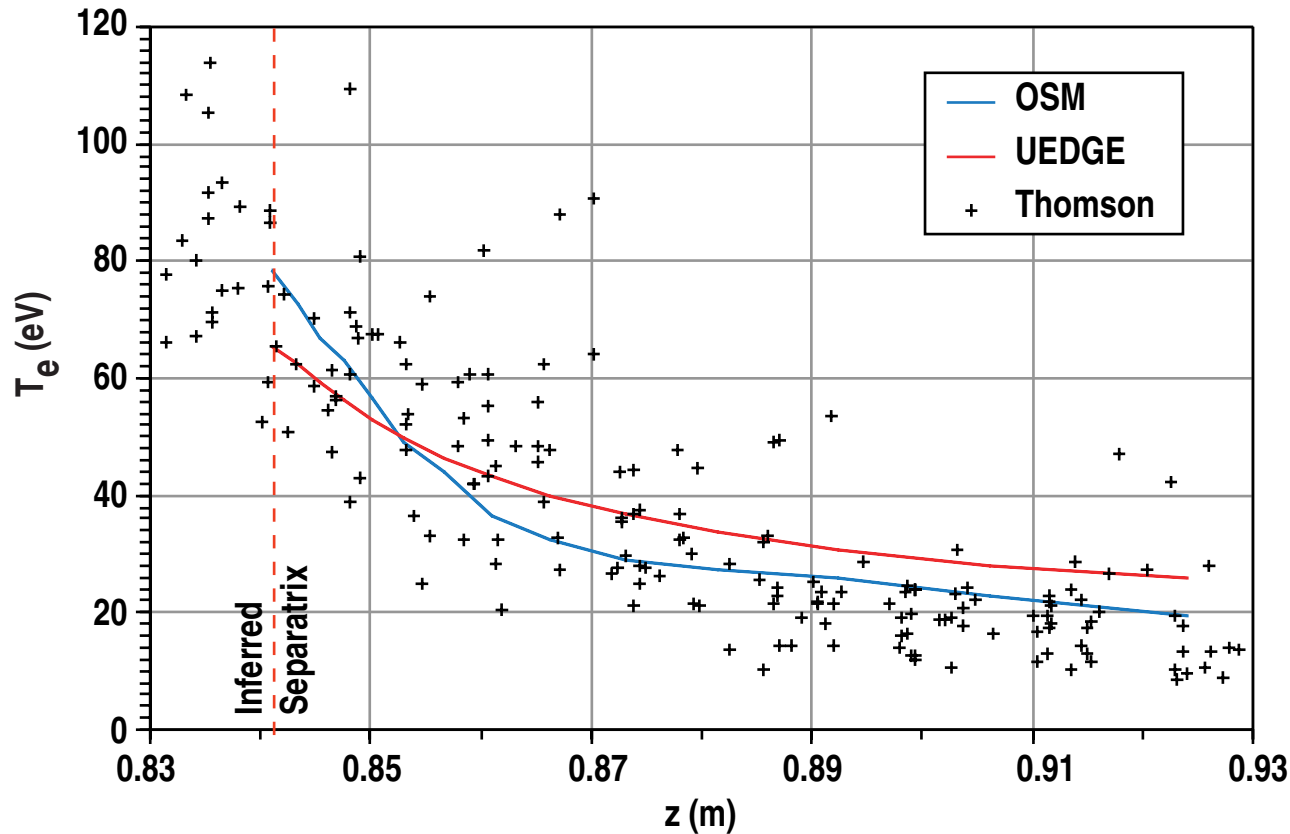
- $n_e(s_{||})$  profiles for the first 4 computational “rings” (onion skins) in the SOL, see earlier figure
- Thomson: crosses
- OSM: blue line
- UEDGE code: red line
- The OSP starts from the Langmuir probe values at the target (squares)
- All data have been shifted by  $\Delta R = -10$  mm relative to the EFIT-based computational grid

# COMPARISON OF OSM AND DIVERTOR THOMSON $T_e$



- $T_e(s_{||})$  profiles for the first 4 computational “rings” (onion skins) in the SOL, see earlier figure
- Thomson: crosses
- OSM: blue line
- UEDGE code: red line
- The OSP starts from the Langmuir probe values at the target (squares)
- All data have been shifted by  $\Delta R = -10$  mm relative to the EFIT-based computational grid

