

# **Comparison of Critical Values of $R/L_{Te}$ for ETG Modes Based on an Analytic Expression with GKS Simulations for DIII-D Discharges**

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# Motivation

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- Understanding electron thermal transport remains a key area of study in the overall understanding of transport in tokamak plasmas.
  - Electron Temperature Gradient (ETG) modes can lead to enhanced electron heat flux when coupling of these modes leads to the formation of so called streamers.
  - Full gyrokinetic stability (GKS) code calculations can be used to find the critical electron temperature gradient scale length for ETG modes but the code requires significant computing time.
  - An analytic expression for  $(R/L_{Te})_{crit}$  can be useful if accurate enough
- ∴ **Compare an analytic expression for  $(R/L_{Te})_{crit}$  with GKS code results**

## **Expression for $(R/L_{Te})_{crit}$ for ETG Modes From Jenko\***

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$$(R/L_{Te})_{crit} = \max\{(1 + \tau)(1.33 + 1.91s/q) \\ \times (1 - 1.5\varepsilon)[1 + 0.3\varepsilon(d\kappa/d\varepsilon)], 0.8R/L_n\}$$

**For magnetic shear  $s \geq 0.2$**

**and normalized pressure gradient  $\alpha \leq 0.1$**

**Where  $s = (r/q)(dq/dr)$  ;  $\alpha = -q^2R(d\beta/dr)$  ;  $\tau = Z_{eff}(T_e/T_i)$  ;**

**$\varepsilon = r/R_0$  ;  $\kappa = \text{elongation}$  and  $R/L_n = (R/n)(dn/dr)$**

\*F. Jenko, W. Dorland and G.W. Hammett, Phys. Plasmas **8** (2001) 4096

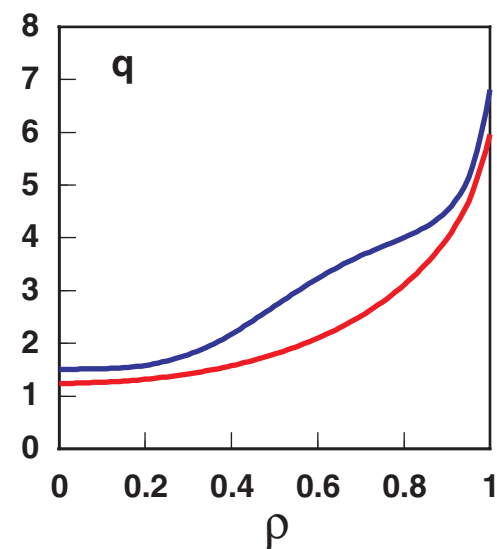
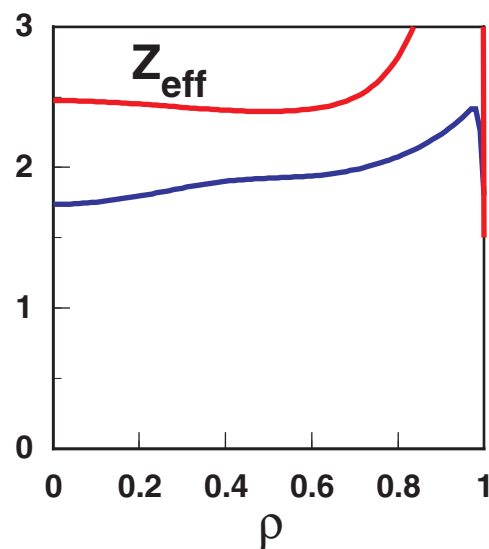
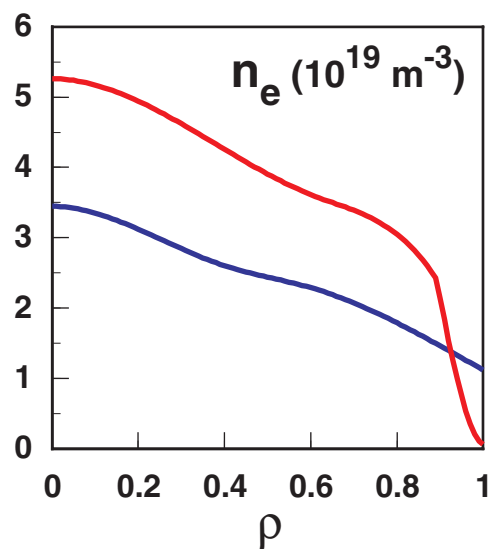
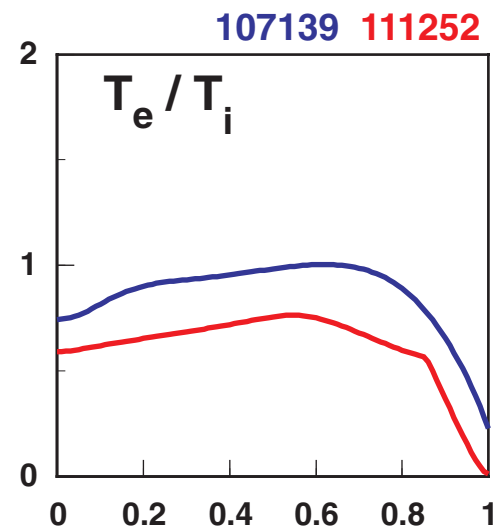
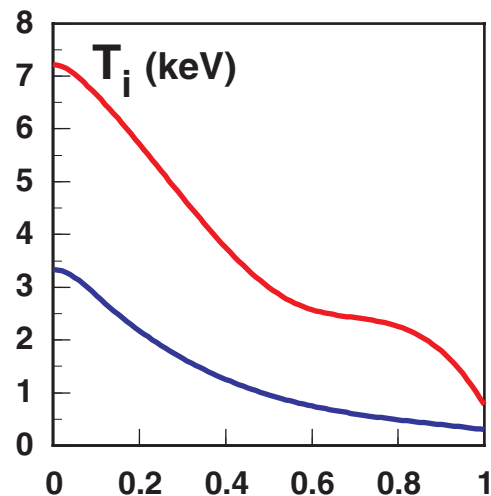
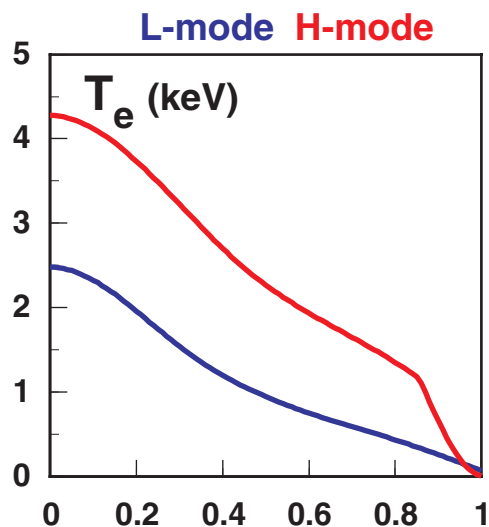
# Experimental Profiles From DIII-D Discharges Used For Comparison

