



# A THEORETICAL AND EXPERIMENTAL INVESTIGATION INTO ENERGY TRANSPORT IN HIGH TEMPERATURE TOKAMAK PLASMAS

*Presented by*  
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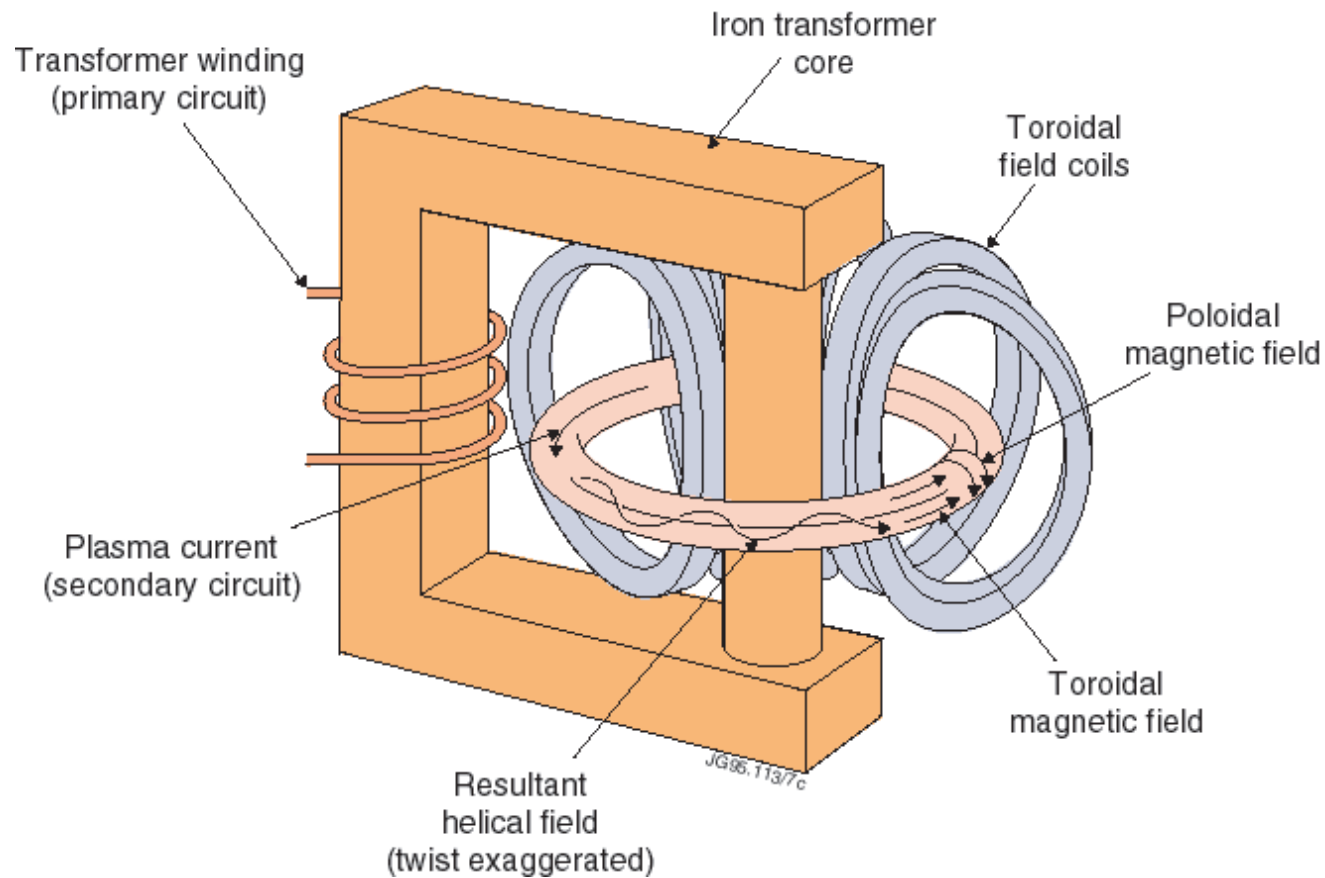
# KEY POINTS

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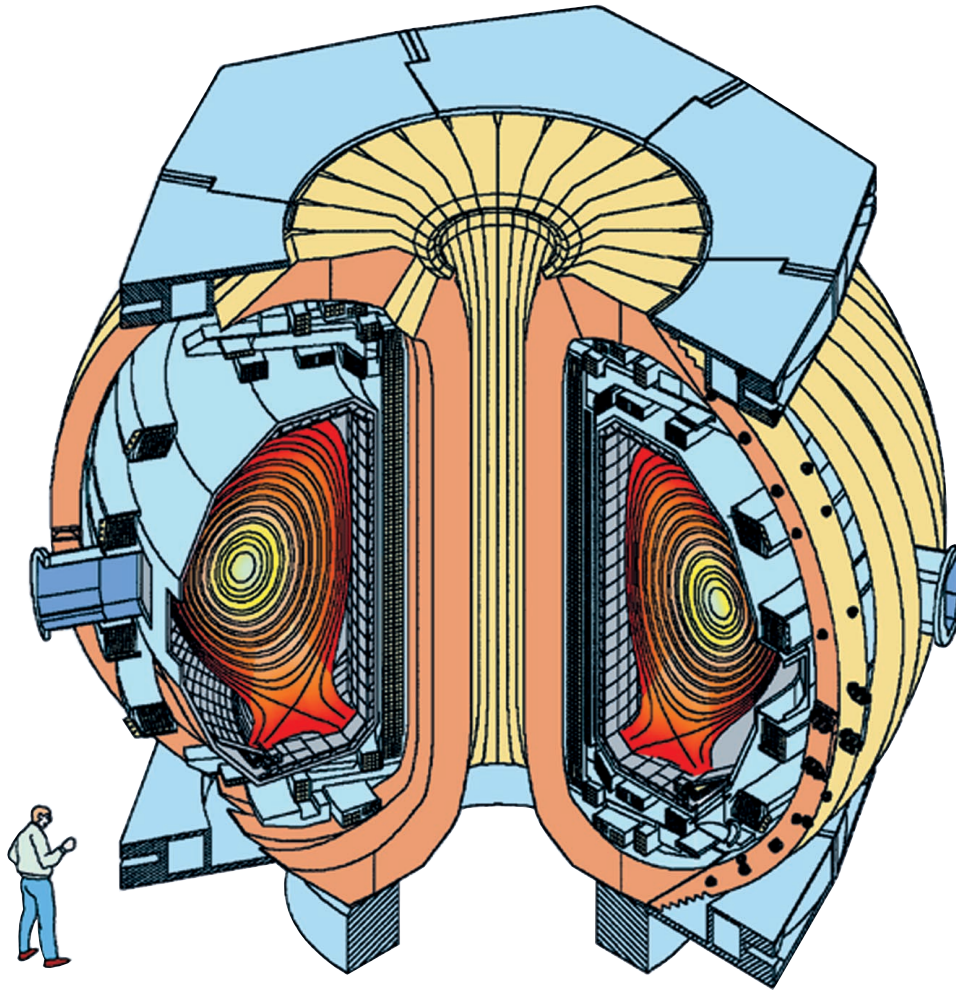
- *Considerable progress has been made in the understanding of the transport processes taking place in a tokamak*
- *In the theoretical area large codes have been developed which simulate the turbulence and ensuing radial transport*
  - *Fully validating one-dimensional model describing transport throughout the radial region is not available*
- *Two methods have been used to supplement the theoretical modeling*
  - *Global energy confinement scaling method*
  - *Dimensionless physics parameter similarity technique*

