

# Optimization of the Safety Factor Profile for High Noninductive Current Fraction Discharges in DIII-D

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# Introduction

# In a Steady-State Tokamak the q Profile is Closely Coupled to Both Transport Coefficients and Noninductive Current Sources

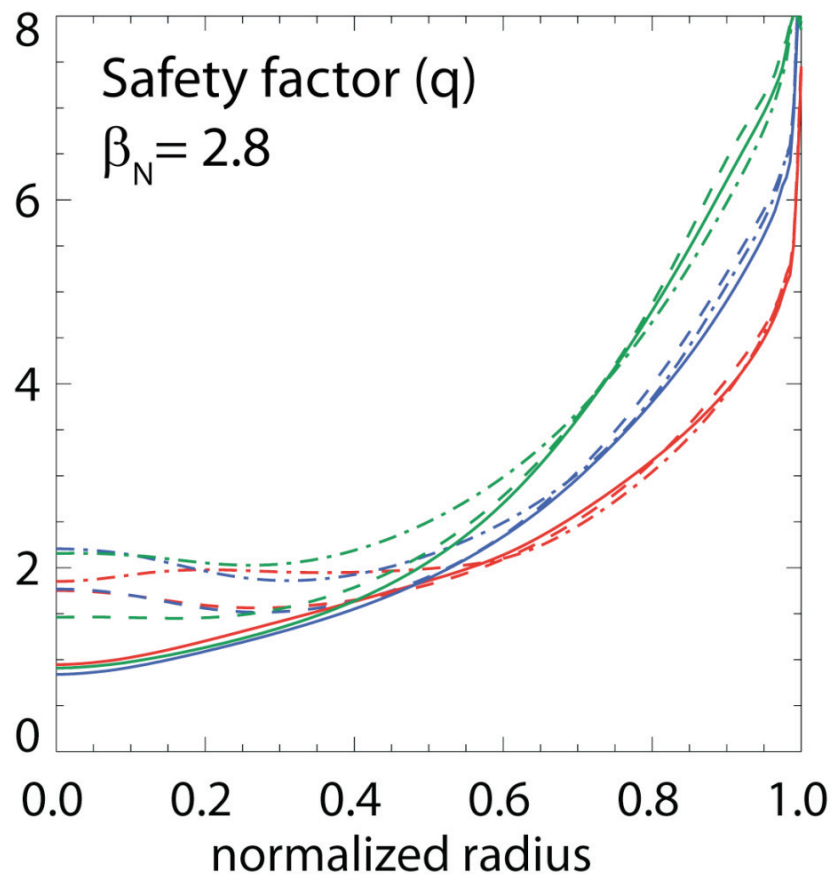
- **Bootstrap:** depends on n, T profiles, local q

$$\langle\langle J_{BS}B \rangle\rangle = -\frac{Fq}{B_{T0}\rho} \left[ T_e \frac{\partial n_e}{\partial \rho} L_{31} + n_e \frac{\partial T_e}{\partial \rho} (L_{31} + L_{32}) + T_i \frac{\partial n_i}{\partial \rho} L_{31} + n_i \frac{\partial T_i}{\partial \rho} (L_{31} + \alpha L_{34}) \right]$$

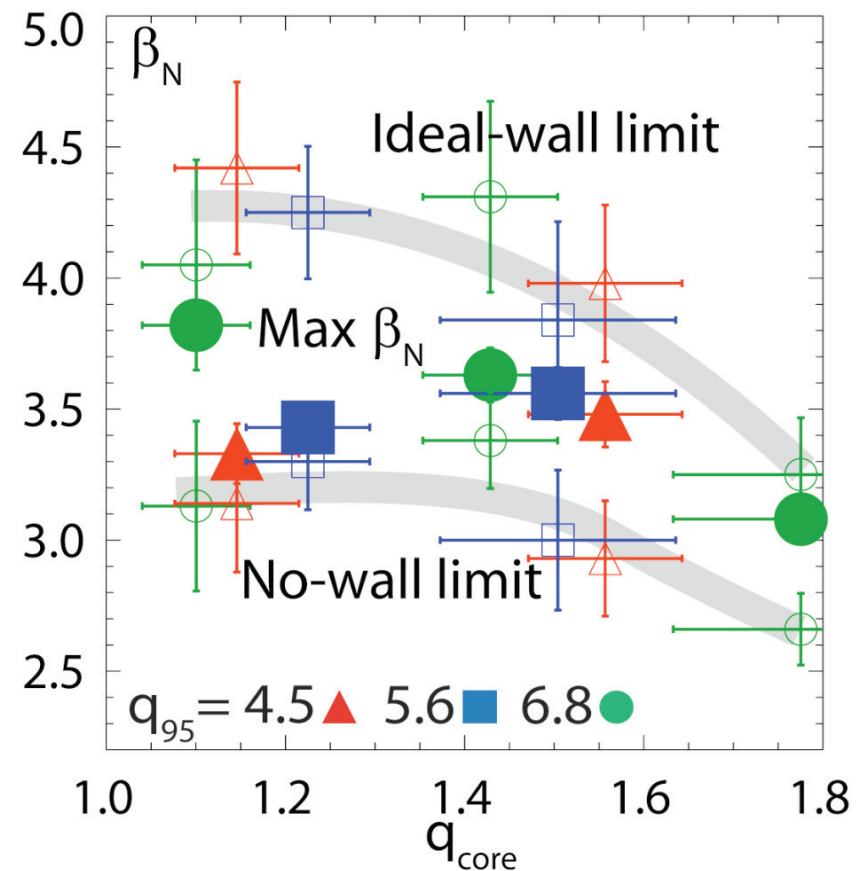
- **Transport:** depends on the q profile and determines the n, T profiles
- **Steady-state:** at high  $f_{BS}$ , the q profile is largely determined by the  $J_{BS}$  profile
- **Stability limit:**
  - Limits on pressure depend on the q profile
  - Reducing n, T gradients increases the  $\beta_N$  limit
- **Presently this complex interdependence is difficult to understand using only models**

# n, T Profiles were Measured vs q Profile at $\beta_N = 2.8$ and at the Maximum $P_{\text{beam}}$ , then $J_{\text{BS}}$ , $f_{\text{BS}}$ , $J_{\text{NI}}$ , $f_{\text{NI}}$ were Calculated

- $q_{\text{min}} \approx 1, 1.5, 2, q_{95} \approx 4.5, 5.6, 6.8$
- Measured and calculated profiles averaged during phase of approximately constant  $\beta_N$