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- **Three pairs of discharges studied**
  - L-mode vs H-mode: compares varying  $T_e/T_i$  with both  $T_e$  and  $T_i$  varied
  - L-mode pair 107564 and 107567: vary  $T_e/T_i$  with fixed  $T_i$
  - L-mode pair 106740 and 106748: vary  $s/q$  by varying  $q$
- **General discharge characteristics**

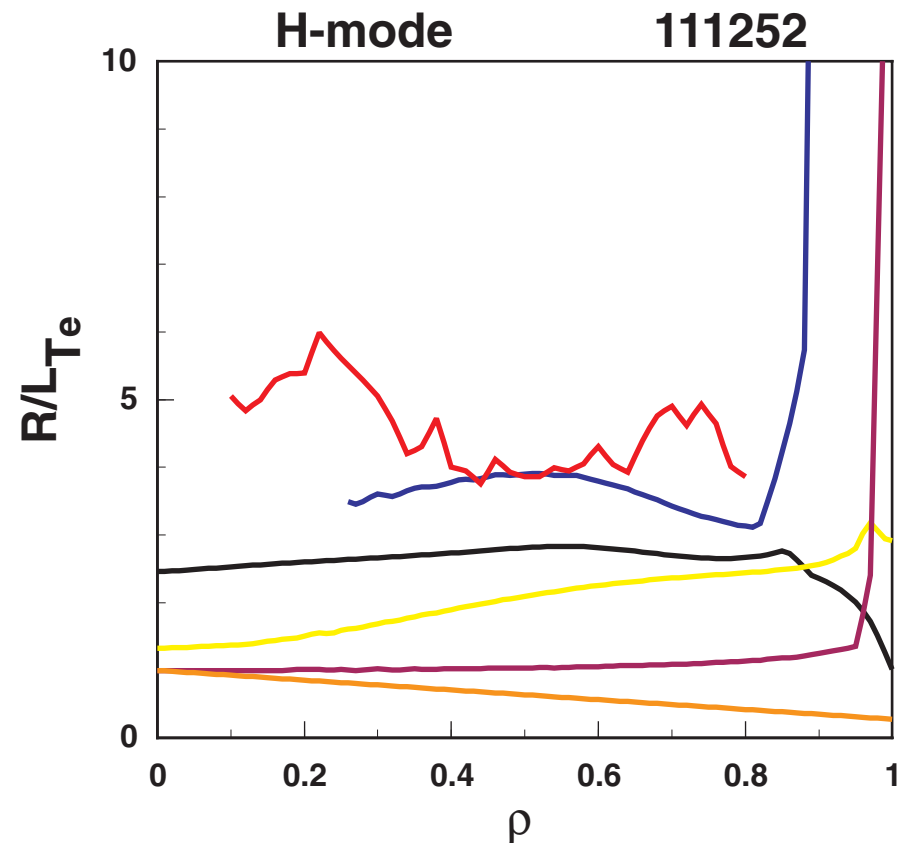
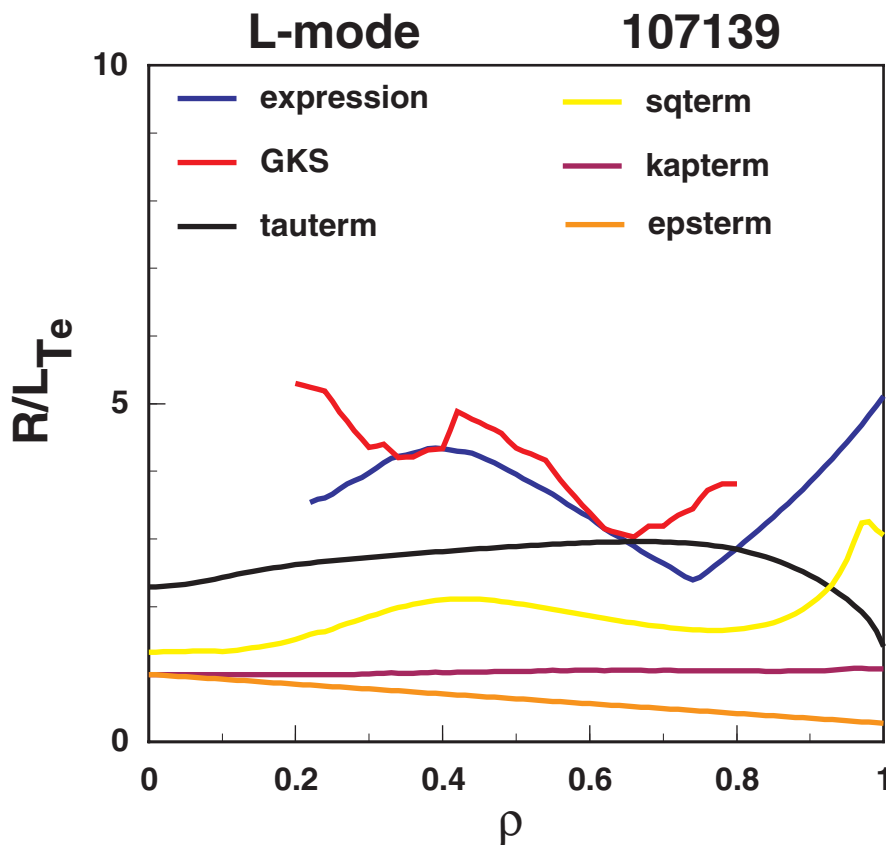
	<u>L-Mode</u>	<u>H-Mode</u>
$B_T$ (T)	2.0	1.9
$I_p$ (MA)	0.8-1.5	1.3
$n_e(10^{19}\text{m}^{-3})$	1.9-2.6	3.6
K	1.4-1.6	1.8