# TOKAMAK: MAGNETIC CONFINEMENT

- Toroidal magnetic field supplemented by a poloidal component produced by a large current in the plasma itself
  - Plasma current is induced by a transformer

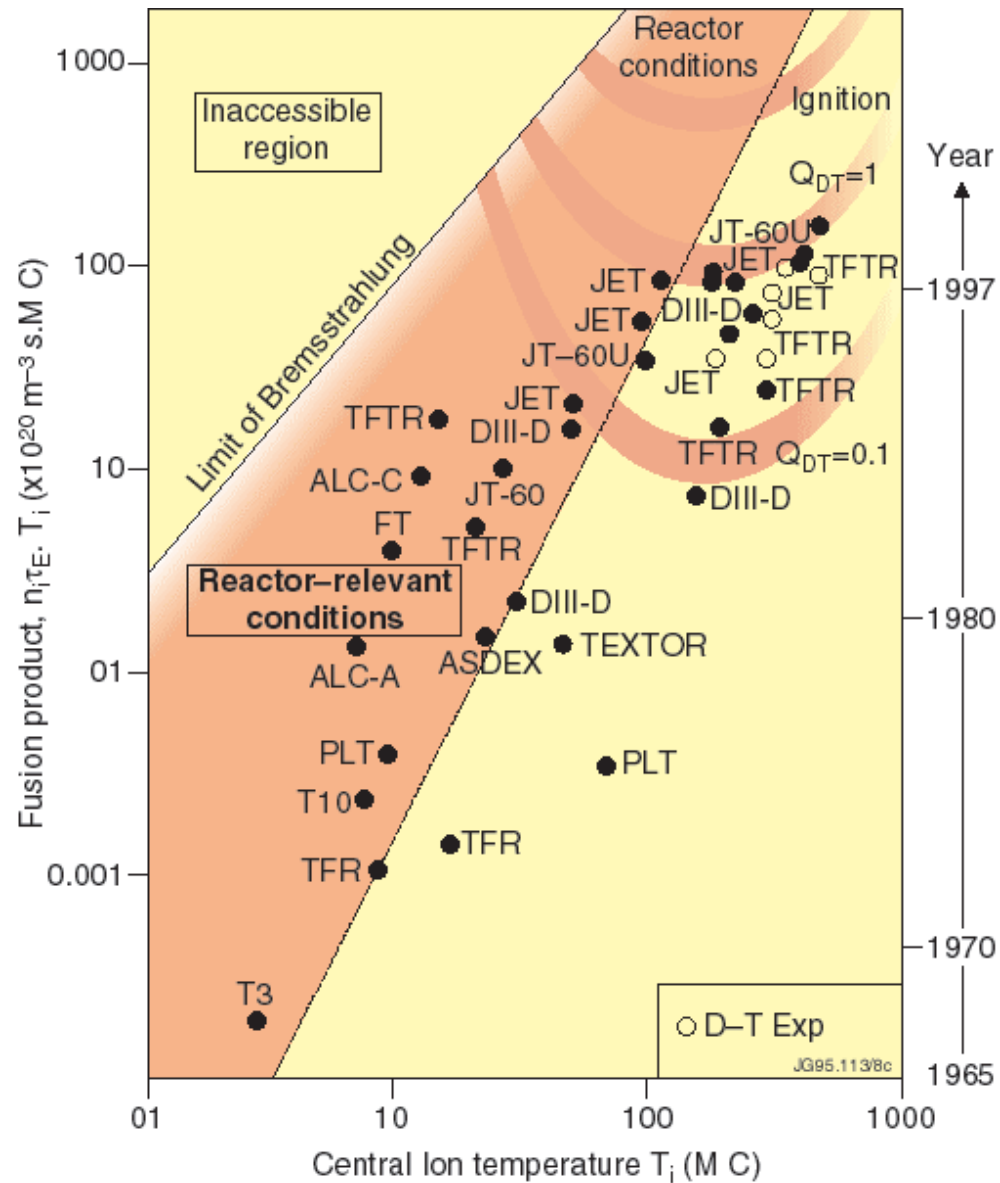


# DEFINITION OF COMMON TERMS



$\tau_E$	—	Energy confinement time (s)
$I_p$	—	Toroidal plasma current (amp)
$B_T$	—	Toroidal magnetic field (T)
$P_{aux}$	—	Auxiliary heating power (W)
$n_e$	—	Electron density ( $m^{-3}$ )
$A_i$	—	Ion mass (atomic mass units)
$R$	—	Tokamak major radius (M)
$a$	—	Tokamak minor radius (m)
$\kappa$	—	Plasma elongation

# STEADY PROGRESS TO REACTOR CONDITIONS



# SUMMARY

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- **Statistical analysis of the energy confinement data**
  - **Virtues: Simplicity and a good track record of predicting behavior**
  - **Weaknesses: Ignore profile effects and possible hidden parameters**
- **Dimensionless physics parameter similarity approach**
  - **Virtue: Profile effects are fully included**
  - **Weaknesses: Range in experimental  $\rho_*$  is small, need a larger experimental database, uncertainty about which are the key parameters**
- **Full 1-D Modeling**
  - **Virtue: In principle all transport processes, sources, and sinks can be included**
  - **Weaknesses: Progress in modeling core, edge region still being worked on**