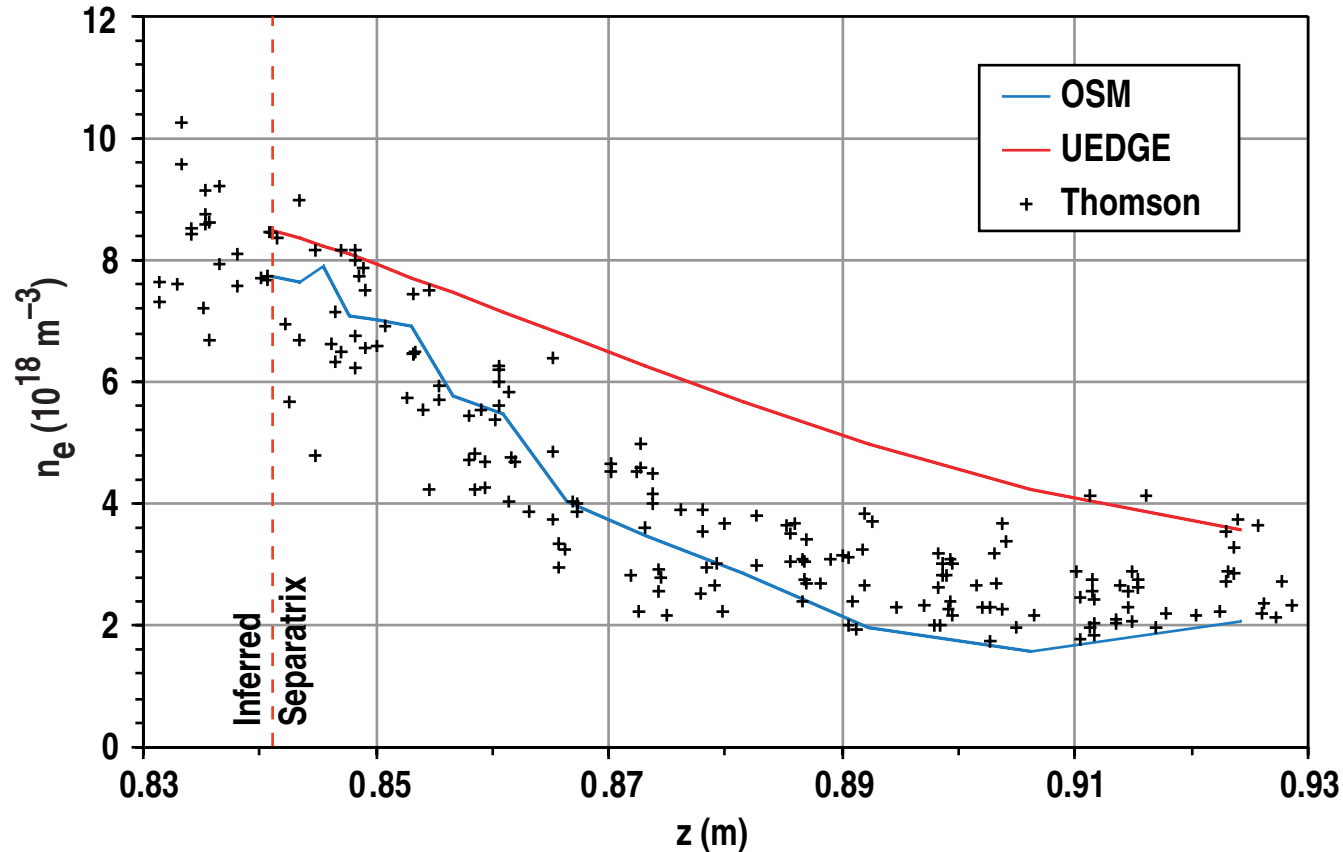
# COMPARISON OF OSM AND UPSTREAM THOMSON $T_e$



- $T_e(z)$  profiles along the line of the Upstream Thomson
- Thomson: crosses
- OSM: blue line
- UEDGE code: red line
- Thomson data have been shifted by  $\Delta Z = +15$  mm relative to the EFIT-based grid