# Comparison of L-Mode and H-mode Profiles



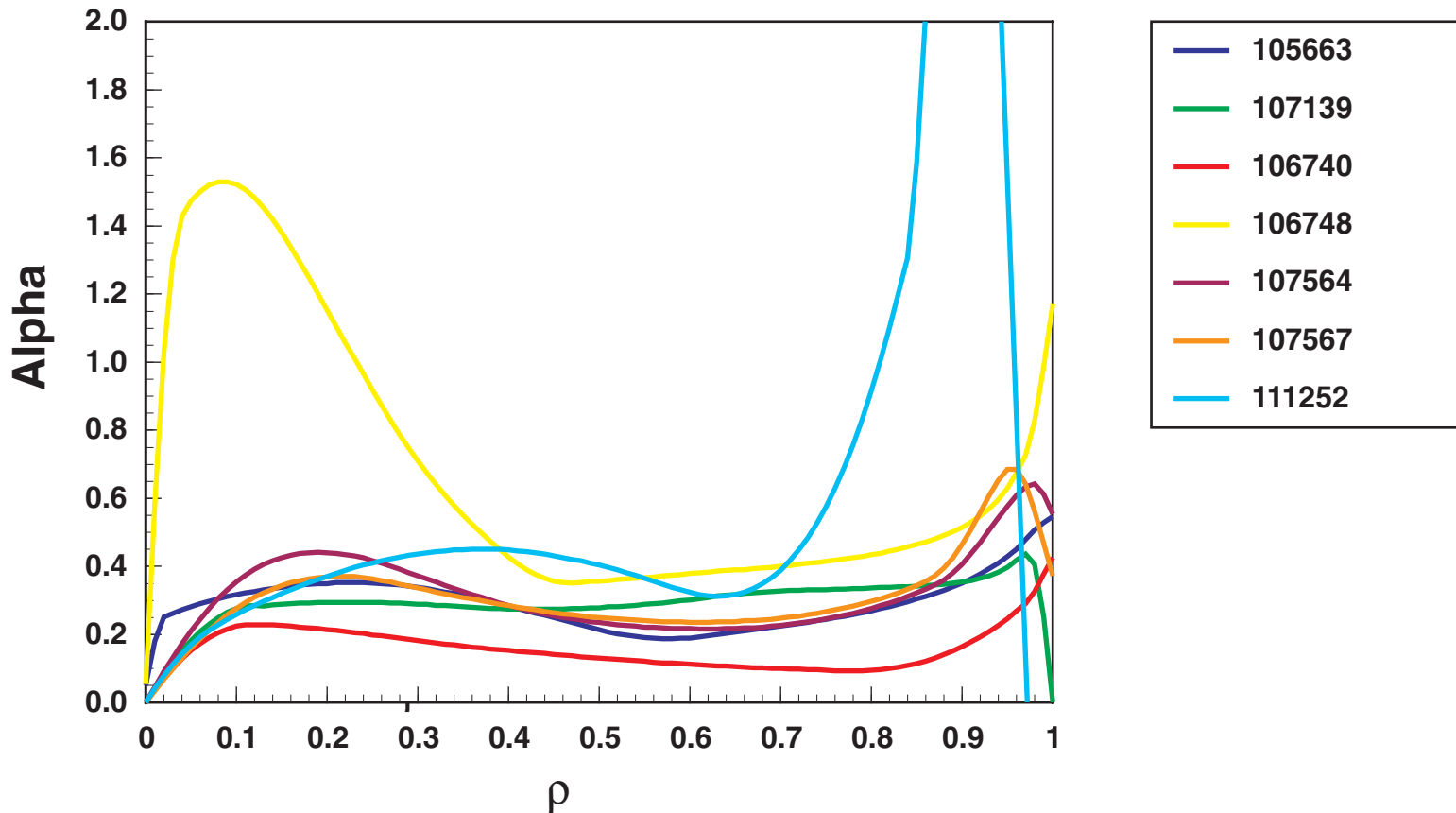
# Analytic Expression Agrees Reasonably Well With GKS Code And Shows Similar Trend Across Plasma

- Analytic expression not evaluated where  $s < 0.2$
- The two most dominant terms in the analytic expression are the terms containing  $\tau = Z_{\text{eff}} T_e / T_i$  and  $s/q$