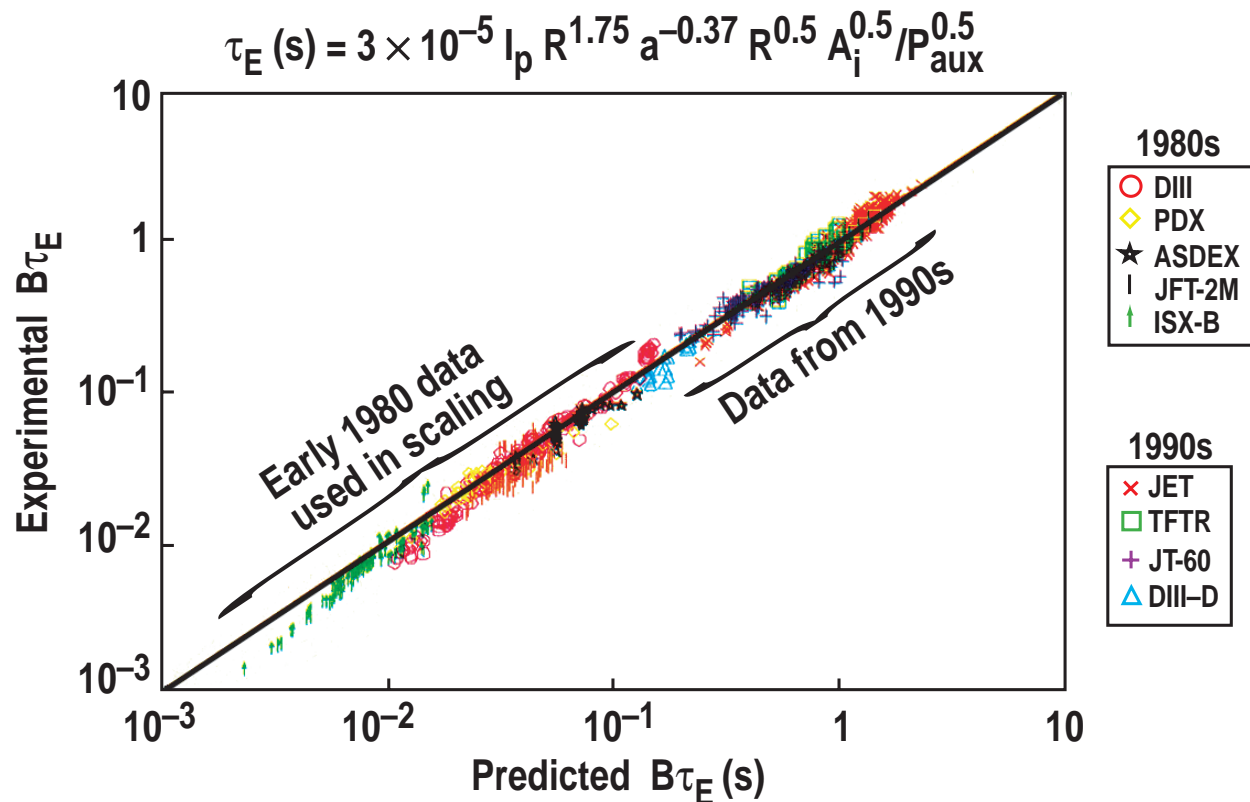
# GLOBAL ENERGY CONFINEMENT SCALING

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- *Yields an overview of the “physics terrain”*
- *Provides some basis for extrapolation to future devices*
- *Potential to give critical information for understanding the underlying nature of radial transport*
- *Empirical energy confinement scaling done in the form of a power law*
  - $\tau_E \propto a^x b^y c^z \dots$
  - *a,b,c are plasma parameters*
  - *x,y,z are simple numerical exponents*

# EARLY CONFINEMENT RELATIONSHIP

- 1982 data from small to medium size tokamaks (DIII, PDX, ASDEX, JET, JFT-2M, ISX-B)
  - $R = 0.9 - 1.6$  m,  $a = 0.25 - 0.45$  m,  $I_p = 100 - 600$  kA,  $P_{aux} = 0.2 - 6$  MW
- 10 years later predicted confinement in much larger tokamaks
  - $R \sim 3$  m,  $a \sim 1$  mm,  $I_p$  up to 7 MA,  $P_{aux}$  up to 30 MW
  - Mean error of 4% and an RMS spread of 12%





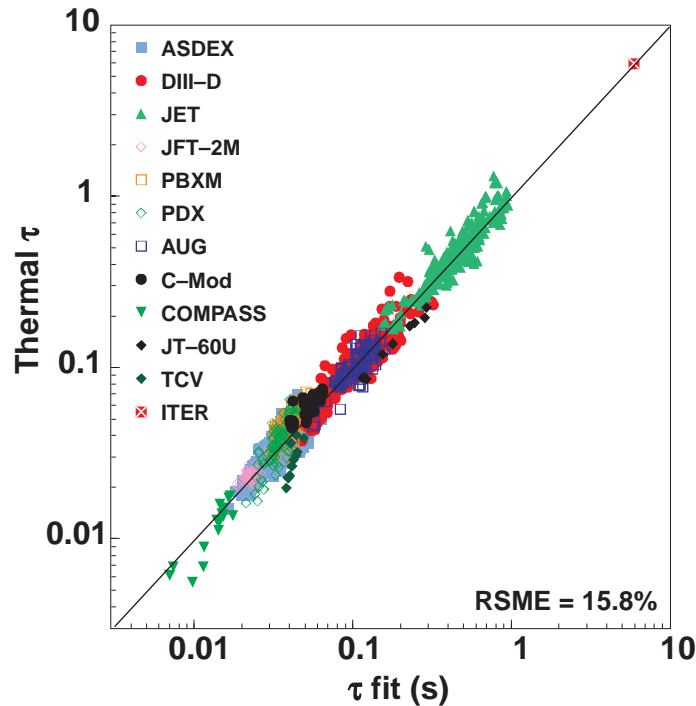
# ***HIGH MODE OR H-MODE CONFINEMENT SCALING***

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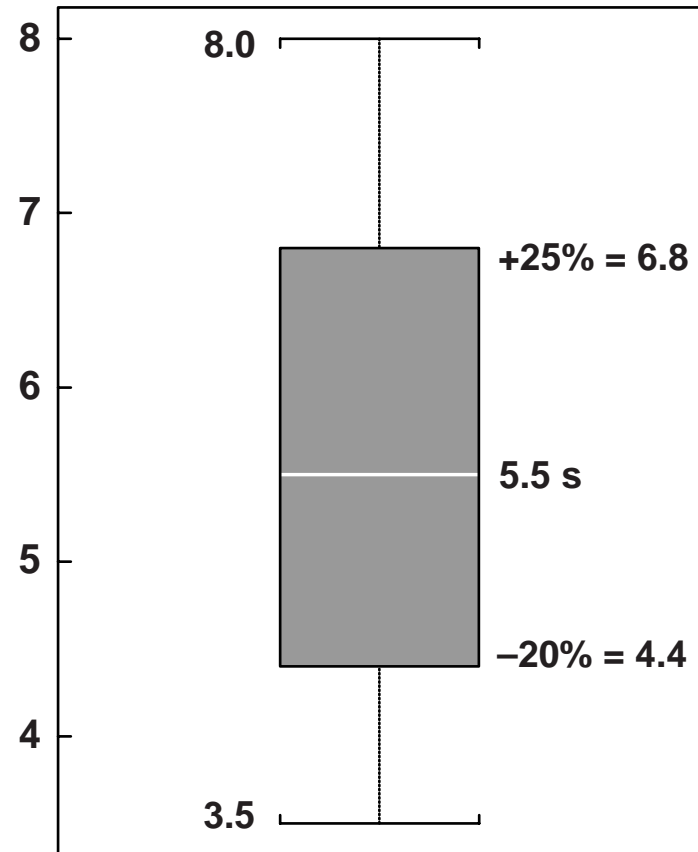
- ***Plasma can transition to a higher energy confinement state***
  - ***This states provides the framework for future machine design***
- ***Empirical relationships have been used to study H-mode confinement***
- ***Most recent work includes data from 13 tokamaks worldwide***
  - ***1398 data points used in scaling***