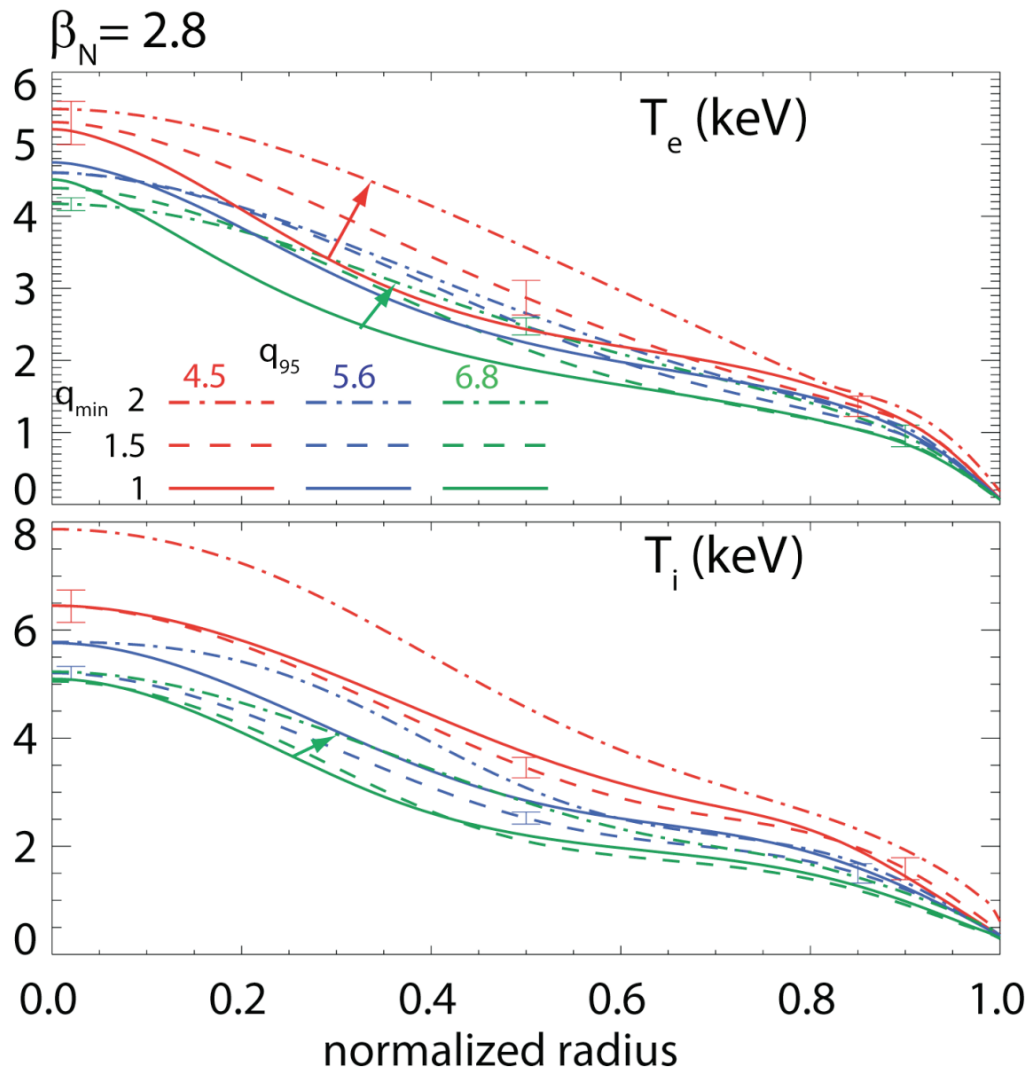


- Maximum  $\beta_N$  close to the calculated ideal-wall  $n = 1$  stability limit

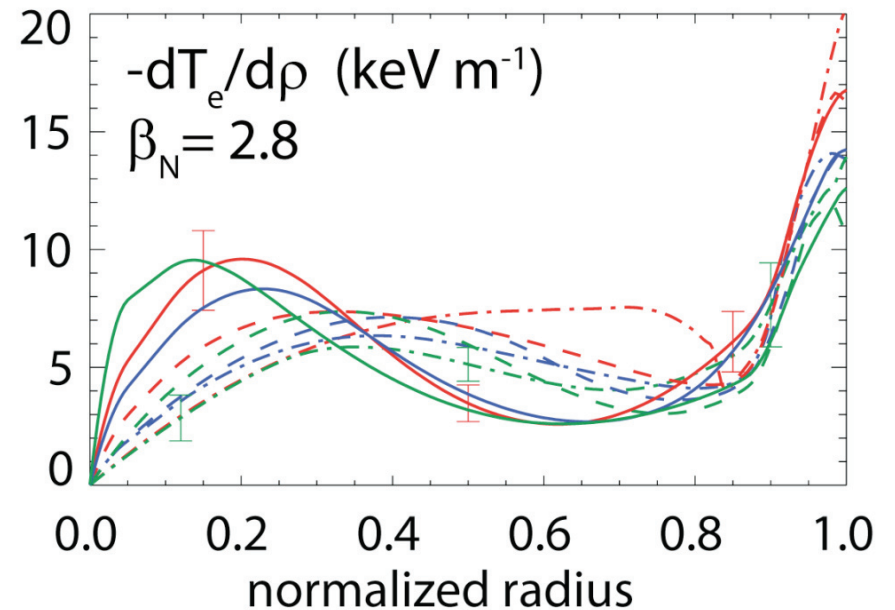


# Temperature and Density Profiles

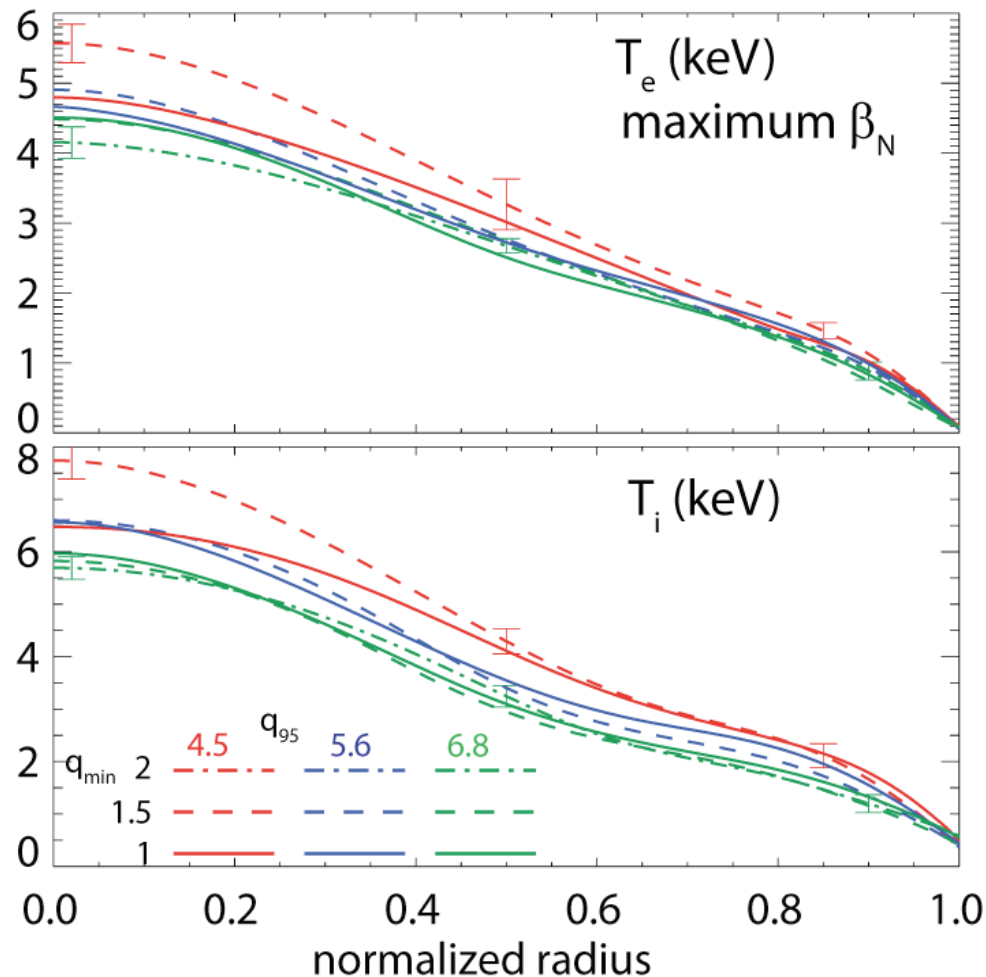
# $T_e$ and $T_i$ Profiles Broaden as $q_{\min}$ is Increased ( $\beta_N = 2.8$ )