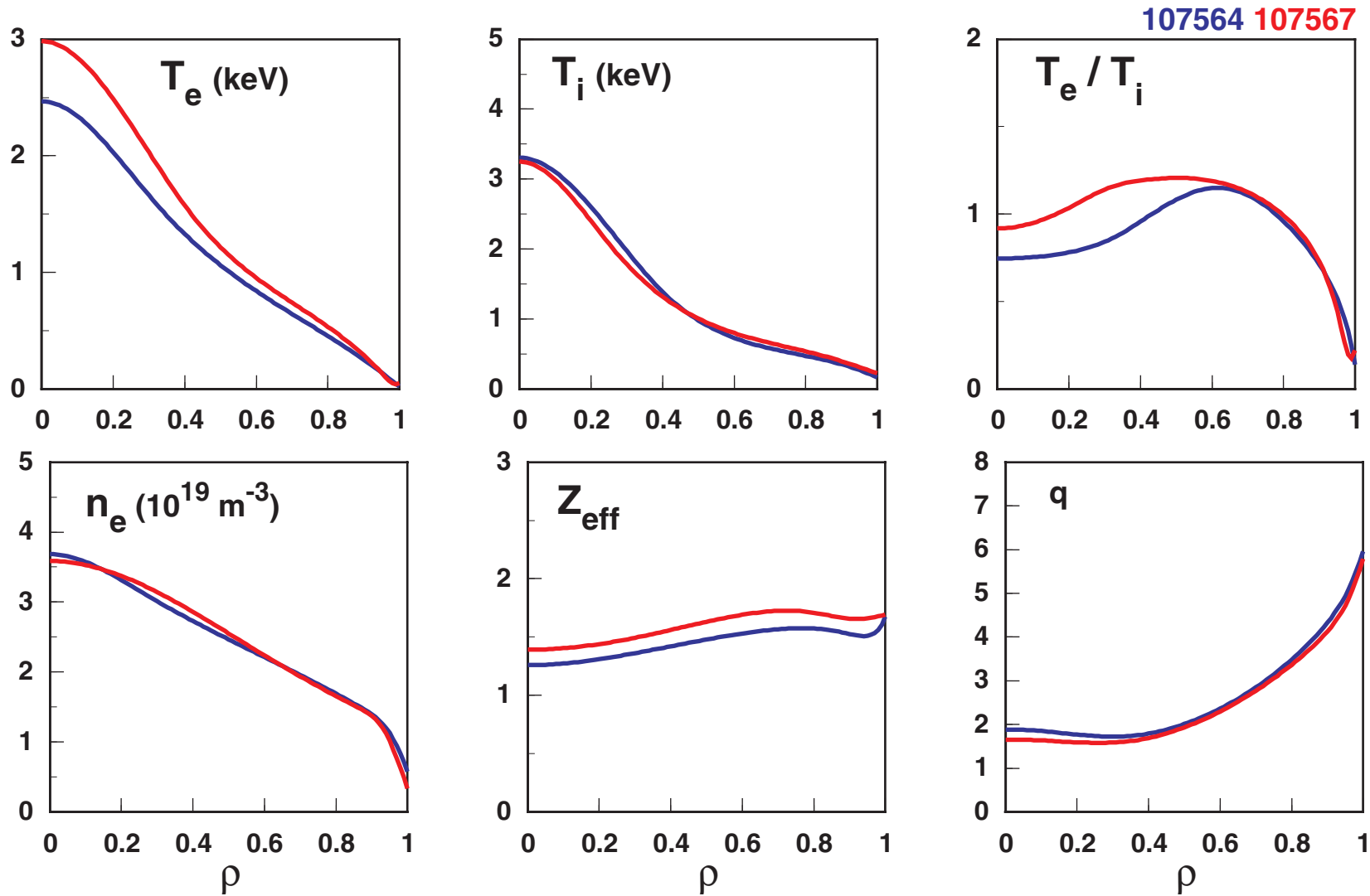


# Alpha Values Are Close To But Typically Above The Model Criteria For Applicability

- The model is expected to be applicable to Tokamak discharges with  $\alpha \leq 0.1$



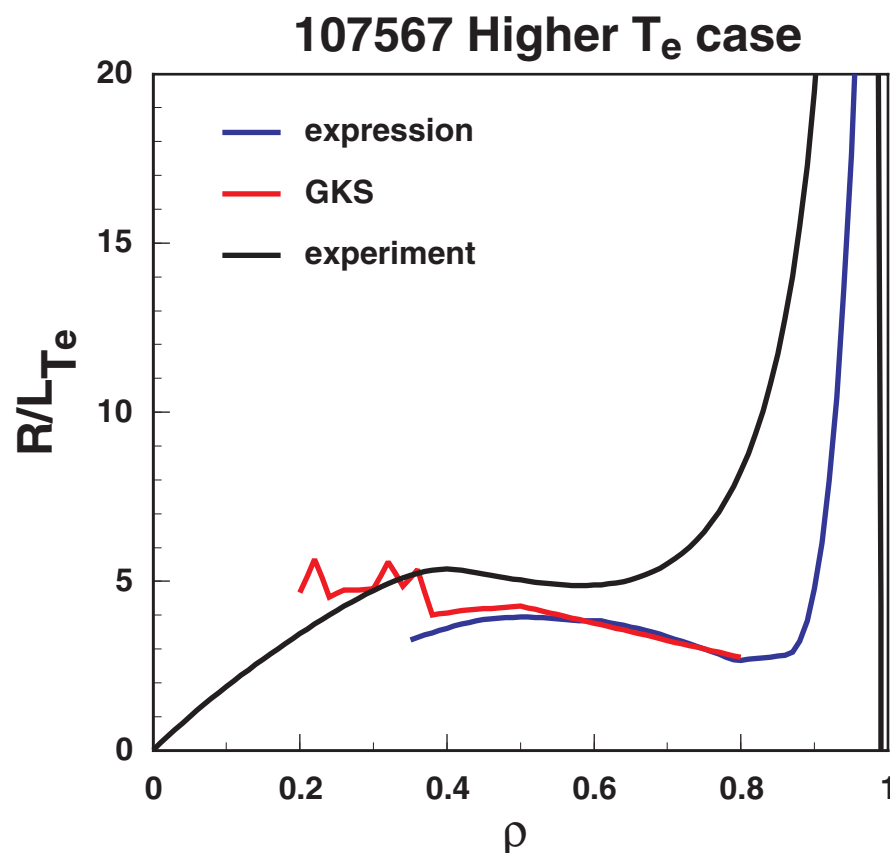
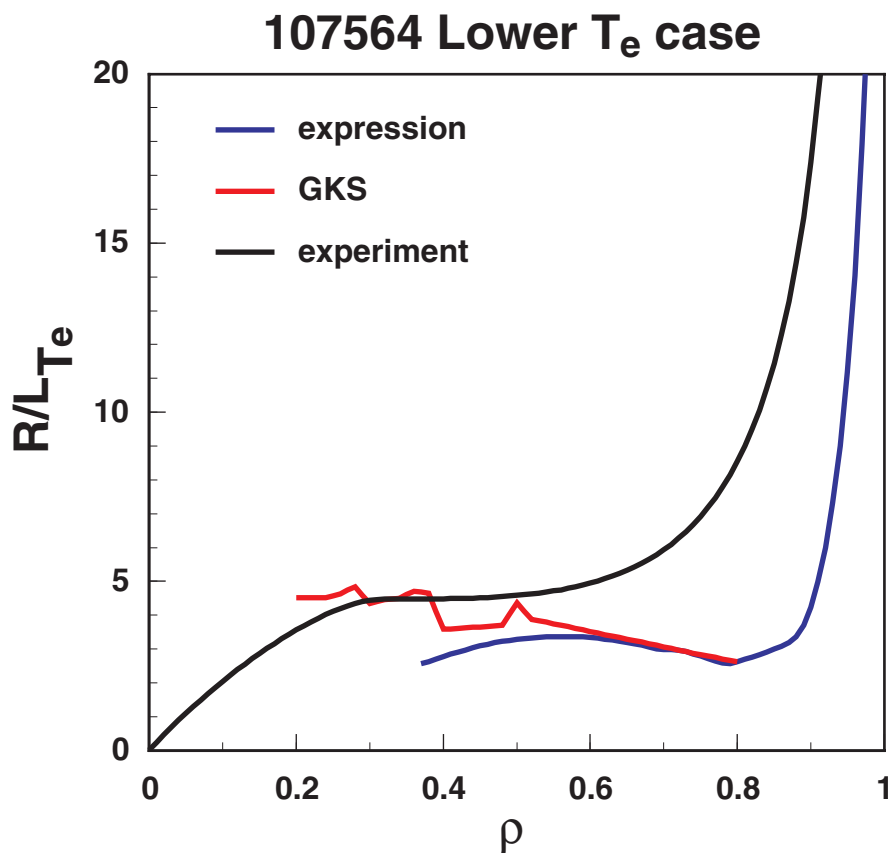
# Plasma Profile Comparison For $T_e$ Variation At Fixed $T_i$



