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# Comparison of Broad Spectrum Turbulence Measurements, Gyrokinetic Code Predictions, and Transport Properties from the DIII-D Tokamak

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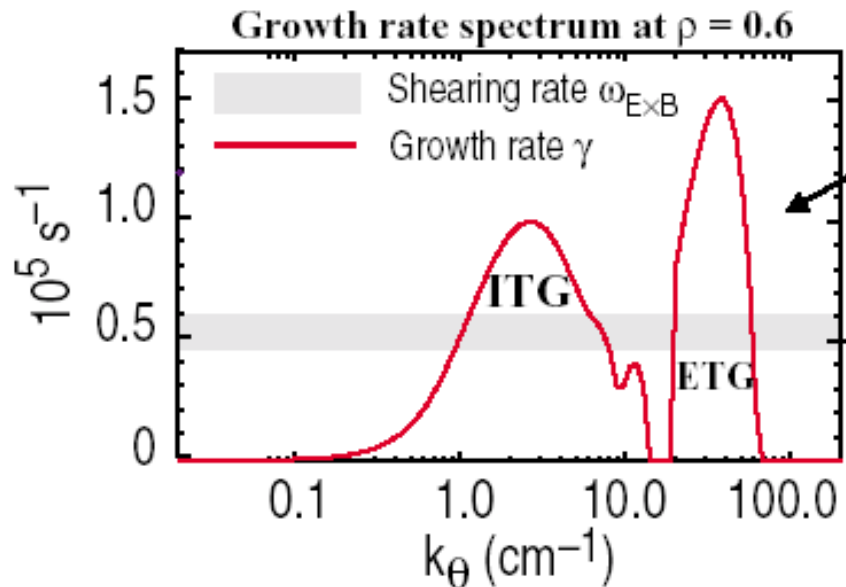


# Overview of results

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- First measurements of high-k turbulence ( $k \sim 35 \text{ cm}^{-1}$ ,  $k_{\perp} \rho_s \approx 10$ ) on DIII-D have been made.
  - Combined with low and intermediate-k measurements, these provide a new, more complete picture of turbulence behavior on DIII-D.
  - Clear turbulence signals at  $k \sim 35 \text{ cm}^{-1}$ ,  $k_{\perp} \rho_s \approx 10$  using new mm-wave backscatter.
  - $k_{\perp} \rho_s \sim 0.2-10$  a range relevant to ITG, TEM and ETG instabilities.
- GKS code shows plasma unstable to ITG, TEM, and ETG consistent with observed turbulent activity
  - however some differences between GKS and observations found.
  - High-k ( $k \sim 35 \text{ cm}^{-1}$ ,  $k_{\perp} \rho_s \approx 10$ ) turbulence increases with  $T_e$  increase (with  $L_n$ ,  $L_{Te} \sim \text{constant}$ ) seemingly contrary to expectation.
- Both measured and calculated response to perturbations (NBI, ECH) varied with wavenumber, supporting need for broad wavenumber comparisons.