- $T_e, T_i$  increase as  $q_{95}$  is decreased
- $dT_e/d\rho, dT_i/d\rho$  increase in the H-mode pedestal as  $q_{95}$  decreases

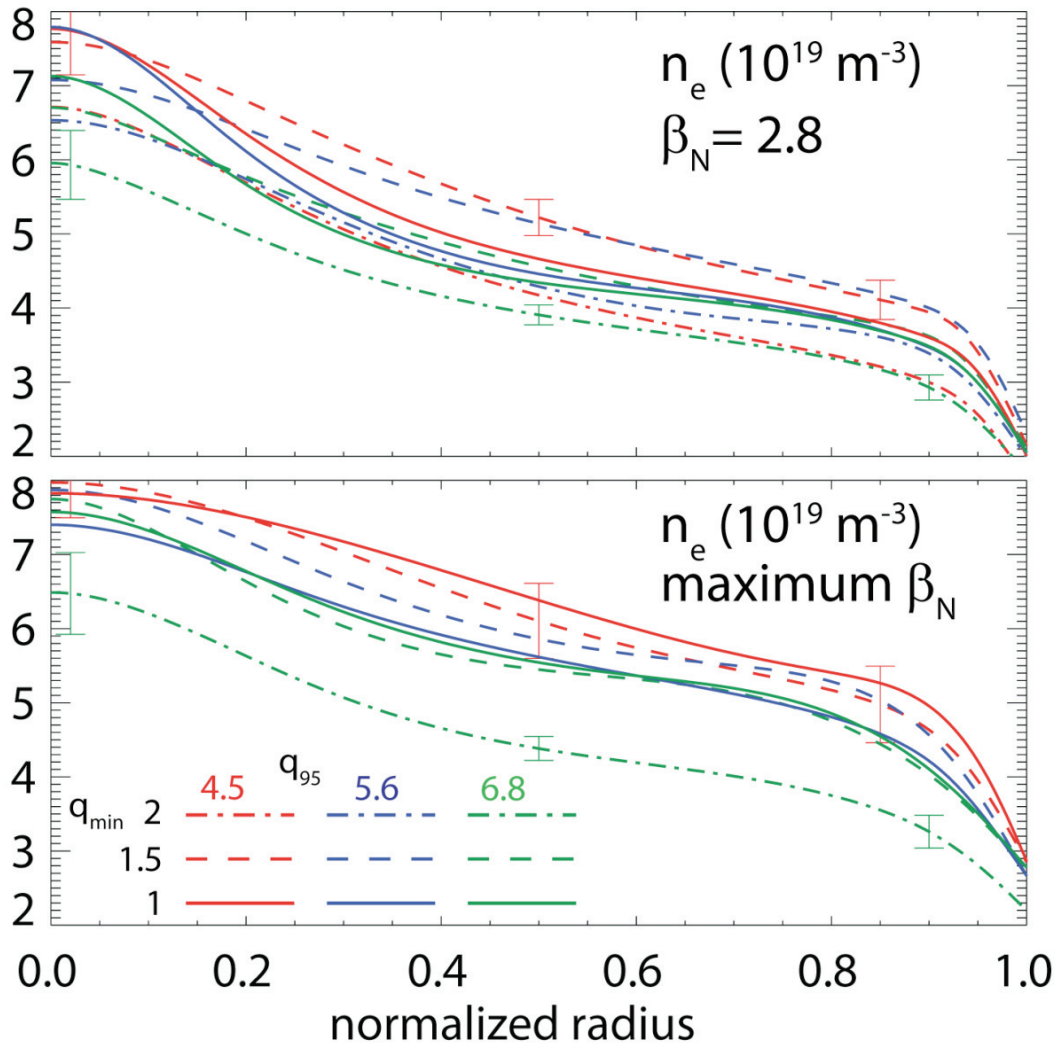


# At the Maximum Achieved $\beta_N$ , the Temperature Profiles are Nearly Independent of $q_{\min}$



- Profiles at  $q_{\min} \approx 1$  and  $\approx 1.5$  are significantly broader at higher  $\beta_N$
- Temperature dependence on  $q_{95}$  is still present

# Pumping of the Particle Exhaust in the Divertor Results in Low Pedestal Density and Peaked Density Profiles

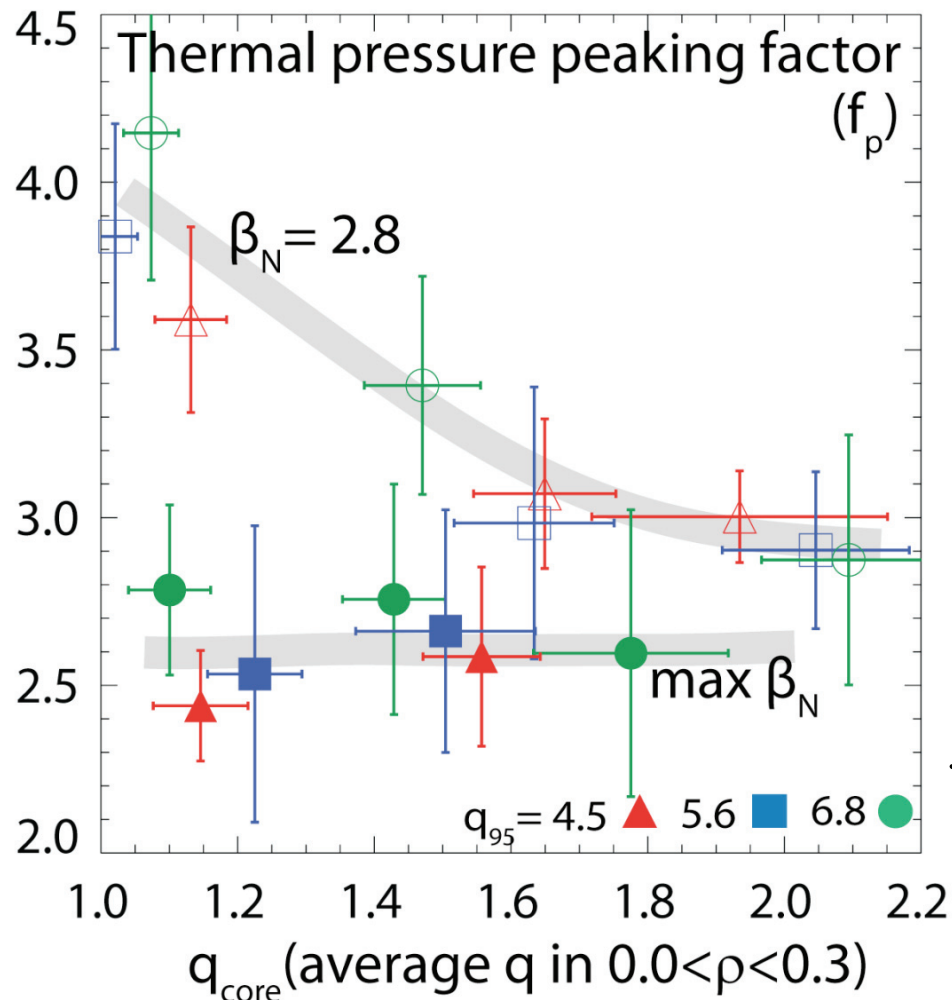


- **At  $\beta_N = 2.8$ :**
  - Density gradient locally peaked near  $\rho = 0.2$
  - Density gradient largest at  $q_{\min} = 1$
- **At the maximum  $\beta_N$ , profile is broader and pedestal density is higher**