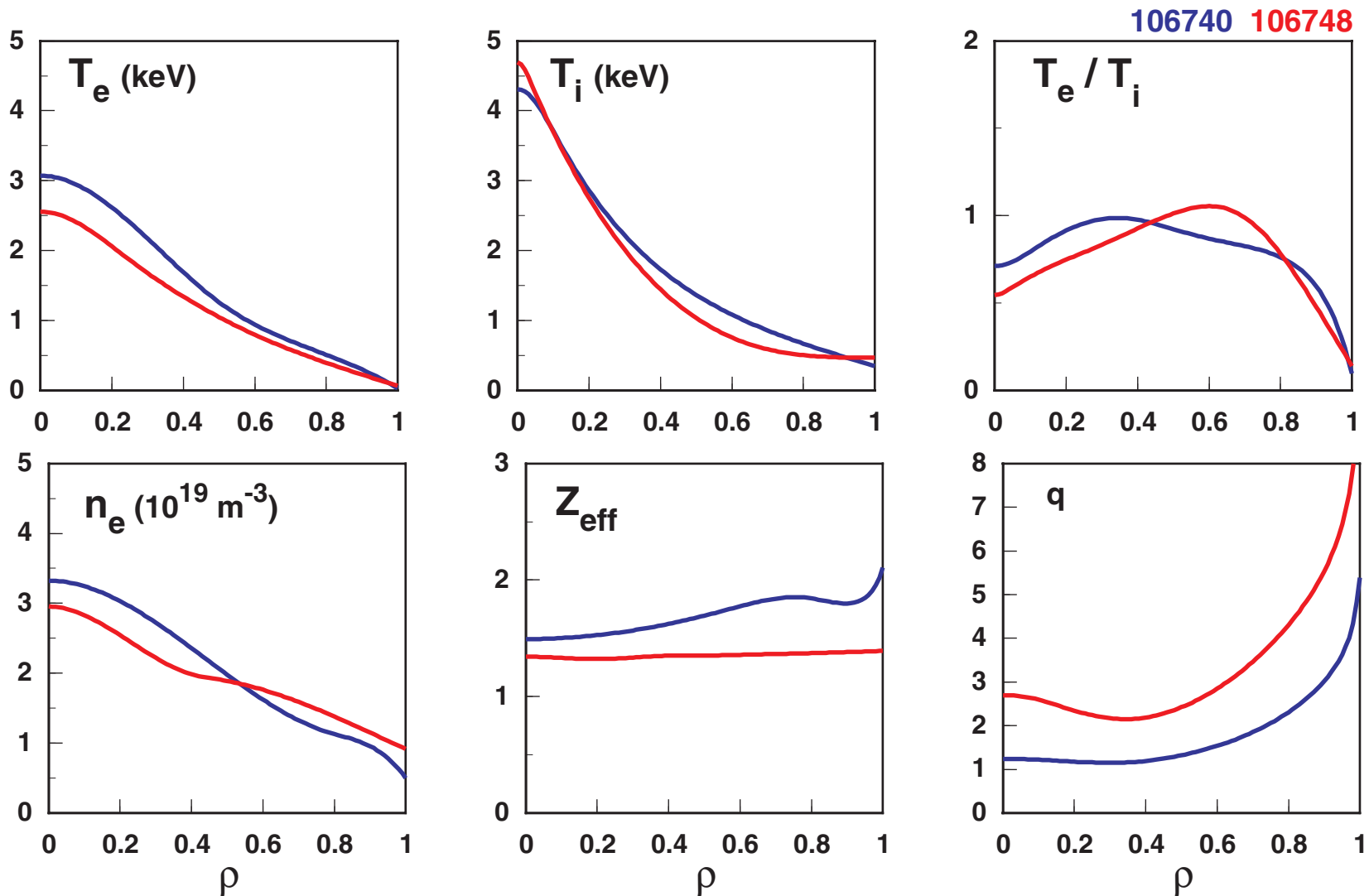


# Agreement Between GKS Code Results and Analytic Expression Remains Good with $T_e/T_i$ Variation

- Excellent agreement toward outside of plasma
- Agreement becomes worse in region where  $T_e/T_i$  begins to differ in the two discharges