# Motivation

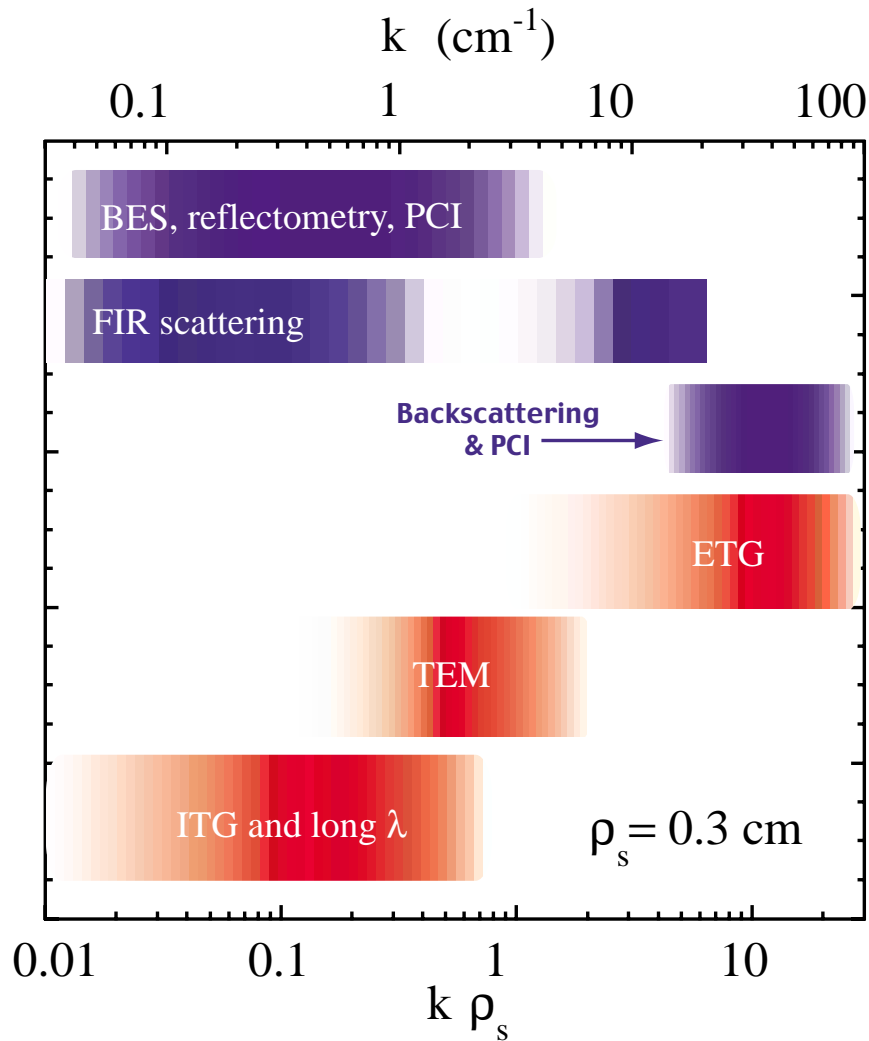


Detailed comparison of transport properties and broad wavenumber range turbulence measurements to theoretical predictions is essential in developing this predictive capability.

- The understanding of anomalous electron and ion transport leading to development of a predictive transport capability represents a significant scientific challenge.

- Provides confidence extrapolating to next-step devices.
- Potentially lead to improved transport control  $\Rightarrow$  optimized pressure profiles and enhanced AT fusion performance.

# Broad wavenumber diagnostic set being developed at DIII-D to address anomalous electron and ion transport



- Wavenumber region potentially occupied by ITG, TEM, and ETG type instabilities.

## • Diagnostic k-space large on DIII-D

- UCLA FIR scattering system upgraded to probe low ( $0\text{-}2 \text{ cm}^{-1}$ ) and intermediate wavenumbers ( $8\text{-}20 \text{ cm}^{-1}$ )
- New concept high-k backscattering system added ( $\sim 40 \text{ cm}^{-1}$ ) (UCLA).
- U. Wisc. beam emission spectroscopy (BES), upgraded for improved sensitivity, probes  $0\text{-}3.5 \text{ cm}^{-1}$
- MIT phase contrast imaging (PCI) upgraded to probe core plasma,  $0\text{-}30 \text{ cm}^{-1}$ .
- Fluctuation and correlation reflectometry probe  $0\text{-}5 \text{ cm}^{-1}$ .

# Properties of FIR and mm-wave turbulence diagnostics

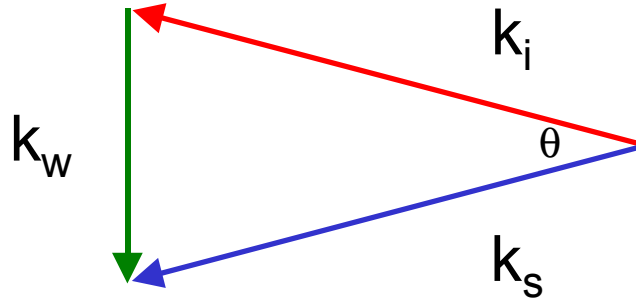
Diagnostic	$k$	$k$ range ( $\text{cm}^{-1}$ )	$k_{\perp}\rho_s$	Spatial resolution
Low-k FIR	$k_{\theta}$	0-2	0-0.3	[ -a, a ] $-1 \leq \rho \leq 1$
Intermediate-k FIR	$k_{\theta}$	8-15	2-5	varies with $k$ , e.g. $-0.4 \leq \rho \leq 0.4$ $0.2 \leq \rho \leq 0.6$
High-k mm-wave backscatter	$k_r$	35-40	$\sim 10$	$\sim a/2$ $\rho \geq 0.4$