# PRESENT DAY H-MODE CONFINEMENT SCALING

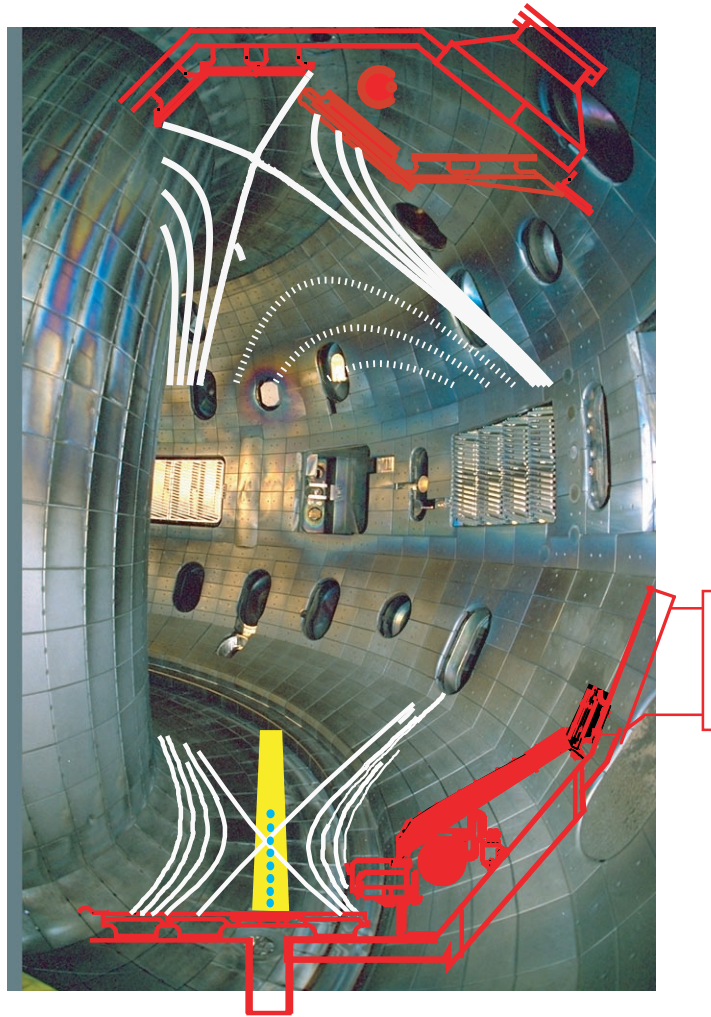
- Dataset spans confinement times over 2 orders of magnitude
- 95% confidence interval for power law form is  $\delta\tau/\tau \approx \pm 17\%$
- $\delta\tau/\tau$  increases when other representations other than power law are considered



- $\tau_E = 0.03 I_p^{0.89} B_T^{0.18} P_{aux}^{-0.64} N_e^{0.43} A_i^{0.13} R^{1.83} \epsilon^{0.24} \kappa^{0.88}$



# DIMENSIONLESS SCALING OR WIND TUNNEL EXPERIMENTS



- For a future machine design, create discharges with the same shape and with as many dimensionless physics profiles matched
- Only  $\rho_*$  can not be matched and its scaling must be determined

$T$	—	Temperature
$\beta$	—	Particle to B pressure ( $nT/B^2$ )
$\nu_*$	—	Collisionality ( $na/T^2$ )
$q$	—	Safety factor ( $B_T a/B_p R$ )
$\rho_s$	—	Larmor radius ( $mv/B$ )
$\rho_*$	—	Normalized gyroradius ( $\rho_s/a$ )
$\chi_B$	—	Bohm diffusion ( $eT/cB$ )

# DIMENSIONLESS PARAMETER SCALING TECHNIQUES

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- *Significant progress has been made towards predicting and understanding radial heat transport using these techniques*
- *Two types of turbulent diffusion depending on step size*
  - *Macroturbulence: step or eddy size ( $\Delta$ ) on the order of the device size ( $a$ )*
  - *Microturbulence:  $\Delta$  on the order of an intrinsic plasma parameter ( $\rho_s$ )*
- *Plasma diffusivity ( $\chi$ ) is proportional to a rate and a step size squared*
- *Expressing  $\chi$  in its dimensionally correct form*
  - $\chi = \chi_B \beta^{\alpha_B} v^{\alpha_v} \rho_*^{\alpha_\rho} q_{95}^{\alpha_q} F(R/a, \kappa, T_e, T_i, \dots)$
  - *F is an unknown function of all the other dimensionless parameters*
  - *For  $\alpha_\rho = 1$  implies  $\Delta = \rho_s$  which is called gyro-Bohm scaling*
  - *For  $\alpha_\rho = 0$  implies  $\Delta = a$  which is called Bohm scaling*
  - *For  $\alpha_\rho = -1$  implies  $\Delta \gg a$  which would arise from stochastic fields*

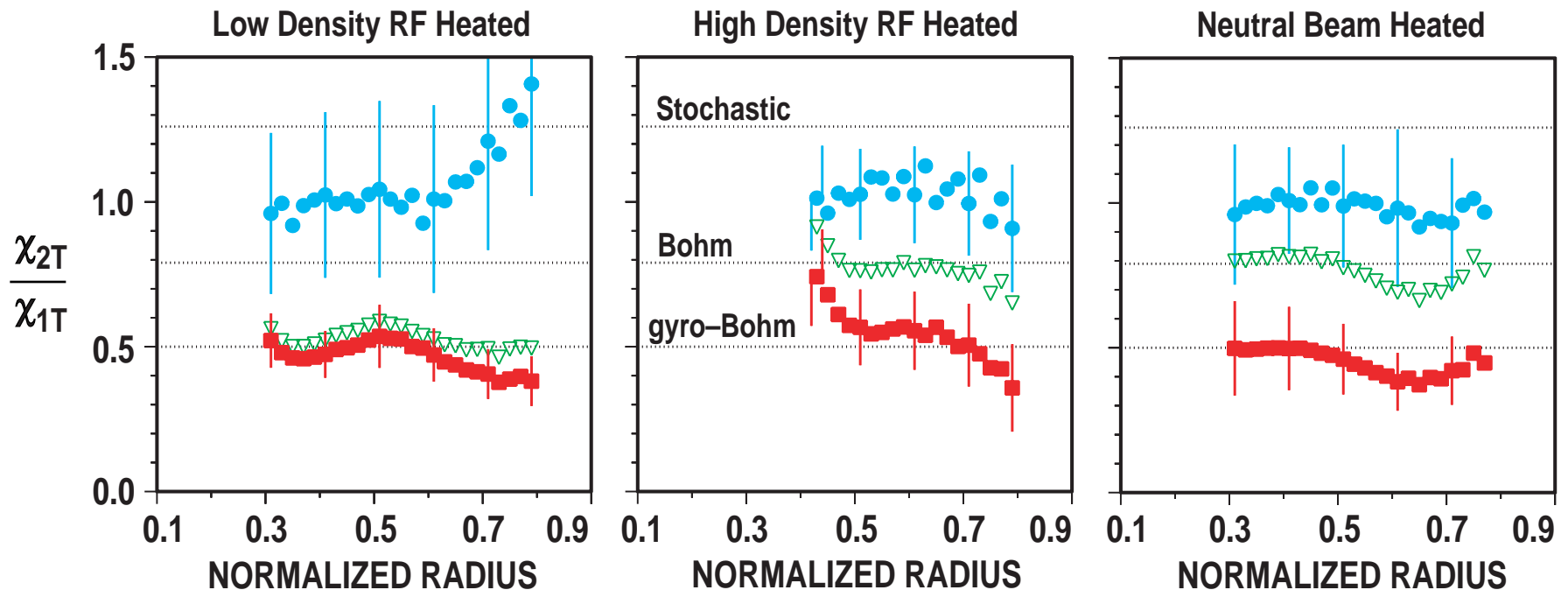
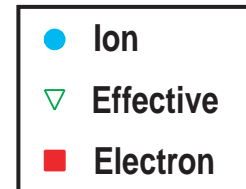
# EXAMPLE OF A $\rho_*$ SCALING EXPERIMENT