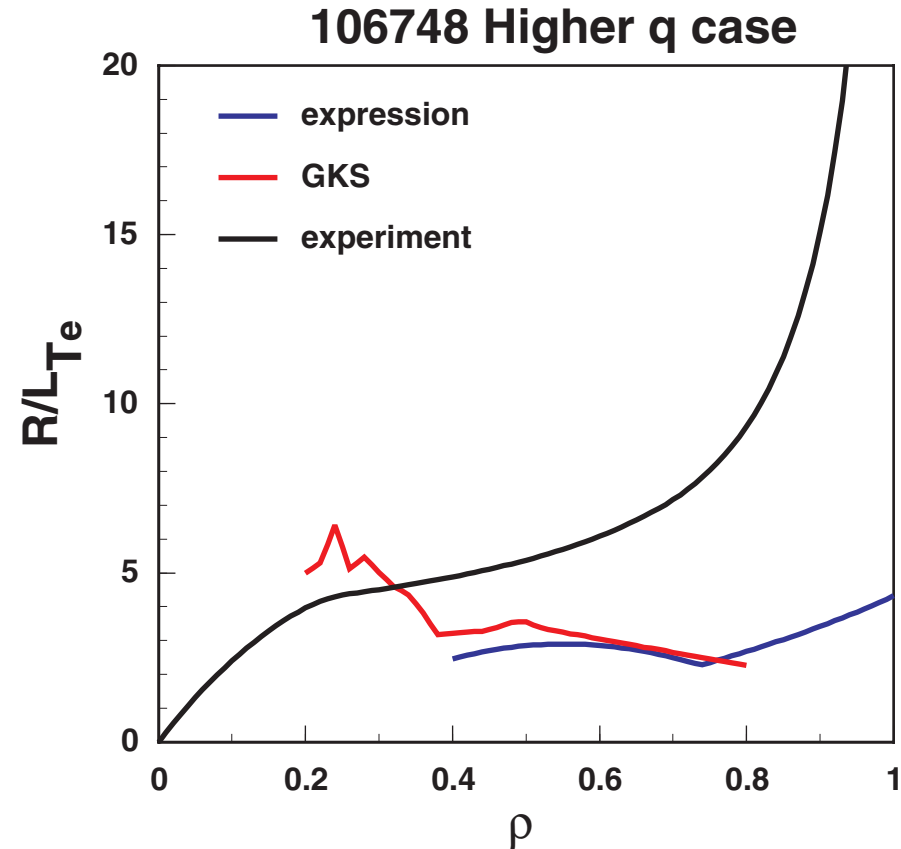
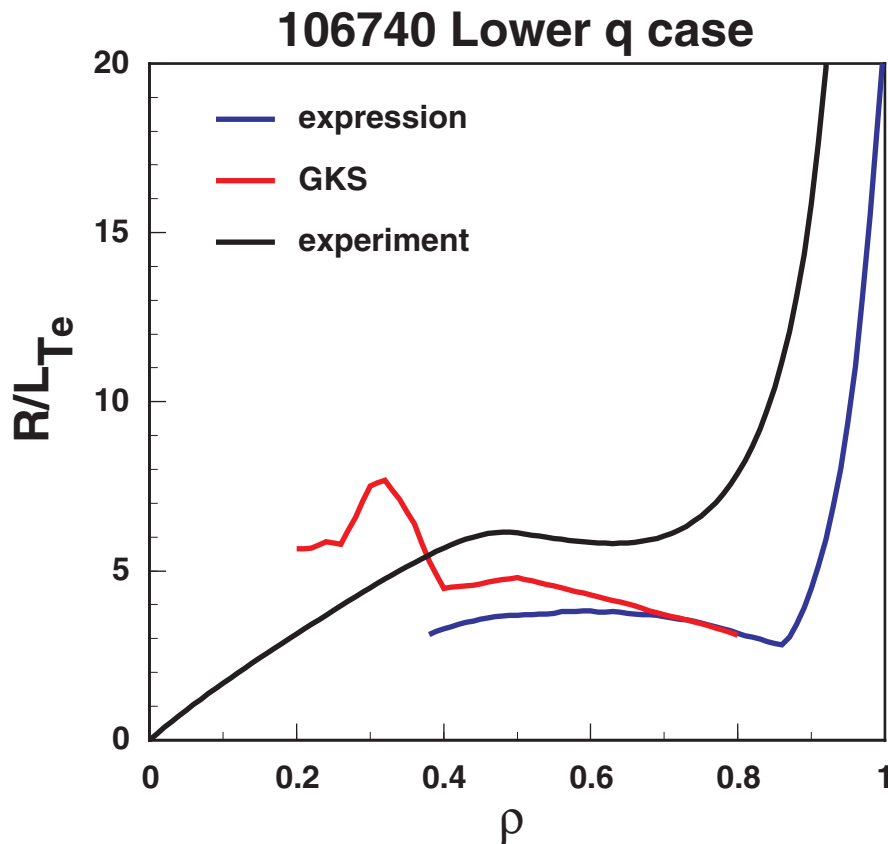