# Collective scattering principles

- Collective Thomson scattering is well-suited to study short wavelength turbulence – **only known technique to probe such short wavelengths.**

Momentum matching gives

$$\underline{k}_i + \underline{k}_w = \underline{k}_s$$



Energy conservation gives

$\omega_i + \omega_w = \omega_s$  i.e scattered radiation Doppler shifted by propagation in lab reference.

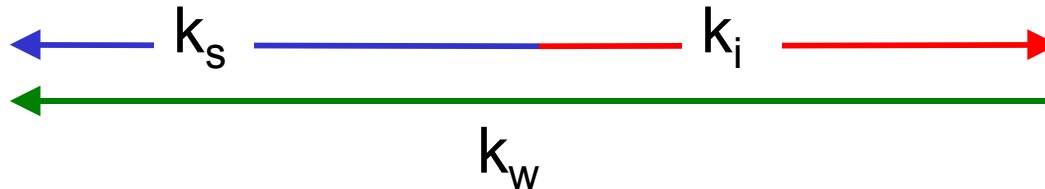
**Bragg Law:**

For  $k_i \sim k_s$ , can show that

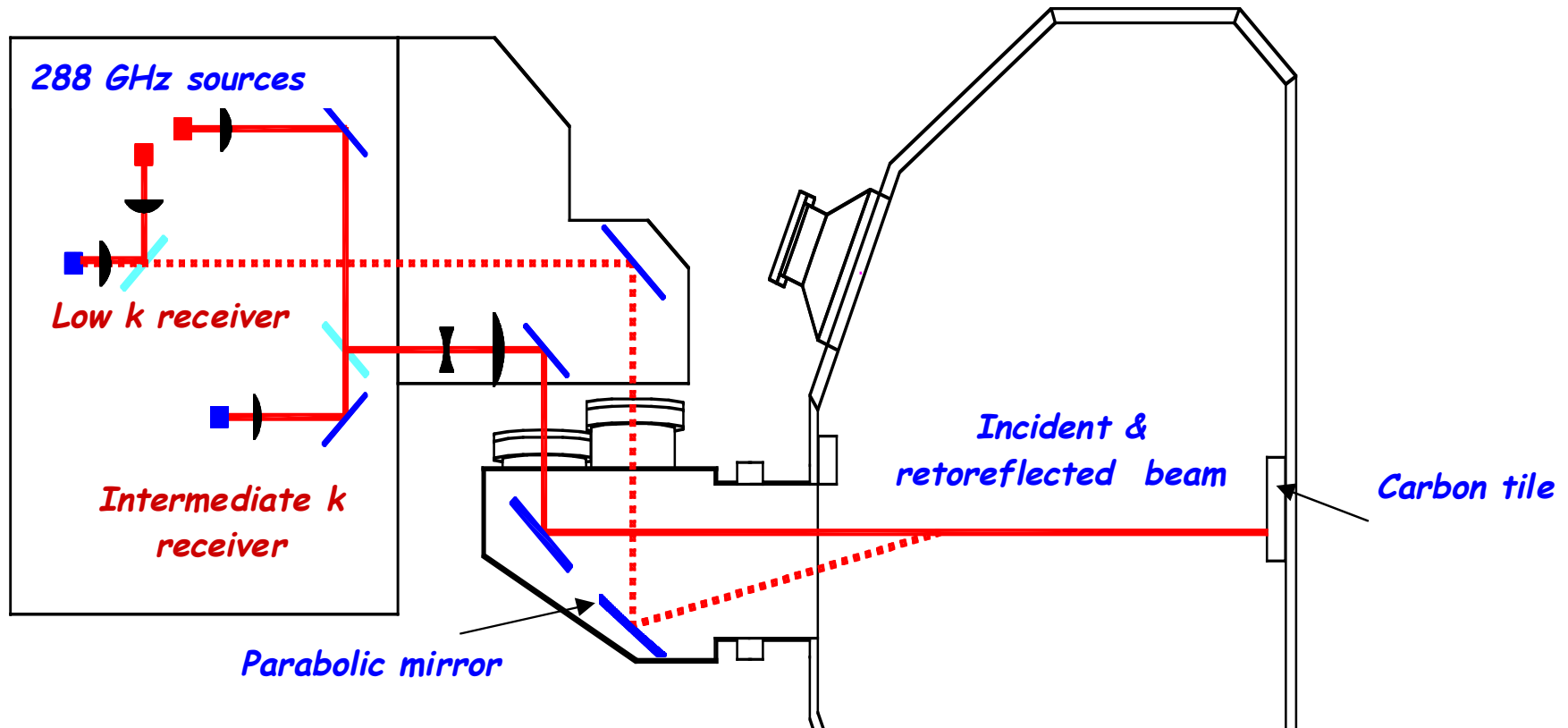
$$k_w = 2k_i \sin \theta / 2$$

Where  $\theta$  is the scattering angle.

**When scattering is backward ( $\sim 180^\circ$ ) probed wavenumber  $\sim 2k_i$**

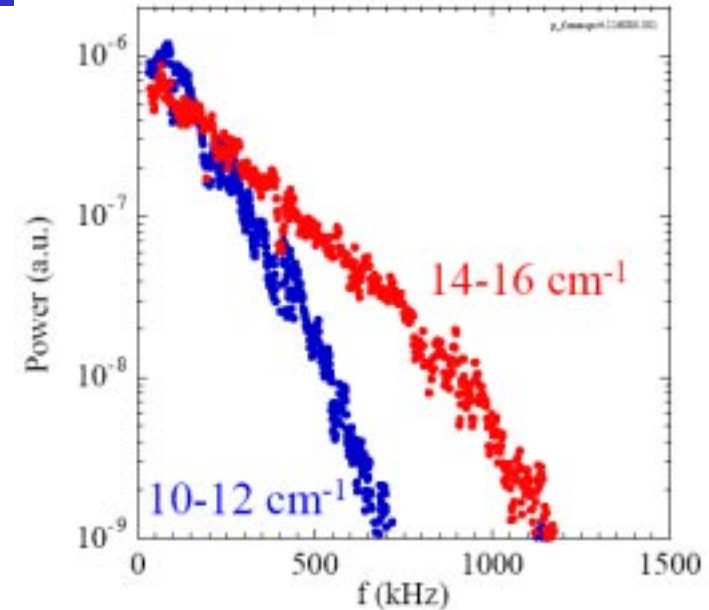
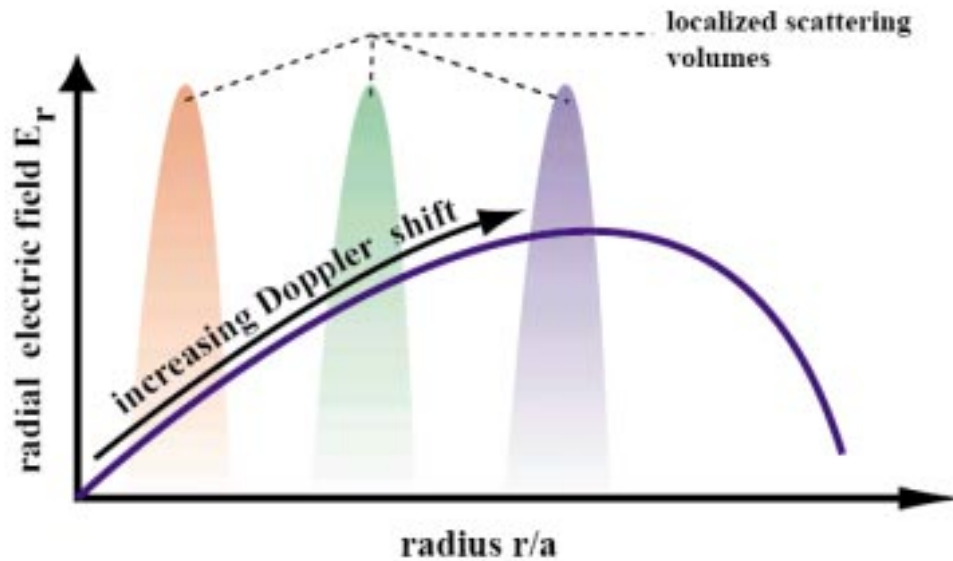