# The Scaling of the Thermal Pressure Peaking Factor

Summarizes the Changes in the  $n, T$  Profiles with  $q_{\min}$  and  $\beta_N$



- At  $\beta_N = 2.8$  pressure is less peaked at higher values of  $q_{\text{core}}$
- Pressure peaking is significantly reduced at the maximum  $\beta_N$ 
  - Little dependence on the  $q$  profile as all  $n, T$  profiles are relatively broad

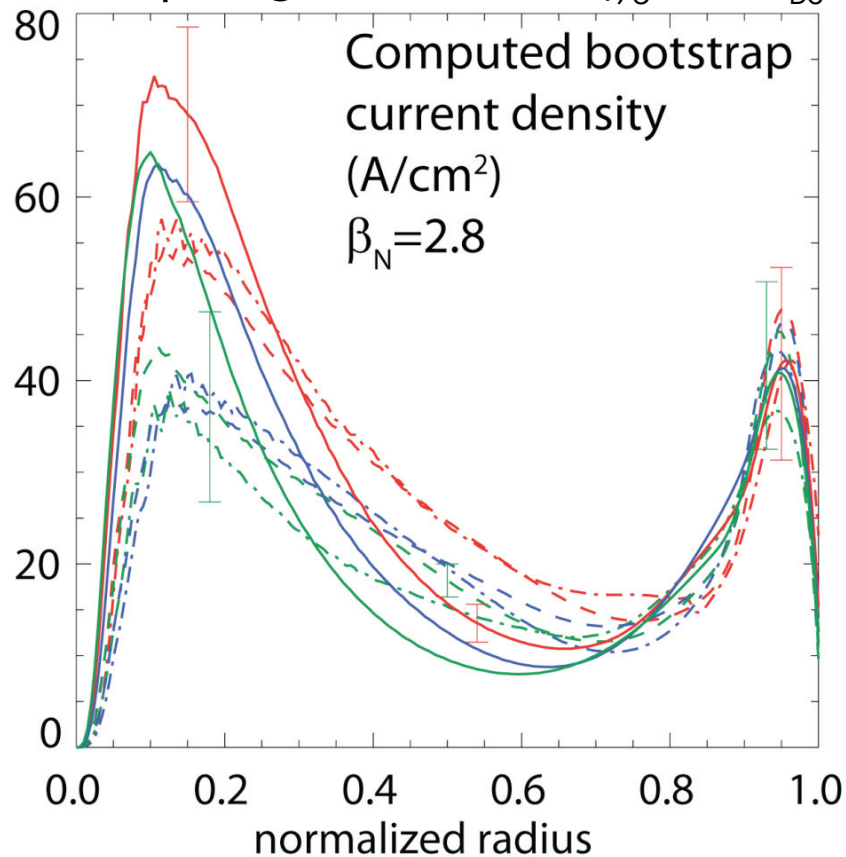
$$f_p = [n_e(0)T_e(0) + n_i(0)T_i(0)] / \langle n_e T_e + n_i T_i \rangle$$

# Calculated Bootstrap Current

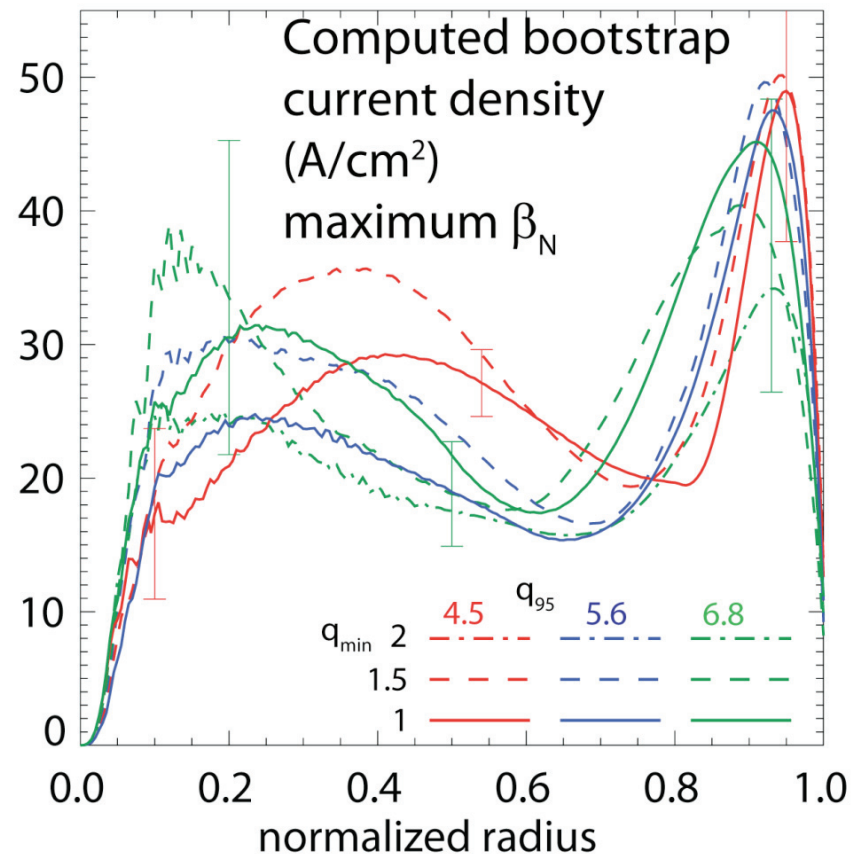
# At $\beta_N = 2.8$ , $J_{BS}$ is Peaked Near $\rho = 0.1$