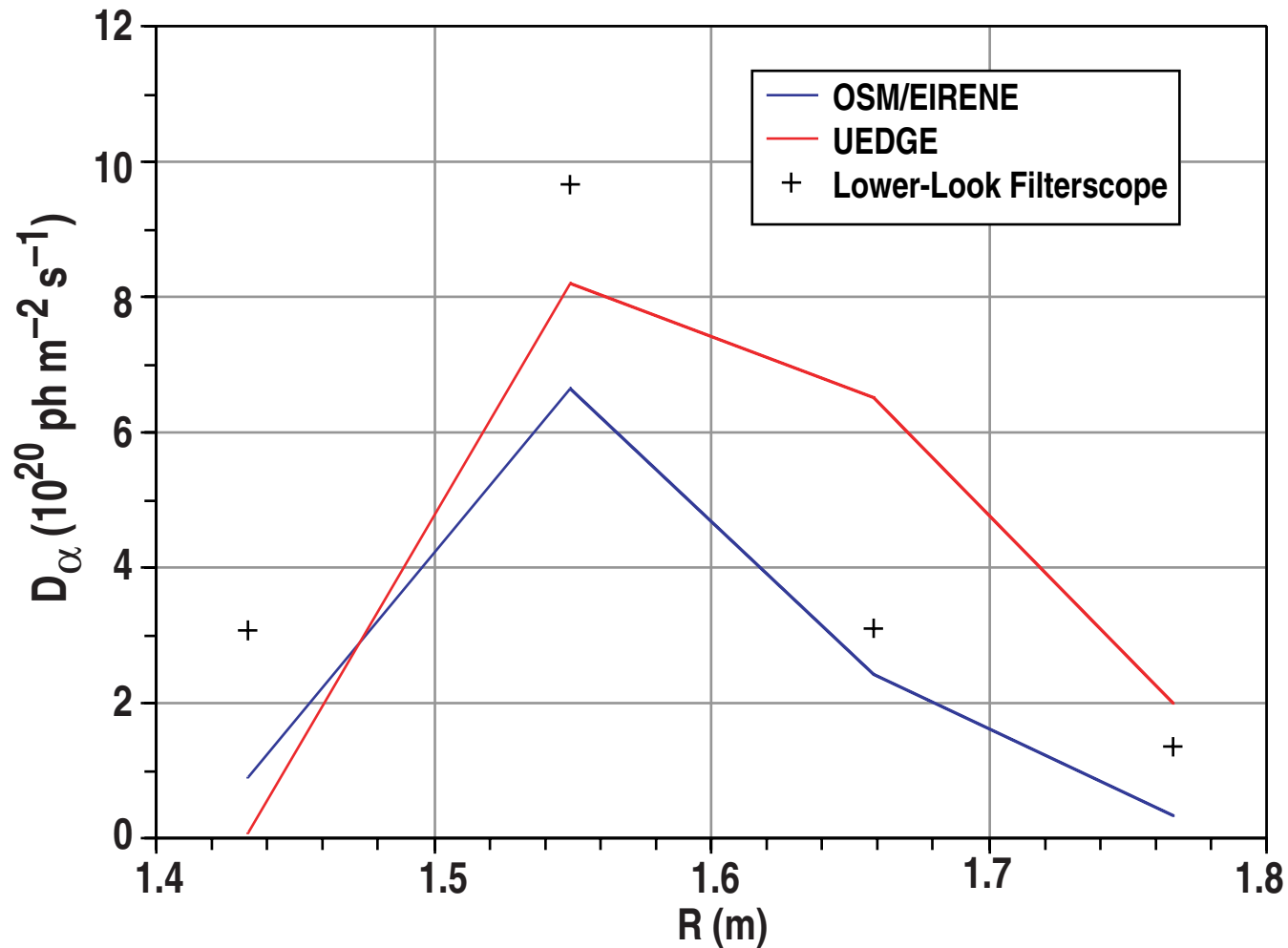


# COMPARISON OF OSM AND UPSTREAM THOMSON $n_e$



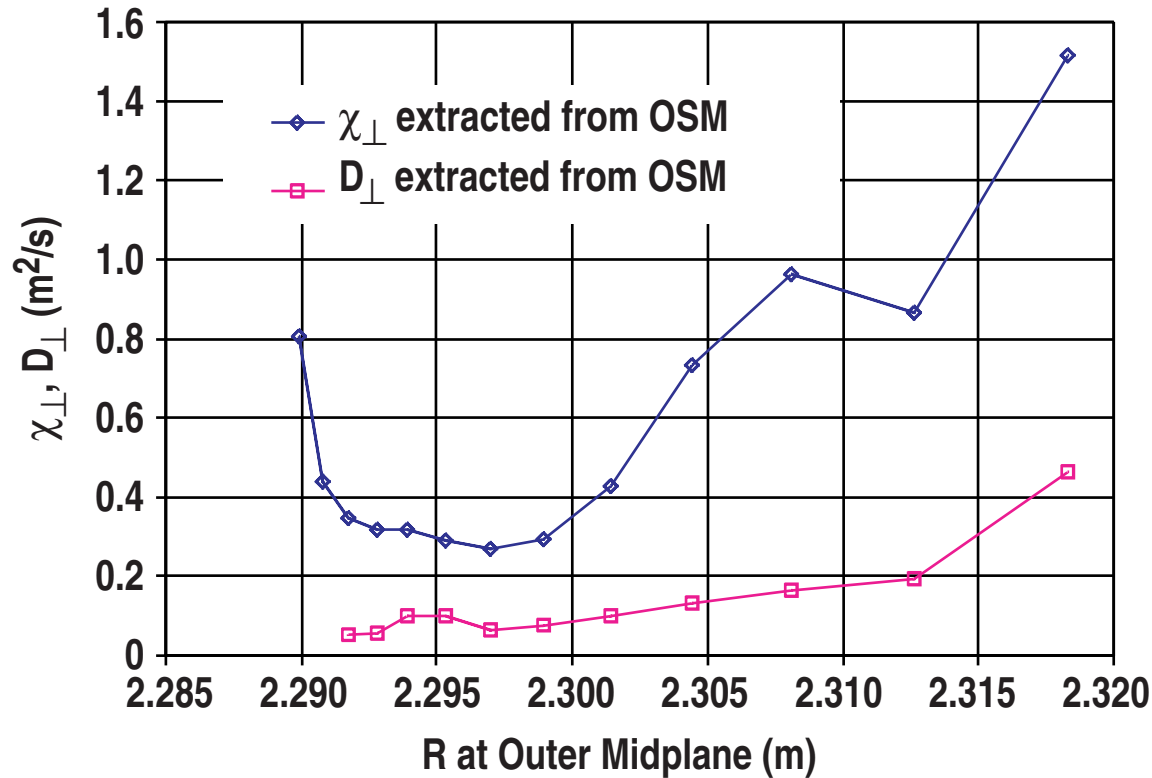
- $n_e(z)$  profiles along the line of the Upstream Thomson
- Thomson: crosses
- OSM: blue line
- UEDGE code: red line
- Thomson data have been shifted by  $\Delta Z = +15$  mm relative to the EFIT-based grid

# COMPARISON OF OSM AND MEASURED $D_\alpha$ POLOIDAL DISTRIBUTION



- $D_\alpha$  emissivity (photons/ $m^2$ /s) across the outer target
- Experiment (filterscope): crosses
- OSM: blue line
- UEDGE code: red line

# VALUES OF $D_{\perp}^{\text{SOL}}$ AND $\chi_{\perp}^{\text{SOL}}$ EXTRACTED FROM THE OSM ANALYSIS



- Cross-field ion and electron power flows were added, so the  $\chi_{\perp}^{\text{SOL}}$  value is an average of  $\chi_{\perp e}^{\text{SOL}}$  and  $\chi_{\perp i}^{\text{SOL}}$
- The trend for  $\chi_{\perp}^{\text{SOL}}(r)$  to increase with distance into the SOL has also been reported for JET

# CONCLUSIONS

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- OSM analysis has been tested against a larger edge data set than before
- OSM results are within error/scatter of Langmuir probe,  $D_{\alpha}$ , and edge Thomson measurements, encouraging further testing and development of the method
- A number of issues remain to be addressed:
  - EFIT uncertainties license data shifting, but may “sweep under the carpet” real discrepancies, missing physics, etc.; analysis of other discharge types, direction of B, and yet larger edge sets, are required
  - Thomson data are particularly valuable, but have substantial scatter (Thomson samples the fluctuations). Un-swept, averaged data required
  - Detachment, PFZ, and impurity modeling are still to be tackled
  - Coupling to UEDGE code