

# **NIMROD**

## **FROM THE CUSTOMER'S PERSPECTIVE**

**MING CHU**  
*General Atomics*

**Nimrod Project Review Meeting**  
**July 21 – 22, 1997**

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# OUTLINE

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- I. **Summary of  $\beta$  (MHD) Research**
  - 1.  **$\beta$  Limit is Determined by Ideal MHD**
    - $\alpha$ . **Troyon Scaling Law Verified**
    - $\beta$ . **Dependence on Global Profile**
  - 2. **Nonideal MHD Modes Observed at the  $\beta$  Limit**  
**— Plasma Rotation and Kinetic Effects Important**
    - $\alpha$ . **Resistive Plasma Modes**
    - $\beta$ . **Resistive Wall Modes**
  - 3.  **$\beta$  Limit Dynamics Depend on 3-D Effects**
    - $\alpha$ . **Nonlinear Free Boundary Modes**  
**— Vertical Displacement, External Kinks**
    - $\beta$ . **Nonlinear Development of Magnetic Field**

## OUTLINE (Continued)

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### II. Challenges in MHD for ITER and Large Tokamaks

1.  $\beta$  Limits of Steady-State Tokamaks
2. Disruption Dynamics
3. More 3-D MHD

### III. Survey of Existent (Nonlinear) MHD Codes

### IV. Desirable Features of NIMROD

### V. Validation Issues

1. Internal Consistency
2. Check with Known Linear Codes
3. Check with Other Nonlinear Codes
  - $\alpha$ . Scenario Development
  - $\beta$ . Quantitative Comparison

# IDEAL MHD THEORY PREDICTS A SIMPLE BETA LIMIT SCALING

- NUMERICAL CALCULATIONS (1982–1984)

- $\beta(\max) \propto \frac{I(\text{MA})}{a(\text{m}) B(\text{T})}$  "Troyon scaling." Define  $\beta_N = \frac{\beta(\%)}{I/aB}$
- $\beta_N(\max) = 2.8 - 3.2$  Ideal  $n = 1$  kink mode (Troyon, Tuda).
- $\beta_N(\max) = 3.7 - 4.4$  Ideal  $n = \infty$  ballooning (Sykes, Bernard, Tuda).

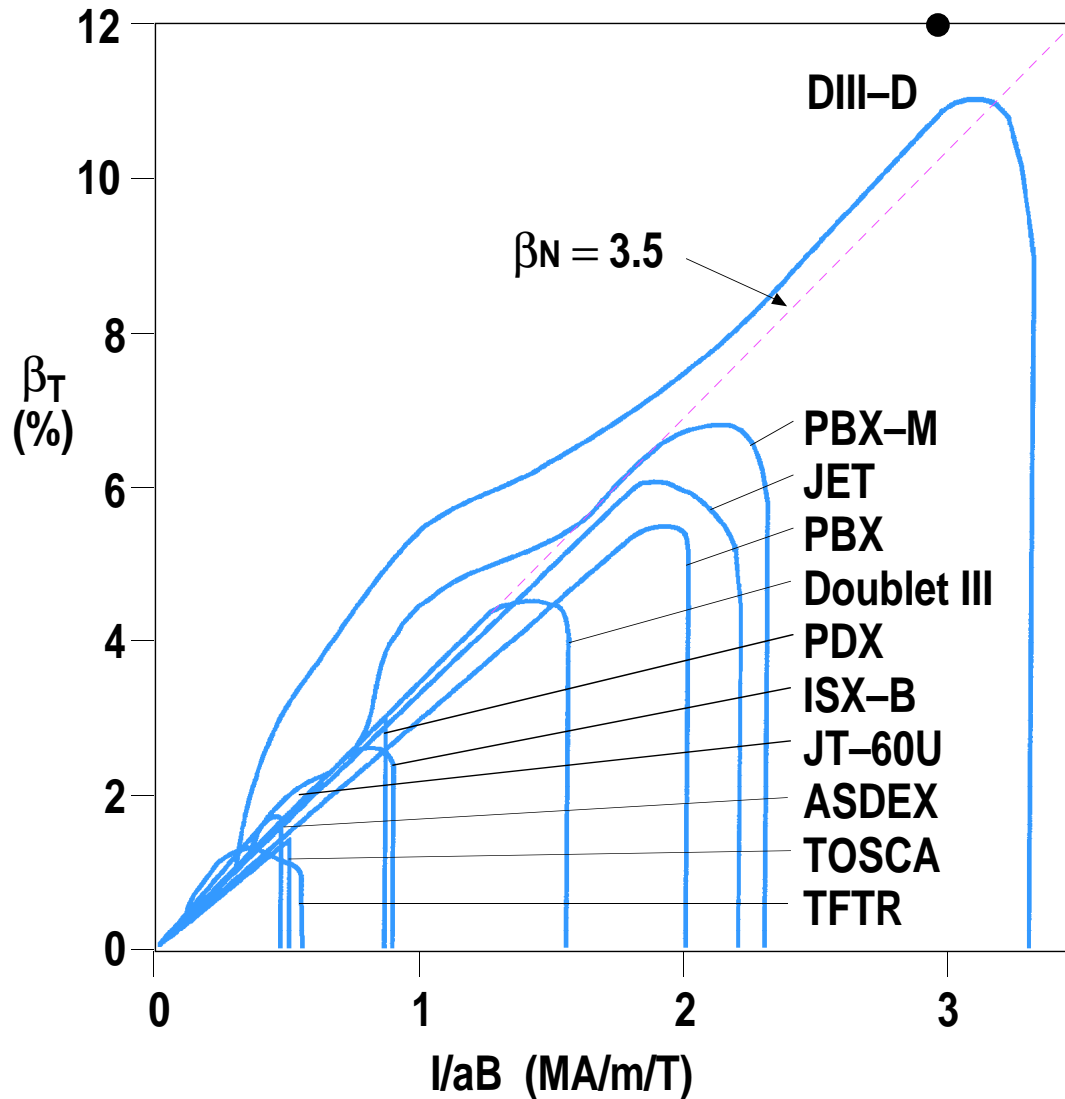
- EXPERIMENTS:

- $\beta_N(\max) \approx 3.5$  "Standard."
- $\beta_N(\max) \leq 6$  With profile modification.

- ANALYTIC CALCULATIONS:

- $\beta(\max) = 28 \frac{\epsilon}{q} = 5.6 \frac{I}{aB}$  Troyon scaling derived for simplified profiles (Wesson).
- High- $n$  and low- $n$  limits become the same for  $q \gg 1$ . Asymptotic scaling (Ramos).

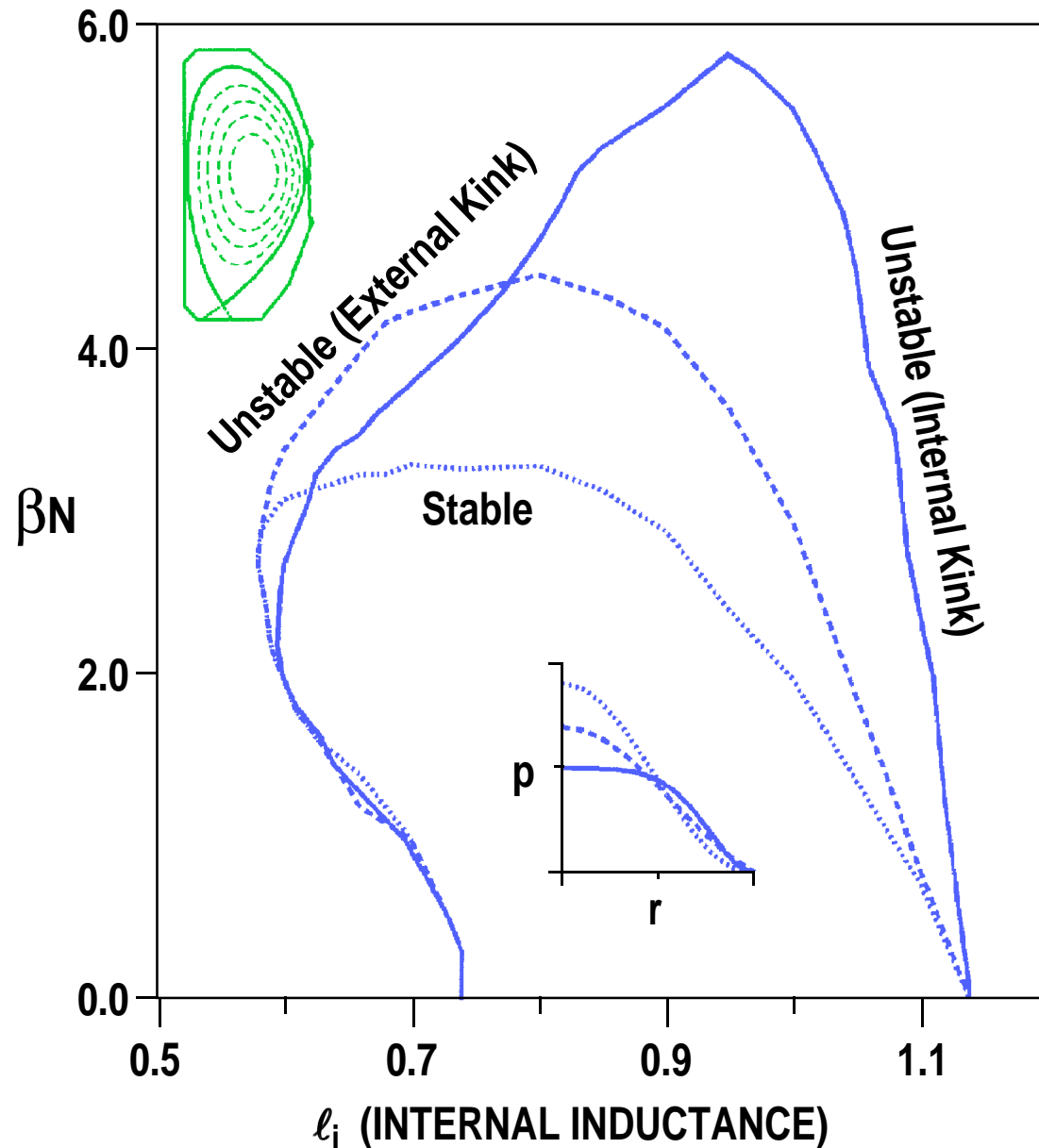
# EXPERIMENTS CONFIRM BETA LIMIT SCALING