## At Maximum $\beta_N$ , the $J_{BS}$ Profile is Significantly Broadened

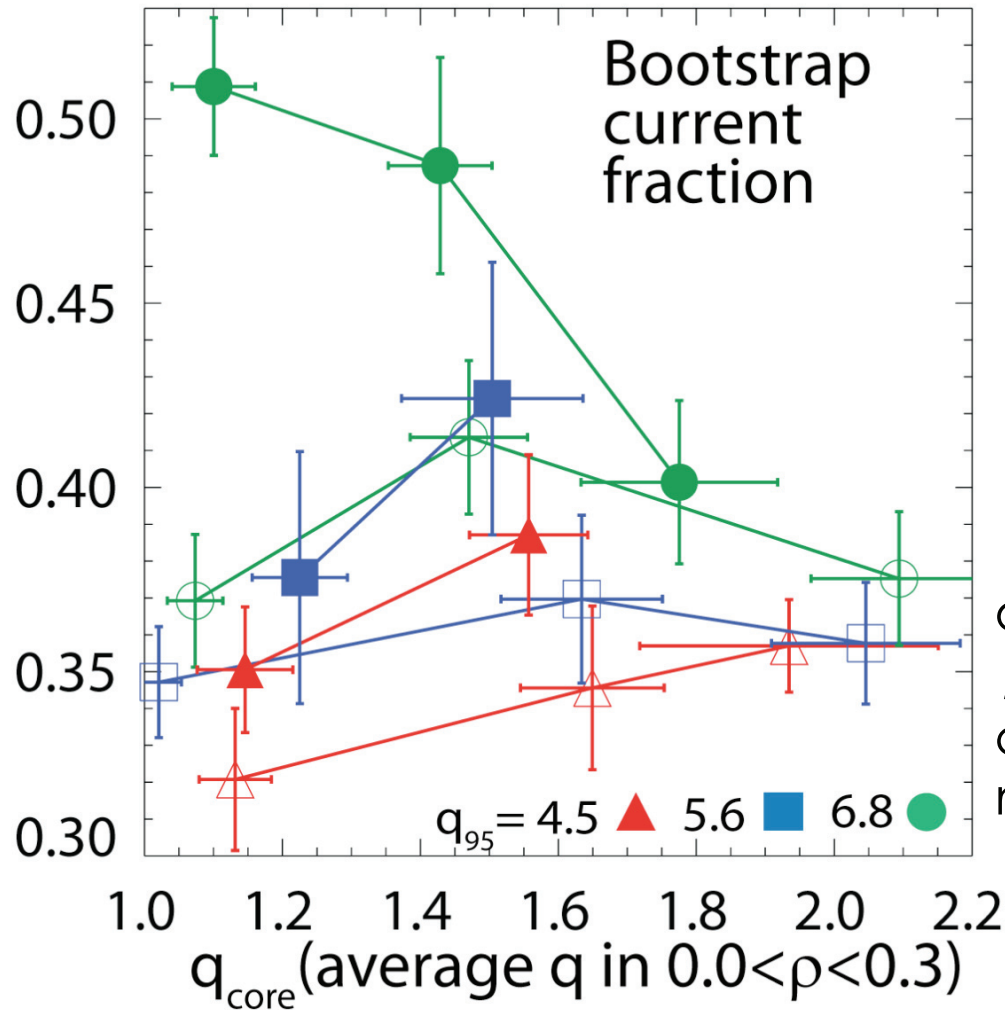
- $q_{min} = 1$ : peaked  $n_e \rightarrow \max J_{BS}$
- H-mode pedestal: no systematic variation of  $J_{BS}$  with  $q_{min}$  or  $q_{95}$ 
  - $\partial/\partial\rho$  larger at lower  $q_{95}$  but  $J_{BS} \propto q$



- Both temperature and density profiles broader at max  $\beta_N$
- H-mode pedestal:  $J_{BS}$  profile width increases with  $q_{95}$

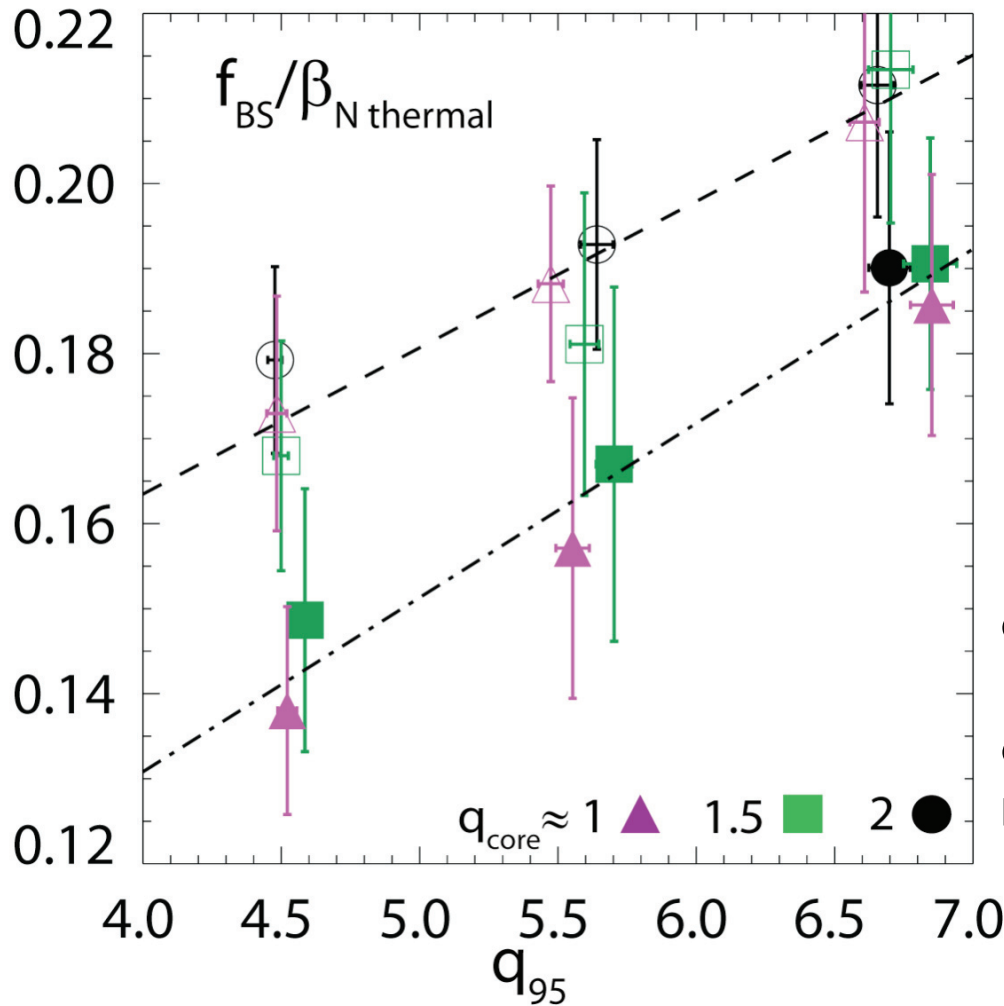


# The Dependence of $f_{BS}$ on $q_{core}$ is Comparable to the Dependence on $q_{95}$



- $f_{BS}$  is maximum at the largest values of  $q_{95}$  and  $\beta_N$
- Reduced  $f_{BS}$  at highest  $q_{core}$ :  $n$ ,  $T$  profile broadening and low achieved  $\beta_N$