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- *Plasma size and shape are held fixed and  $B$  and  $T$  change to vary only  $\rho_*$*
- *For a change in  $B$ , to keep  $\beta$ ,  $v_*$ , and  $q$  constant*
  - $n \propto B^{4/3}$
  - $T \propto B^{2/3}$
  - $I \propto B$
- *The effective charge ( $Z_{\text{eff}}$ ), ion mass,  $T_e/T_i$ , heating profiles, and the density and temperature scale lengths should also be held constant*
- *Variation in  $\rho_*$  is proportional to  $B^{-2/3}$*
- *Experiment varied  $B$  from 1 to 2 T*
  - *Dimensionless parameters well matched*
  - $\rho_*$  *varies by 1.6 as expected*

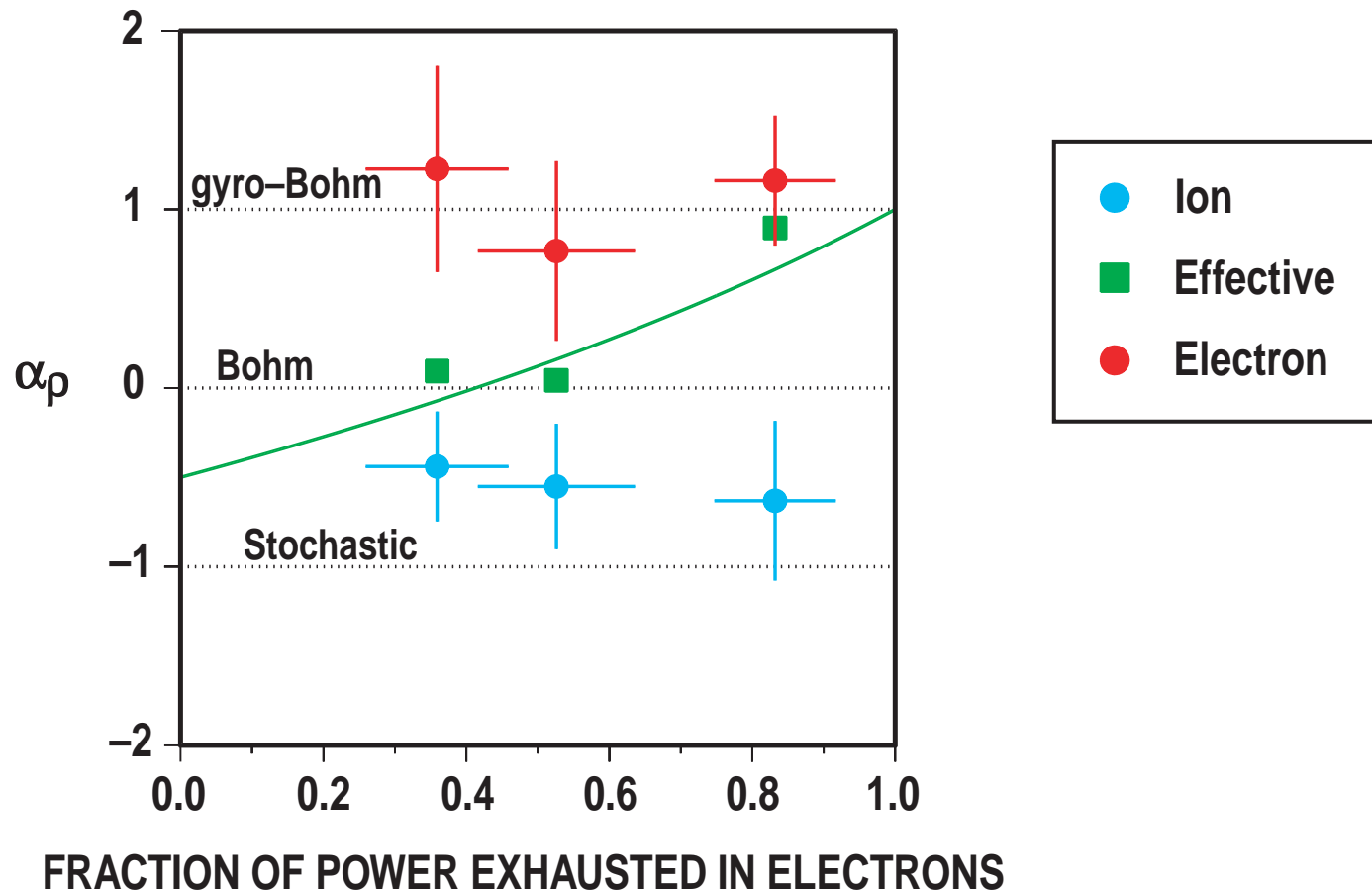
# $\rho_*$ SCALING OF ION AND ELECTRON SPECIES IS DIFFERENT

- Electrons scale as gyro-Bohm
- Ions scale between Bohm and stochastic
- Effective diffusivity is the combined average of electrons and ions