$$\beta_N(\text{max}) = 3.5 \pm 0.5$$

$I/aB$  is limited by current-driven kink instabilities at  $q \approx 2$ .

# BETA LIMIT INCREASES WITH OPTIMIZATION OF PROFILES



- Theoretical calculations predict  $n = 1$  kink stability improves with broad  $p(r)$  and peaked  $J(r)$  (high  $\ell_i$ ).
- High  $\ell_i$  increases magnetic shear near the plasma edge, improves stability for larger edge pressure gradient.
- Experimentally confirmed in DIII-D, TFTR, JET, JT-60U.

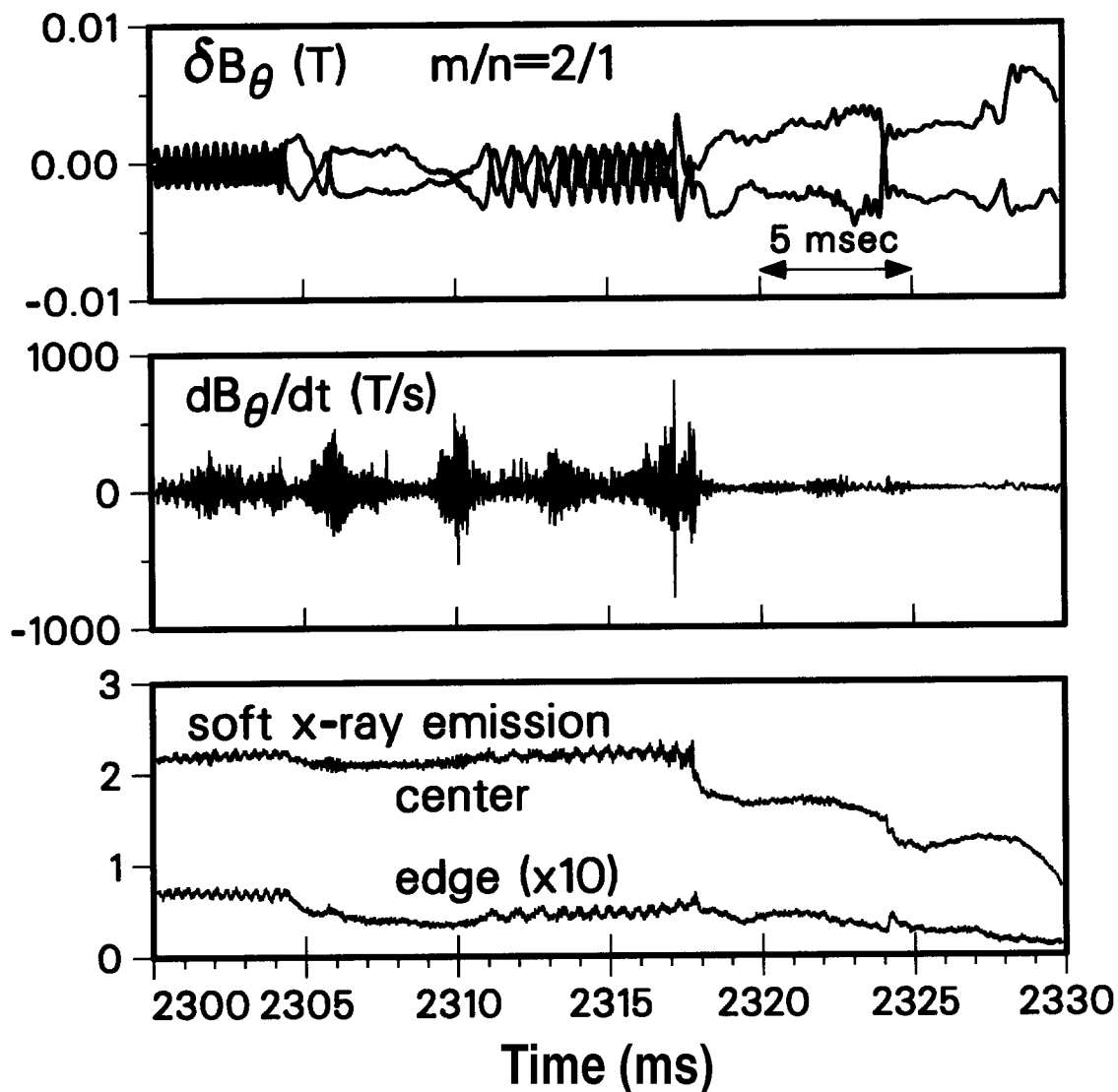
# NONIDEAL MHD MODES OBSERVED AT THE $\beta$ LIMIT PLASMA ROTATION AND KINETIC EFFECTS IMPORTANT