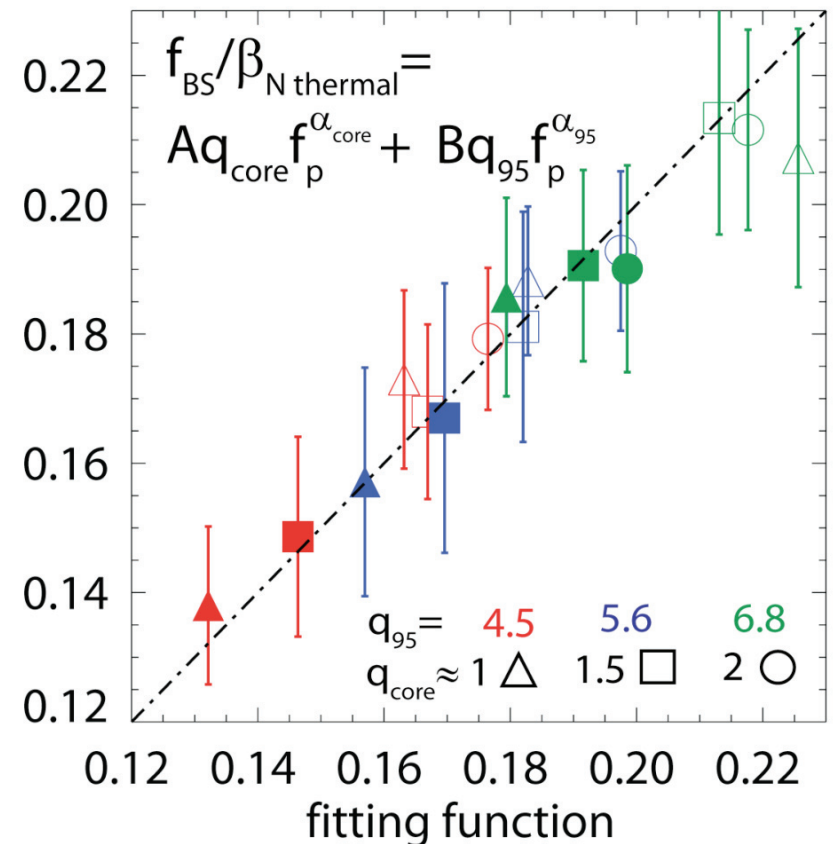
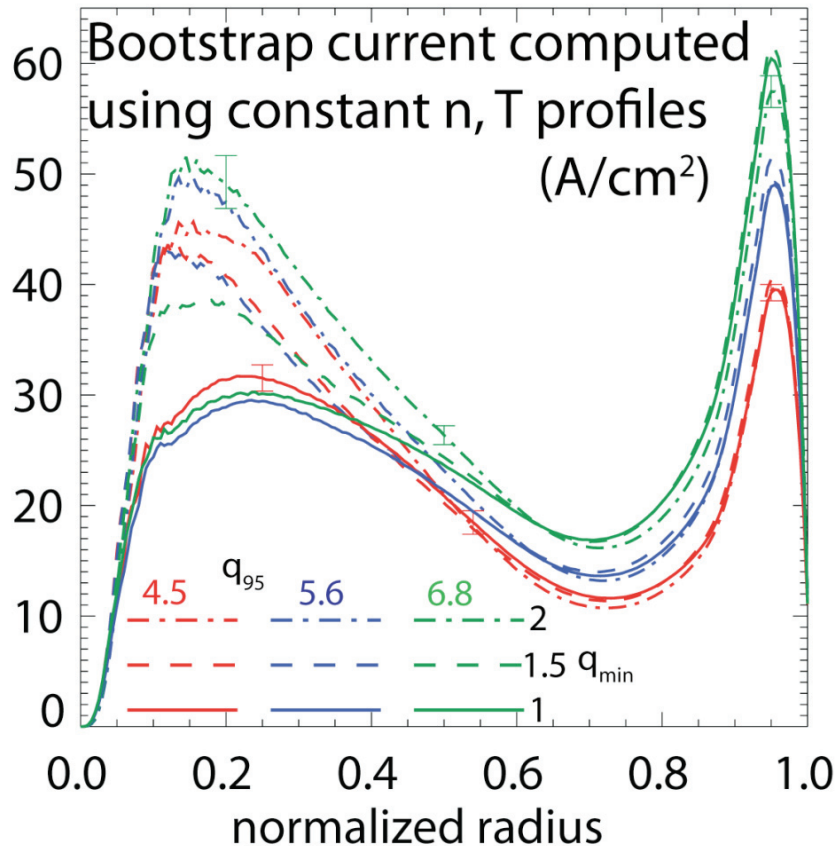
# The Commonly Used Scaling $f_{BS} \propto \beta_P \propto \beta_N q_{95}$ is not the Best Description of the Results



- Offset at  $q_{95} = 0$ :  $q_{\text{core}}$  important
- Max  $\beta_N$  points below  $\beta_N = 2.8$  data: reflects  $n, T$  profile changes

# Scaling Function $f(q_{\text{core}}, q_{95}, f_p)$ Reflects the Observed Dependence of $f_{\text{BS}}/\beta_N$ on $q, n, T$ Profiles

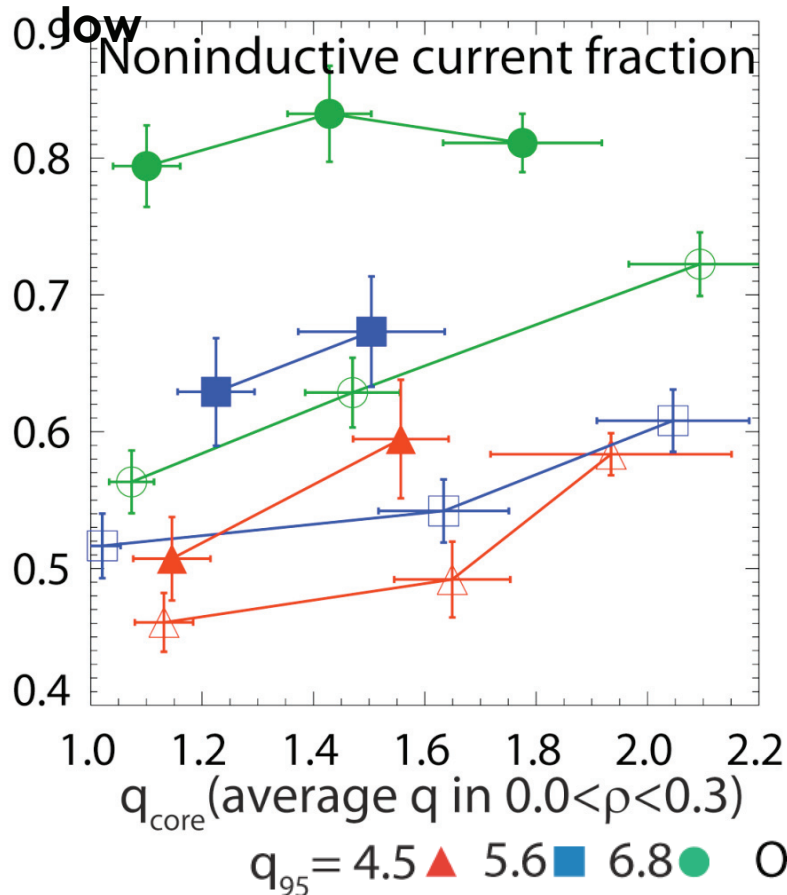
- **Test case illustrates  $J_{\text{BS}} \propto$  (local  $q$  value)**
  - Differs from experiment  $J_{\text{BS}}$  profiles
- **Plasma divides into two regions:**
  - Inner half:  $J_{\text{BS}} \propto q_{\text{core}}$
  - Outer half:  $J_{\text{BS}} \propto q_{95}$
- **Two regions  $\rightarrow$  scaling function with separate  $q_{\text{core}}$  and  $q_{95}$  terms**
- **Opposite scaling of  $\nabla n, \nabla T$  with  $f_p$  in the inner and outer regions**
  - Opposite signs for  $\alpha_{\text{core}}$  and  $\alpha_{95}$