# Plasma Profile Comparison At Two q Values



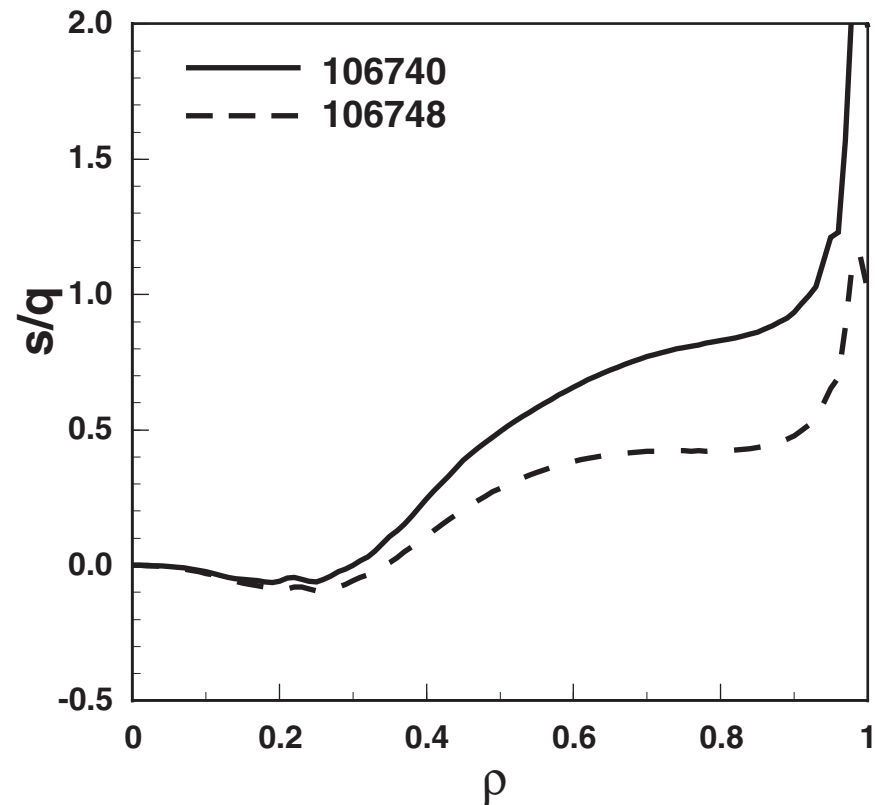
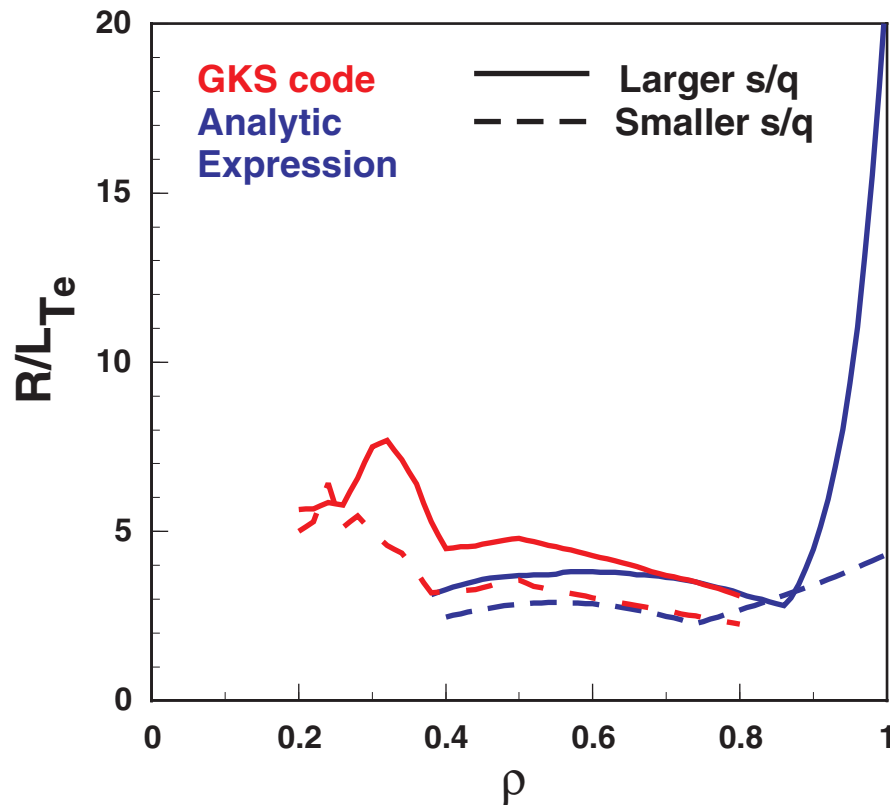
# Agreement Between GKS Code Results and Analytic Expression Remains Good At Low and High $q$ Values