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- Resistive Plasma Modes
- Locked Modes
- Sawtooth
- Edge Localized Modes (ELMs)
- Resistive Wall Modes

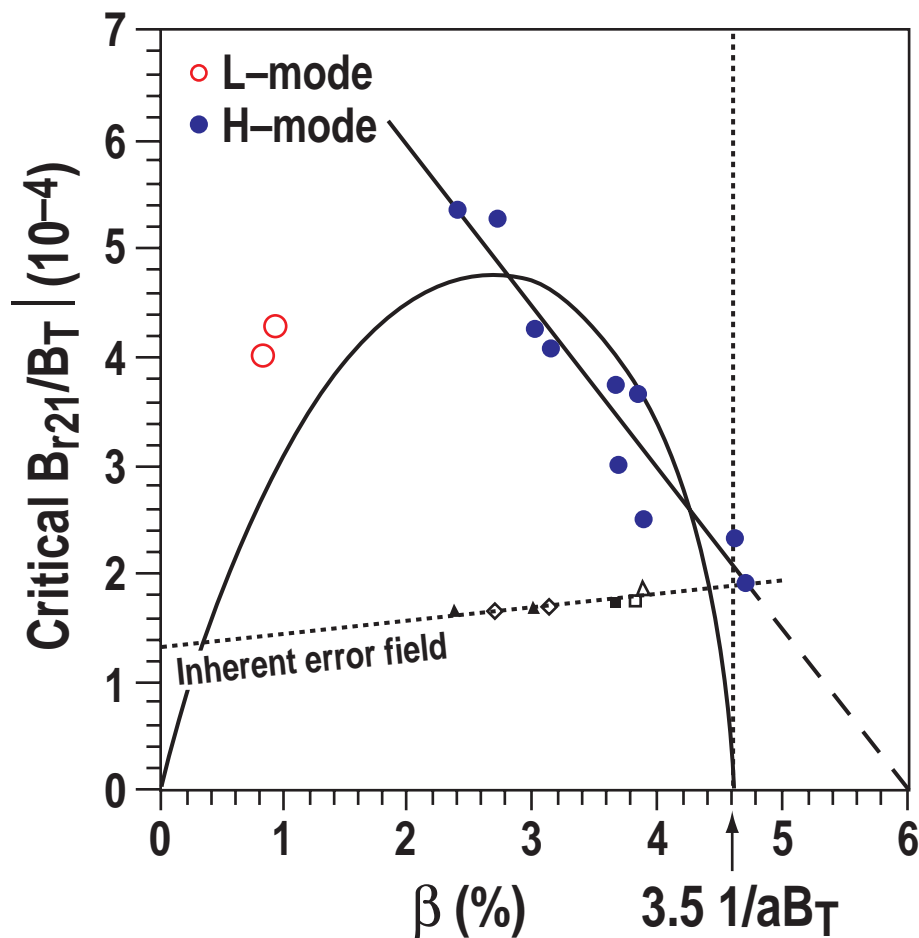
# DISRUPTION AT HIGH $\beta$ SHOWS STABILIZING EFFECT OF ROTATION