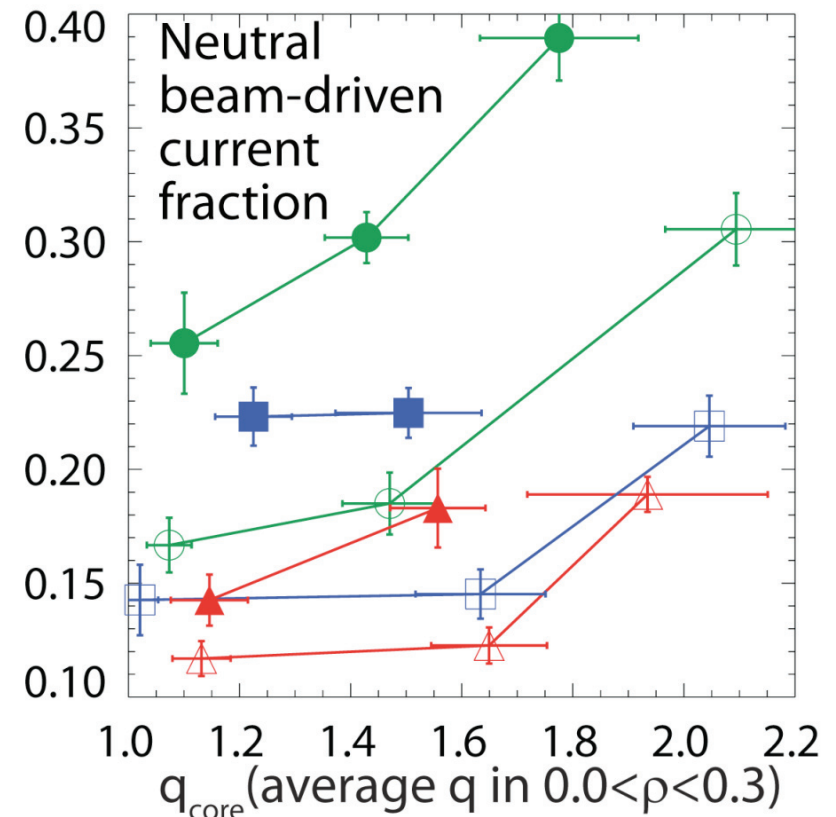
# Total Noninductively Driven Current

# The Calculated $f_{NI}$ Increases with Both $q_{core}$ and $q_{95}$

- Result of combined changes in  $f_{BS}$  and  $f_{NBCD}$
- One exception:  $q_{core} = 1.8$ ,  $q_{95} = 6.8$  where max  $\beta_N$  is low



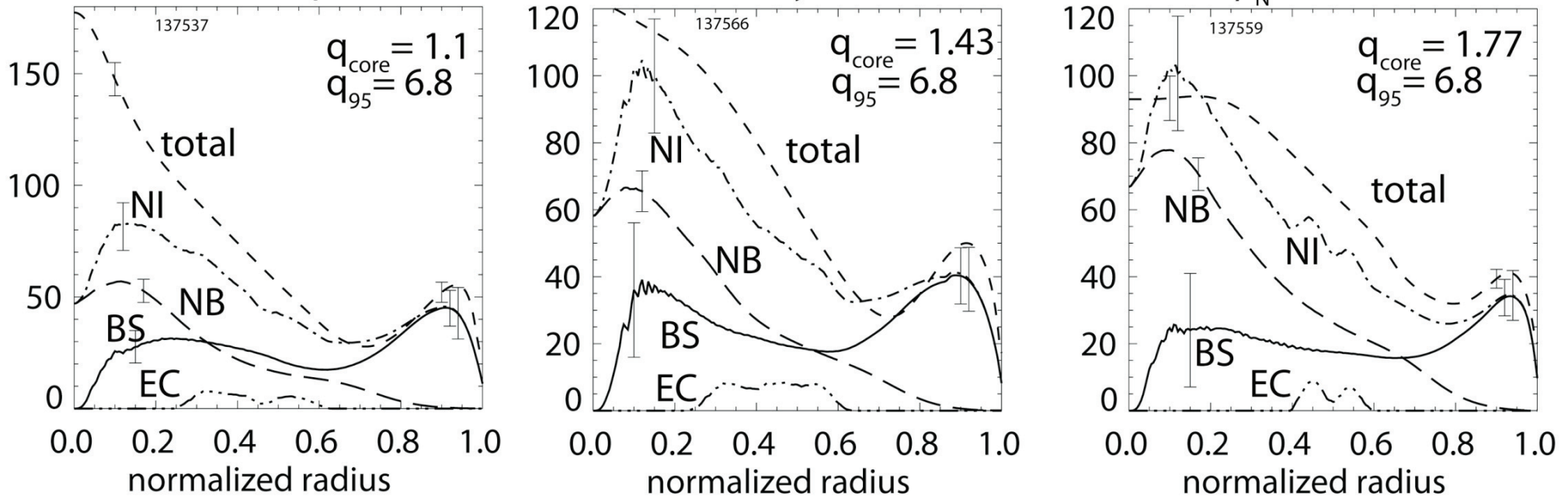
- $f_{NBCD}$  increases with  $q_{core}$ 
  - Higher  $T_e$ , lower  $n_e$





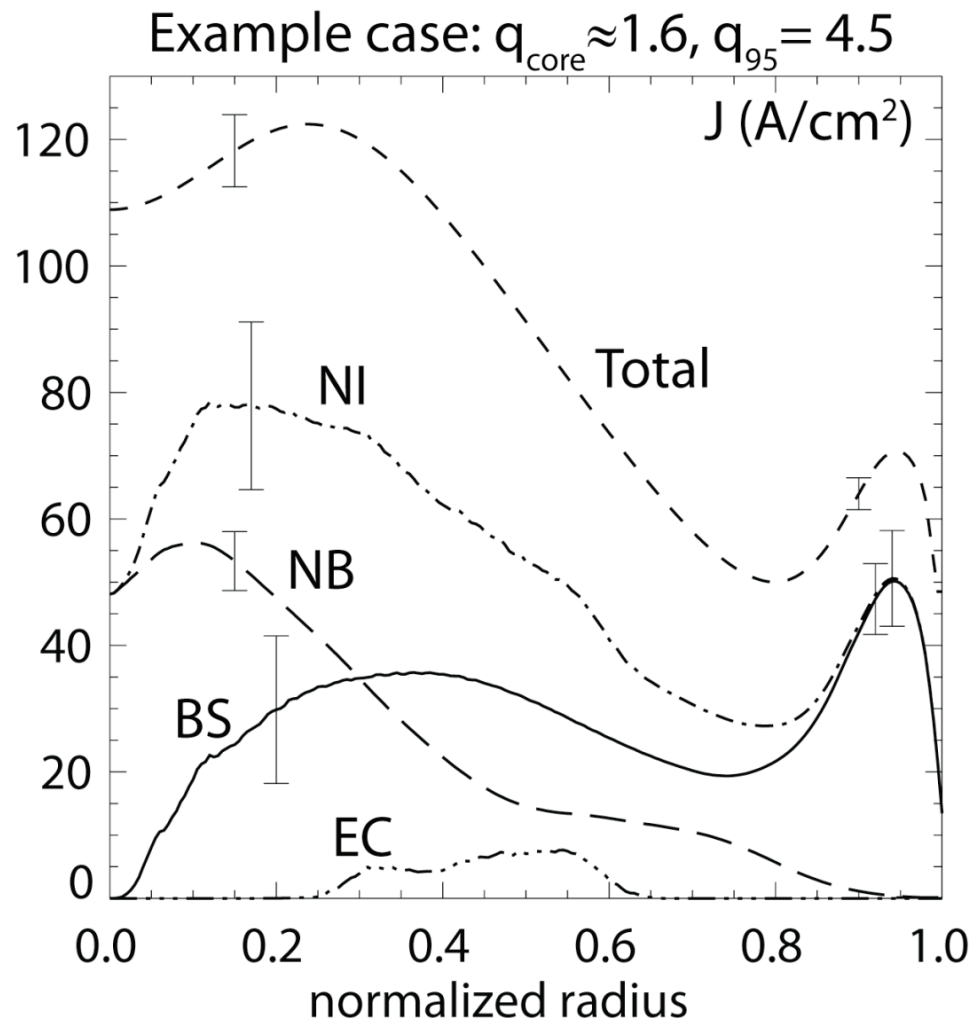
# $q_{95} = 6.8$ Discharges are the Closest to $f_{NI} = 1$ , $J_{NI}$ and J Profile Shapes are Best Matched at $q_{core} \geq 1.4$