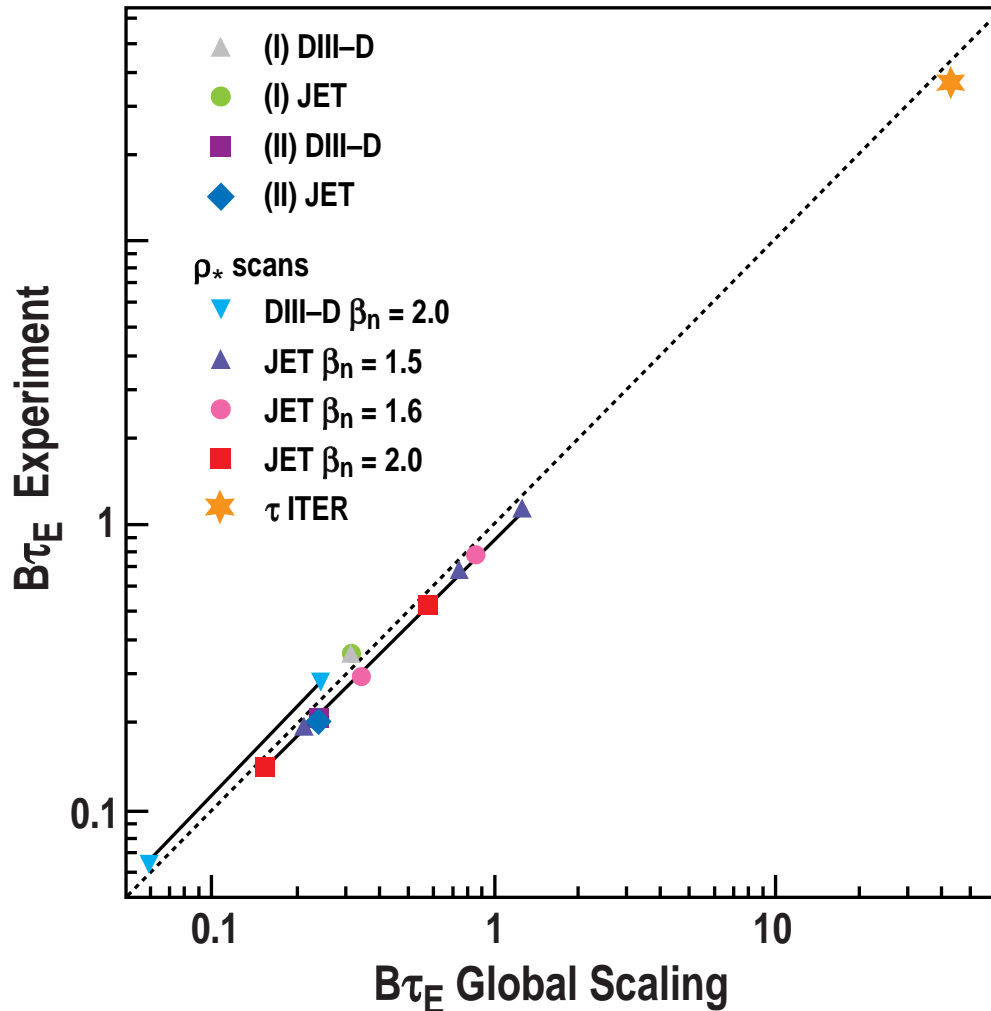


# IONS AND ELECTRONS SCALE DIFFERENTLY THAN THE GLOBAL AVERAGE

- For the beam heated case, the global scales like Bohm when neither species does
- Global is the weighted average, by power flow, of the individual species



# SINGLE PARAMETER $\rho_*$ EXTRAPOLATION TO FUTURE MACHINES IS FEASIBLE



- Presently range in  $\rho_*$  is too small in one machine to predict a large future machine
- Uncertainty will be reduced by a joint  $\rho_*$  scan on at least two machines of different sizes
- Small scale turbulence and electrostatic (weak  $\beta$ )

$$\tau_E \propto B^{-1} \rho_*^{-3.15} \beta^{0.03} \nu^{-0.42} q_{95}^{-1.43}$$

$$\propto I_p^{0.84} B^{0.39} n^{0.18} \rho_{aux}^{-0.41} L^{2.00}$$



# PREDICTIVE TRANSPORT MODELING

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- **Objective**
  - *Predict temporal evolution of existing experiments*
  - *Gain insights into the physics governing transport*
  - *For future devices: extrapolate, investigate profile effects, and study new regimes — none of which can be done by global scaling laws*
- **Historically, transport models have been constructed from purely empirical observations of experimental data**
  - *Limited predictive capability due to a narrow range of observations*
- **Lately, considerable progress has been made in understanding the underlying physics governing confinement**
  - *Focus on anomalous (turbulence driven) transport*
  - *Improvements in computer code technology*

## A LARGE GROUP OF MODELS ARE BEING TESTED

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<i>Model</i>	<i>Model Providers</i>	<i>Physics</i>
<i>Weiland</i>	<i>J. Weiland (EU)</i>	<i>ITG</i>
<i>Multimode</i>	<i>J. Kinsey, G. Bateman (US)</i>	<i>Drift waves, RBM, kinetic ballooning, neoclassical</i>
<i>Waltz GLF23</i>	<i>R. Waltz, J. Kinsey (US)</i>	<i>ITG</i>
<i>IFS/PPPL, no E×B; IFS/PPPL, E×B</i>	<i>B. Dorland (US)</i>	<i>ITG</i>
<i>CDBM</i>	<i>A. Fukuyama (JA)</i>	<i>Current diffusive ballooning modes</i>
<i>RLW B, RLW</i>	<i>D. Boucher (JCT)</i>	<i>Semi-empirical</i>
<i>Culham</i>	<i>M. Turner (EU)</i>	<i>Semi-empirical</i>
<i>Mixed</i>	<i>A. Taroni (EU)</i>	<i>Semi-empirical</i>
<i>Mixed-shear</i>	<i>G. Vlad/M. Marinucci (EU)</i>	<i>Semi-empirical</i>
<i>T11/SET</i>	<i>A. Polevoi (RF)</i>	<i>Semi-empirical</i>
<i>CPTM</i>	<i>Yu. Dnestrovskij (RF)</i>	<i>Semi-empirical</i>

# **A LARGE DATABASE HAS BEEN ASSEMBLED FOR USE IN MODEL VALIDATION**

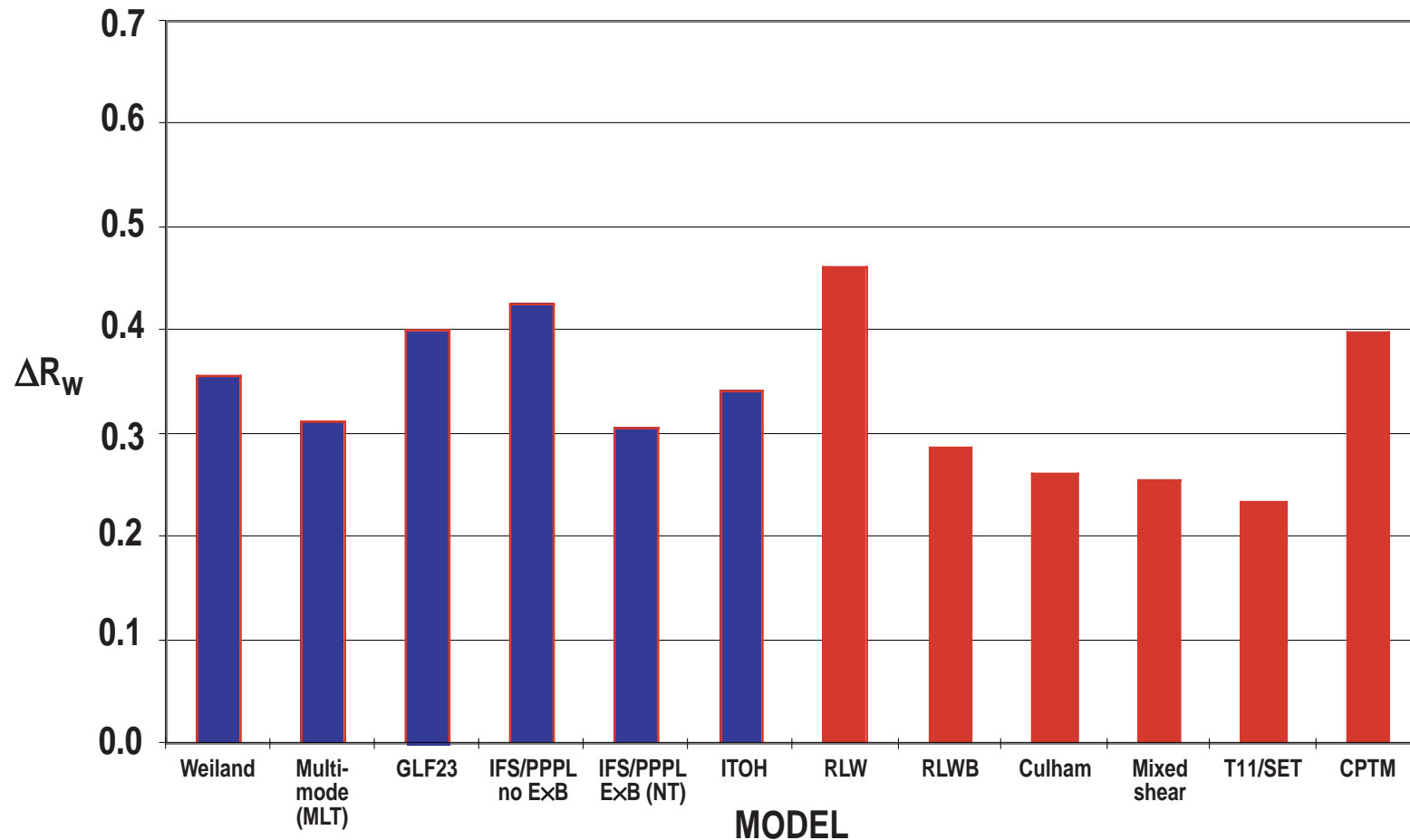
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- *Represents an open and systematic procedure for assessing the performance of transport models against well documented data*
- *Database consists of 209 discharges from 12 different tokamaks*
- *Eleven transport models are being tested by a larger number of modelers*
- *Quantitative comparison is made between the model prediction and the experimental data for both global and local quantities*