- Rotating  $m/n = 2/1$  locks after a sawtooth, then grows to disruption.
- Consistent with stabilization by a resistive wall:
  - $2/1$  mode is saturated while  $\omega_{\text{rot}} \tau_w \gg 1$
  - $2/1$  mode grows after it stops rotating,  $\gamma \lesssim \tau_w^{-1}$



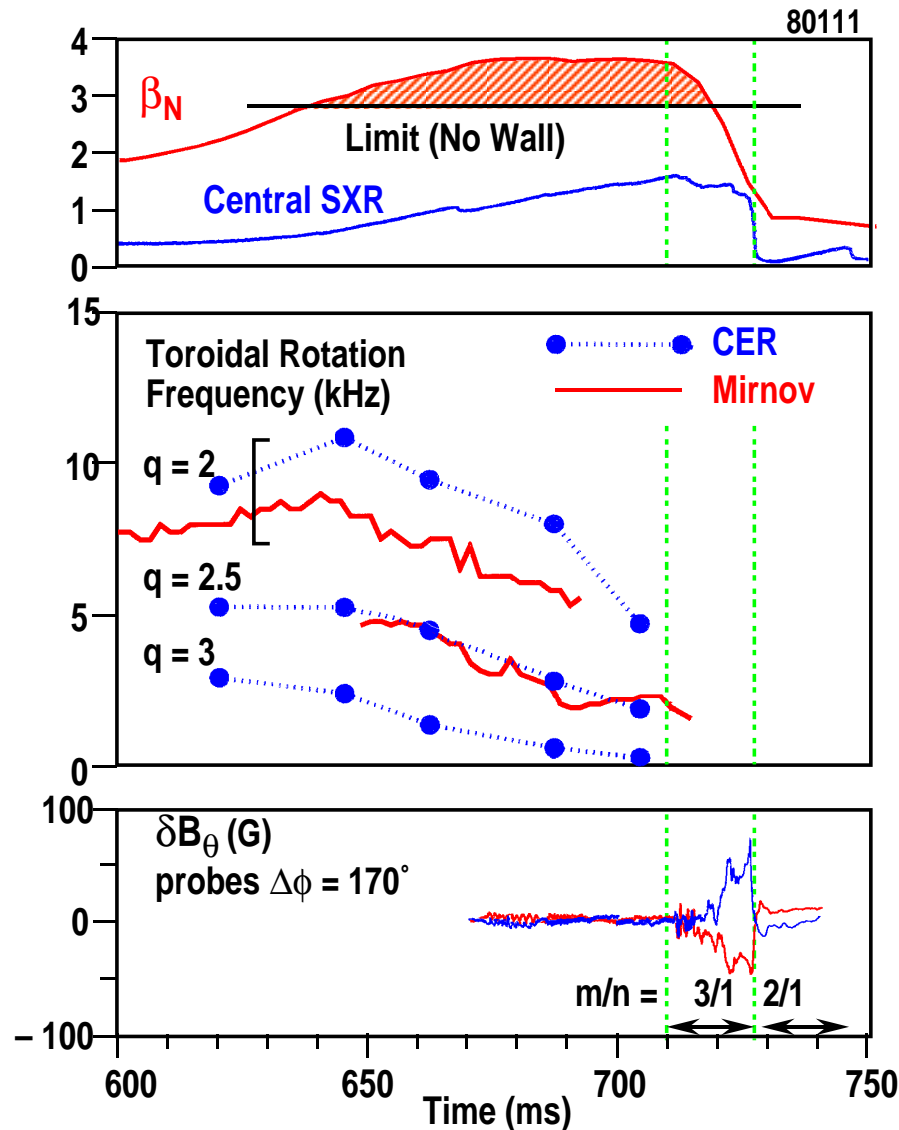


THE CRITICAL  $m = 2, n = 1$  RELATIVE ERROR FIELD FOR A LOCKED MODE DECREASES AS THE  $\beta$  LIMIT IS APPROACHED. THE INHERENT ERROR FIELD DUE TO F-COILS IS ALSO SHOWN