Components of the current density (A/cm<sup>2</sup>) at the maximum  $\beta_N$



- $J_{BS}$  profiles at max  $\beta_N$  are roughly uniform while J profile is peaked
  - Externally driven current ( $J_{CD}$ ) required at  $\rho < 0.8$
  - $J_{NBCD}$  profile aligns well with J inside  $\rho < 0.8$
- Required  $J_{CD}$  near the axis is very large for  $q_{core} \approx 1$
- At the highest  $q_{core}$ , possibility of  $J_{NI}$  overdrive near the axis

# To Achieve $f_{NI} = 1$ at $q_{95} \approx 5$ , Significantly Increased $J_{NI}$ Located Off Axis is Required

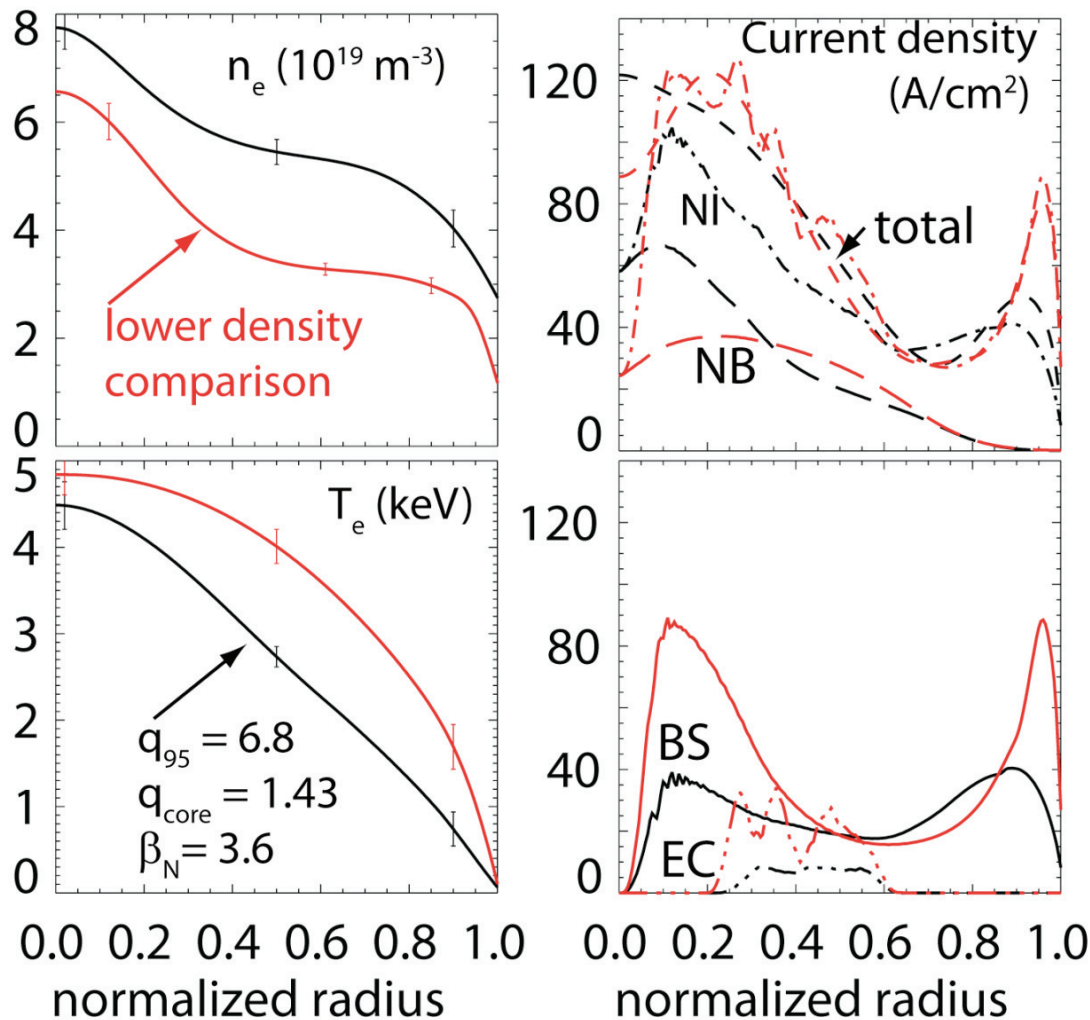


- $q_{95} \approx 5$  required for sufficient fusion gain in a reactor or for ITER steady-state mission
- In this example:  
 $f_{BS} \approx 0.39, f_{NI} \approx 0.6$
- For  $f_{NI} = 1$  in this example (compared to  $q_{95} = 6.8$ ):
  - Factor 2 additional  $J_{NI}$  is required
  - >factor 3 additional total noninductive current is required

# Paths to Higher $f_{BS}$ at Fixed $q_{95}$ are Increased $\beta_N$ , Increased $q_{core}$ or Increased Gradients

- **Increase  $\beta_N$  limit by broadening P profile**
  - $n, T$  profiles broaden as  $\beta_N$  is increased
    - $\beta_N$  limits may be higher than calculated
  - Off-axis beam injection to broaden fast ion pressure profile
    - $f_{p\ total}$  (here  $\approx 3.3$ ) closer to  $f_{p\ thermal}$  (here  $\approx 2.6$ )
  - Broader P moves gradients and  $J_{BS}$  off-axis
- **$q_{min}$  controllable with external CD**
  - Choose high  $q_{min}$  to increase  $J_{BS}$ , reduce external CD requirement
  - Compatible with off-axis beam injection
- **Increasing gradients (larger  $f_p$ ) reduces  $\beta_N$  limit**
  - Focus on reduced  $n_e$ , increased  $T_e$  to increase CD and  $J_{BS}$

# Other DIII-D Discharges Have Demonstrated Higher $f_{BS}$ with Decreased $n_e^{ped}$ and Increased $T_e$



- Illustrated by comparison to a discharge from a 2008 AT-style discharge with  $f_{BS} = 0.7$ , same  $q$  profile,  $\beta_N = 3.1$
- Average  $n_e$  lower, but still with substantial core density gradient
- Higher  $T_e$  maintains  $P_e$ ,  $J_{BS}$
- Reduced  $n_e$ , increased  $T_e$  increases  $J_{CD}$
- Possible fast ion diffusion can reduce  $J_{NBCD}$ 
  - Curve in red assumes  $1 \text{ m}^2/\text{s}$

# Summary

# Systematic Dependence of the $n_e$ , $T_e$ , $T_i$ Profile Shapes on the $q$ Profile and $\beta_N$ Strongly Affects the Bootstrap Current

- At  $\beta_N = 2.8$ ,  $T_e$ ,  $T_i$  profiles broaden with increased  $q_{\min}$
- Increasing  $\beta_N$  broadens all profiles
- At high  $\beta_N$ , core  $J_{BS} < J$  with ~uniform profile
  - No systematic dependence on the  $q$  profile
- Peaked profile of  $J_{CD}$  needed so that  $J_{NI}$  matches  $J$
- $q_{95} > 6$  is the best choice for  $f_{NI} = 1$  with the present DIII-D external current drive sources
  - Planned off-axis NBCD, ECCD are good matches to the current drive requirements
- Path to  $f_{NI} = 1$  at  $q_{\min} \approx 5$  is increased  $\beta_N$  and  $T_e$ , reduced  $n_e$ , relatively high  $q_{\min}$