# AVERAGE ERROR IN STORED ENERGY PREDICTION

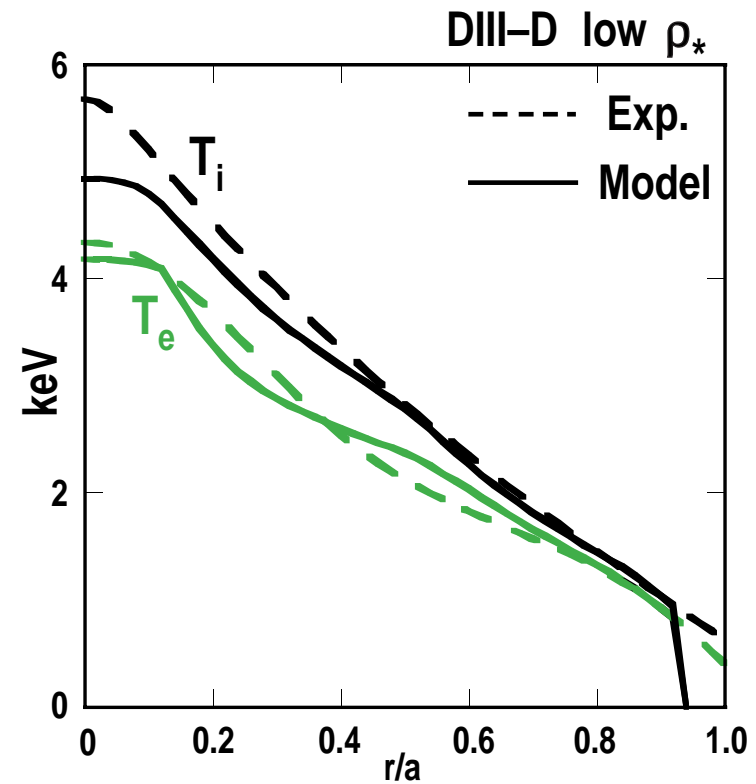
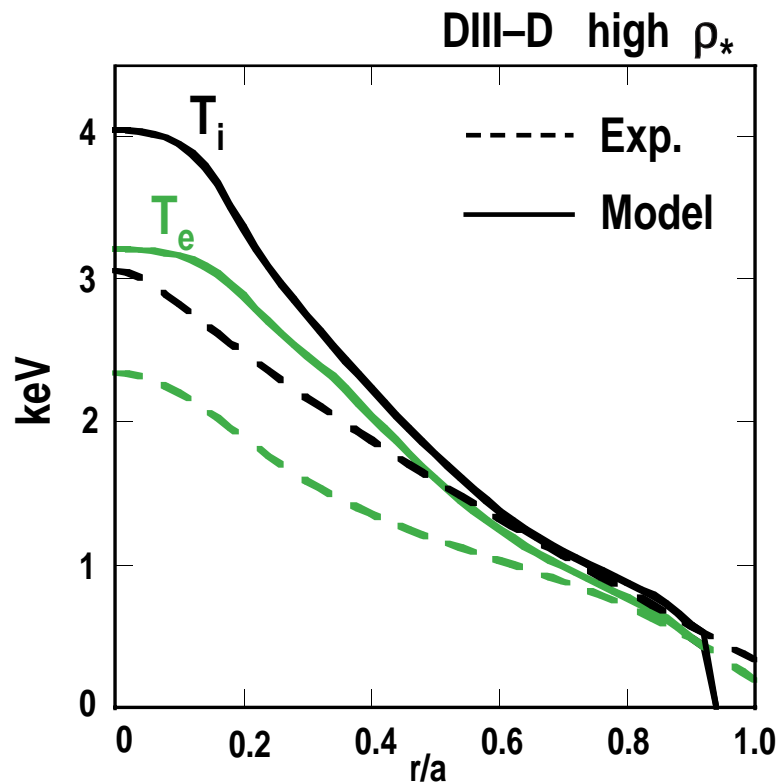
●  $\Delta R_w$  is the average error in the total plasma stored energy