- DIII-D H-mode, SND,  $q_{95} = 3.5$ ,  $\kappa = 1.8$ , 1 MA, 1.2 T,  $5 \times 10^{19} \text{ m}^{-3}$
- Error fields can
  - Reduce  $\beta$  limit
  - Decrease reliability
  - Increase disruptivity

# COLLAPSE AT HIGH $\beta_N$ SHOWS IMPORTANCE OF ROTATION



- $m/n = 3/1$  mode becomes unstable when  $q = 3$  surface ceases to rotate

- $3/1$  mode has predicted features of “Resistive Wall Mode”

[1] E.J. Strait et al., Phys. Rev. Lett. 74 (1995) 2483; [2] T.S. Taylor et al., Phys. Plasmas 2 (1995) 2390.

# $\beta$ LIMIT DYNAMICS DEPEND ON 3-D EFFECTS

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$\alpha$ . Nonlinear free boundary modes

- Vertical displacement
- External kinks

$\beta$ . Nonlinear development of magnetic field

- Island topology
- Field line stochasticity

# CHALLENGES IN $\beta$ LIMITS OF STEADY-STATE TOKAMAKS

## MHD FOR ITER AND LARGE TOKAMAKS

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- Steady state equilibrium profiles
- Advanced tokamak equilibrium profiles
- Resistive wall boundary conditions (smart wall, rotating wall)
- Neoclassical resistive MHD
- Effect of energetic particles

# DISRUPTION DYNAMICS

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- Vertical displacement halo currents
- Avoidance of locked modes by rotation, error field control, and plasma profile control?
- Identification of disruption precursors
- Plasma dynamics during a disruption: heat, particle, and flux transport, and effect on production of energetic particles
- Disruption amelioration scenarios

## MORE 3-D MHD

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1. Bootstrap current phenomena — slow compared to collision frequencies
  - Development of 3-D neoclassical MHD islands
  - Bootstrap current associated with H-mode transport barrier gradients
    - Extent and geometry of ELMs (energy goes to *inside* divertor plate!!)
    - Separatrix geometry leads to avalanche (self-organized critically)
    - Instability → magnetic stochasticity → parallel heat loss → big  $\nabla P$  → Instability
    - Feedback, smart walls; fast particles
2. Effect of plasma rotation and resistive walls on evolution pressure-driven resistive wall modes
  - High-bootstrap-fraction, “advanced” discharges rely on walls for stabilization of ideal MHD kinks (low-n) modes
3. Error field criteria (possibly neoclassical)
4. Sawteeth reconnection (deviations from Kadomtsev)

Courtesy F. Perkins

## DESIRABLE FEATURES OF NIMROD

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- \* Two Fluid Formulation
- \* Readily Available
- \* User Friendly
- \* Easy to Maintain
- \* Fast Turnaround

## CHARACTERISTICS OF MHD CODES

	MH3D	NFTC	MARS	FAR	XTOR	PIES	ARES	CTD	NIMROD
N.L. Res. MHD	X	X		X	X	X		X	X
Free Boundary N.L.									?
Neoclassical Tearing				X		X			X
Scrape-off Layer									?
Resistive Wall	X	X	X				X	X	X
$q < 1$	X	X	X	X	X		X	X	X
Two Fluid	X							X	X
Rotation		X	X					X	X
Predict Diagnostics	X								X
Fast Particles	X								?
Radial Element	General	F.D.	F.E.	F.D.	F.D.	F.D.	F.D.	F.D.	General
Fourier in Poloidal	X	X	X	X	X	X	X	X	novel
Fourier in Toroidal	X	X	X	X	X	X	X	X	X
Linear Regime	q. Imp	s. Imp	eig.	Imp.	s. Imp		eig.	s. Imp	General
Nonlinear Regime	q. Imp	s. Imp		exp.	s. Imp	iter.		s. Imp	General



# VALIDATION ISSUES

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1. Internal self-consistency of the code
2. Check with known linear codes
  - GATO
  - DCON
  - MARS
3. Check with known nonlinear codes
  - MH3D
  - XTOR
  - CTD
  - NEOFAR
- $\alpha$ . Scenario development
  - Halo current
  - Disruption
- $\beta$ . Quantitative comparison
  - Nonlinear stability boundary