- Agreement improves toward outside of plasma where  $s/q$  is larger



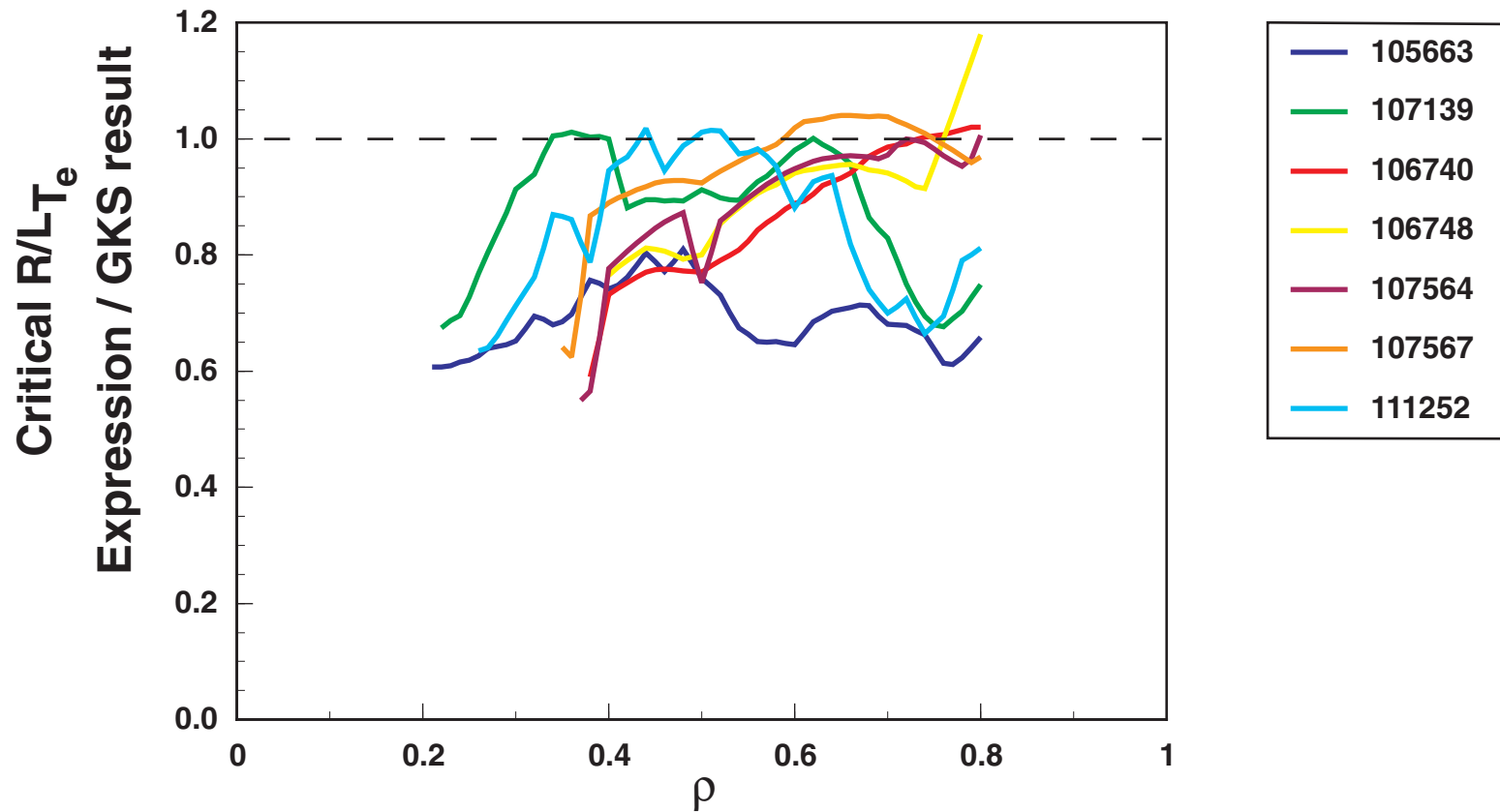
# Larger $s/q$ Is Stabilizing For ETG Modes

- The critical  $R/L_{Te}$  is larger at larger  $s/q$



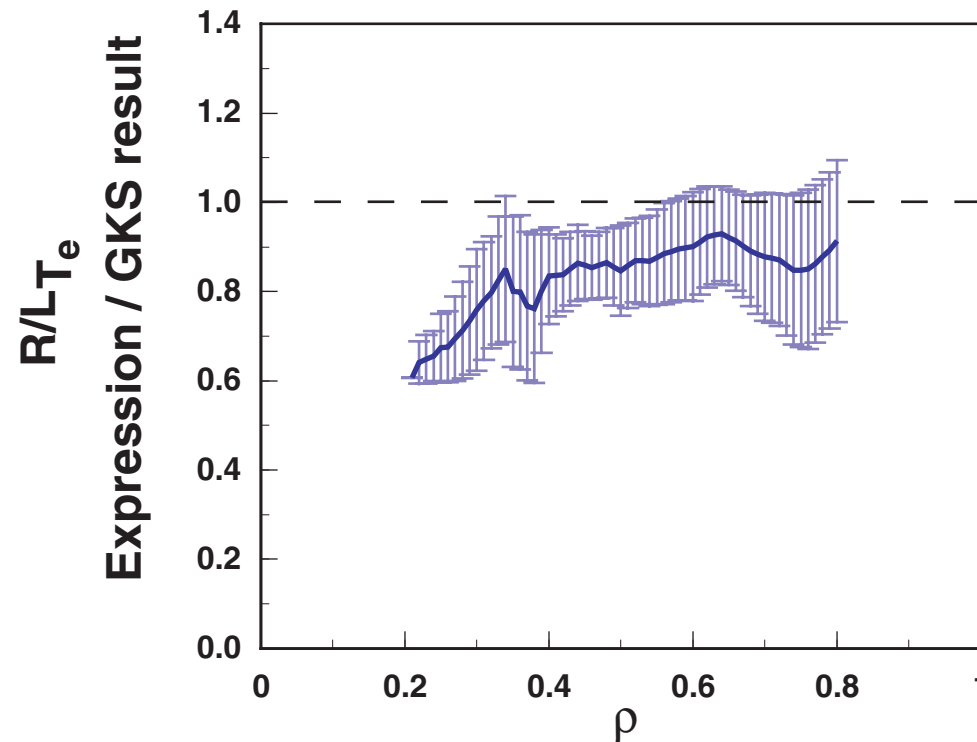
# $R/L_{T_e}$ Values From The Expression Are Systematically Below Values From The GKS Code, But Are Generally Within 30 %

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# When Averaged Over All Cases Studied A Slight Trend Toward Better Agreement Is Observed Toward The Plasma Edge

- Values from the expression are averaged by radial location over all cases studied
- Error bars represent  $\pm 1 \sigma$  in the distribution



# SUMMARY

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- Critical  $R/L_{Te}$  values for ETG modes from the GKS code were compared to values from an analytic expression developed in F. Jenko, et al., Phys. Plasmas 8 (2001) 4096.
- Although the region of applicability of the expression is marginally violated for the normalized pressure gradient  $\alpha$  ( $\alpha \leq 0.1$ ) for the experimental discharges studied, the expression agrees reasonably well with GKS code calculations.
- $R/L_{Te}$  values from the expression are systematically below values from the GKS code but are generally within 30% of GKS results with a slight trend toward better agreement toward the plasma edge.