$$\Delta R_w = \sqrt{\sum_i \left( \frac{W_{si}}{W_{xi}} - 1 \right)^2 / N}$$



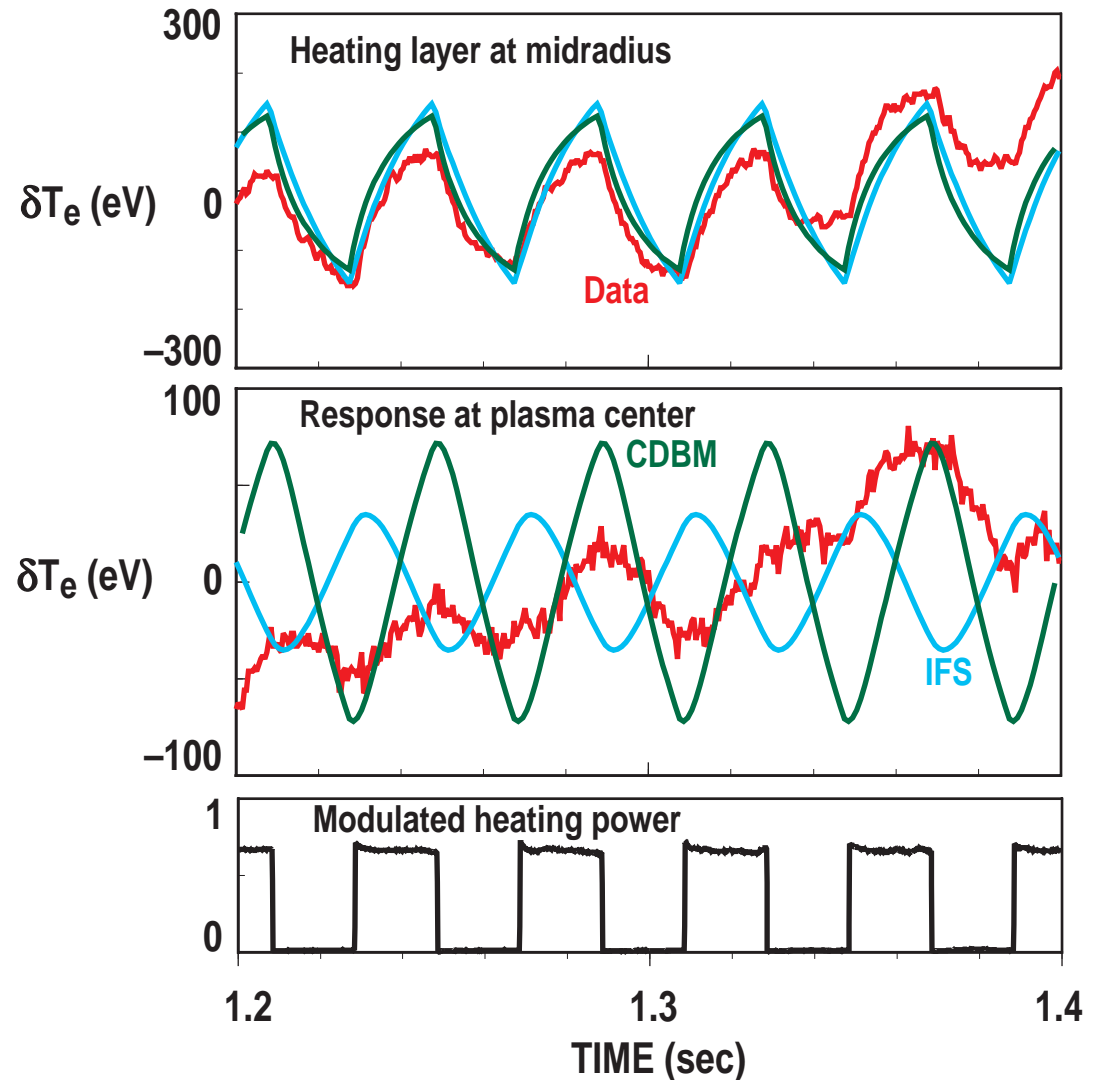
# A PLASMA EDGE PEDESTAL MODEL IS REQUIRED

- Present transport models deal in the plasma interior ( $r/a < 0.9$ )
- Predictions of future machine performance depend critically on the edge temperature



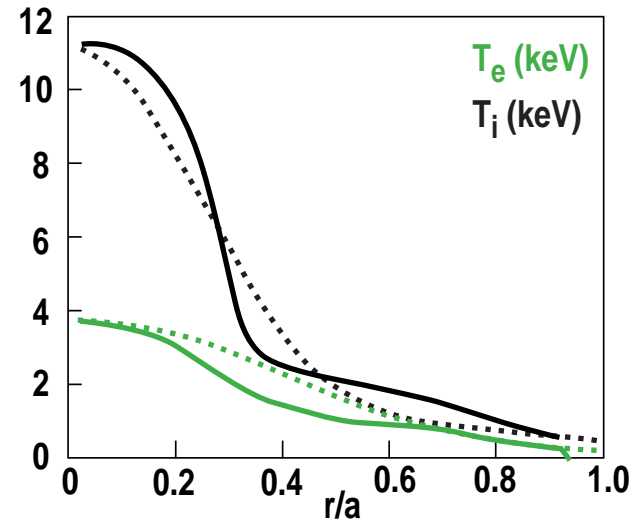
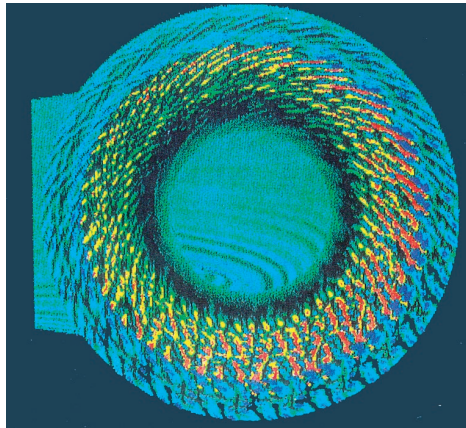
# MODELS RESPONSE TO MODULATED HEATING PROVIDES A MORE SENSITIVE VALIDATION TECHNIQUE

- Electron response to modulated ECH is measured with a fine temporal and spatial resolution
- Two different physics models predict similar behavior at the heating location but different behavior at the plasma center

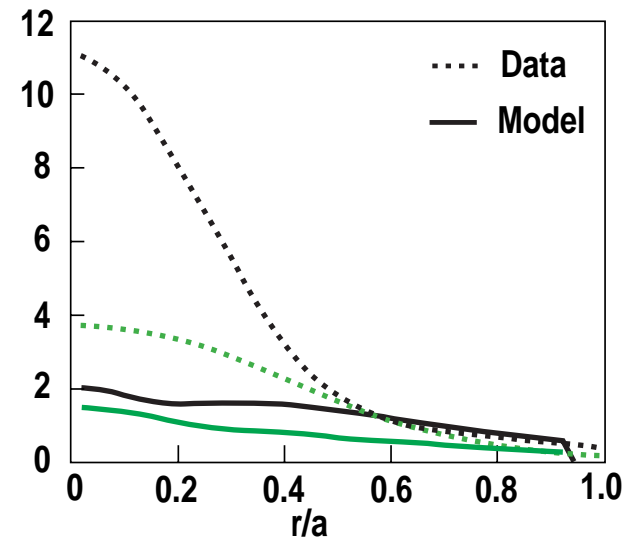
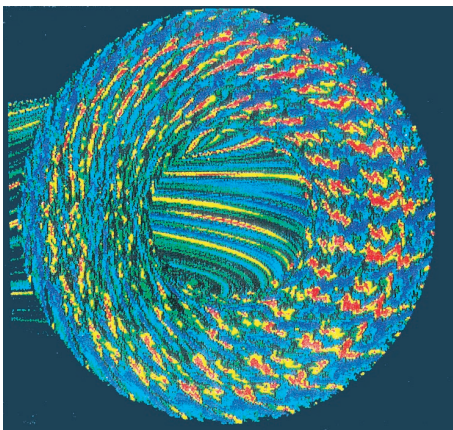


# MODELS ARE EVOLVING AS FURTHER PHYSICAL EFFECTS ARE INCLUDED

With  $E \times B$  flow shear



Without  $E \times B$  flow shear



- Gyrofluid simulation of toroidal ITG turbulence
- Turbulence decorrelation and stabilization by sheared  $E \times B$  flow
- Application of  $E \times B$  shear breaks up eddies and considerably reduces transport by a factor of ten
- For details see Burrell's talk at this conference (WB21.04 ,Thursday 15:30)