# Low & intermediate k measurements via FIR scattering



- Forward scattering at 288GHz ( $\lambda \sim 1\text{mm}$ ).
- Low and intermediate-k passed multiple validity tests: no cross correlation between signals, Doppler shifts consistent as k changed.

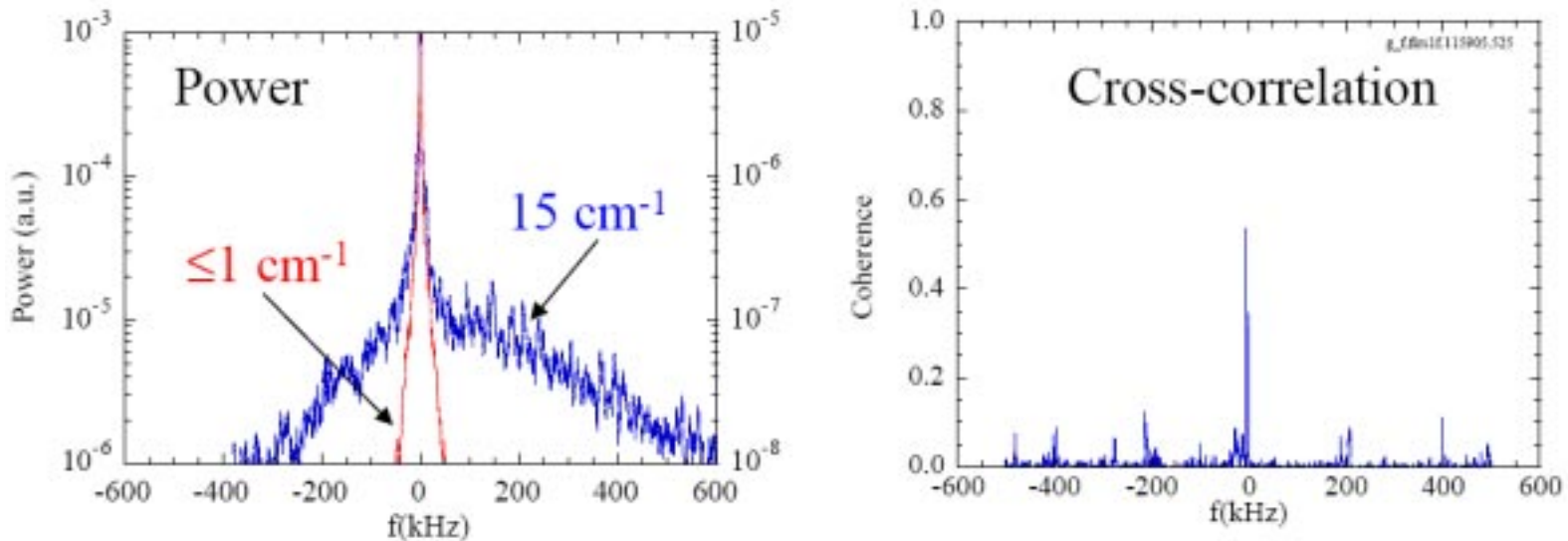
# Validity tests of intermediate-k data



- Initial FIR data from Ohmic discharge.
  - Expect proportionally higher Doppler shifts as  $k$  is increased
- Size of scattering volume appx. same - overlap of volumes is  $\sim 10$  cm.
- Spectral width at higher  $k$  larger than that at lower  $k$  by approx ratio of  $k$ 's.
- Consistent with Doppler shift  $\Delta\omega = k \cdot v$  (dominated by  $E \times B$  turbulent flow)

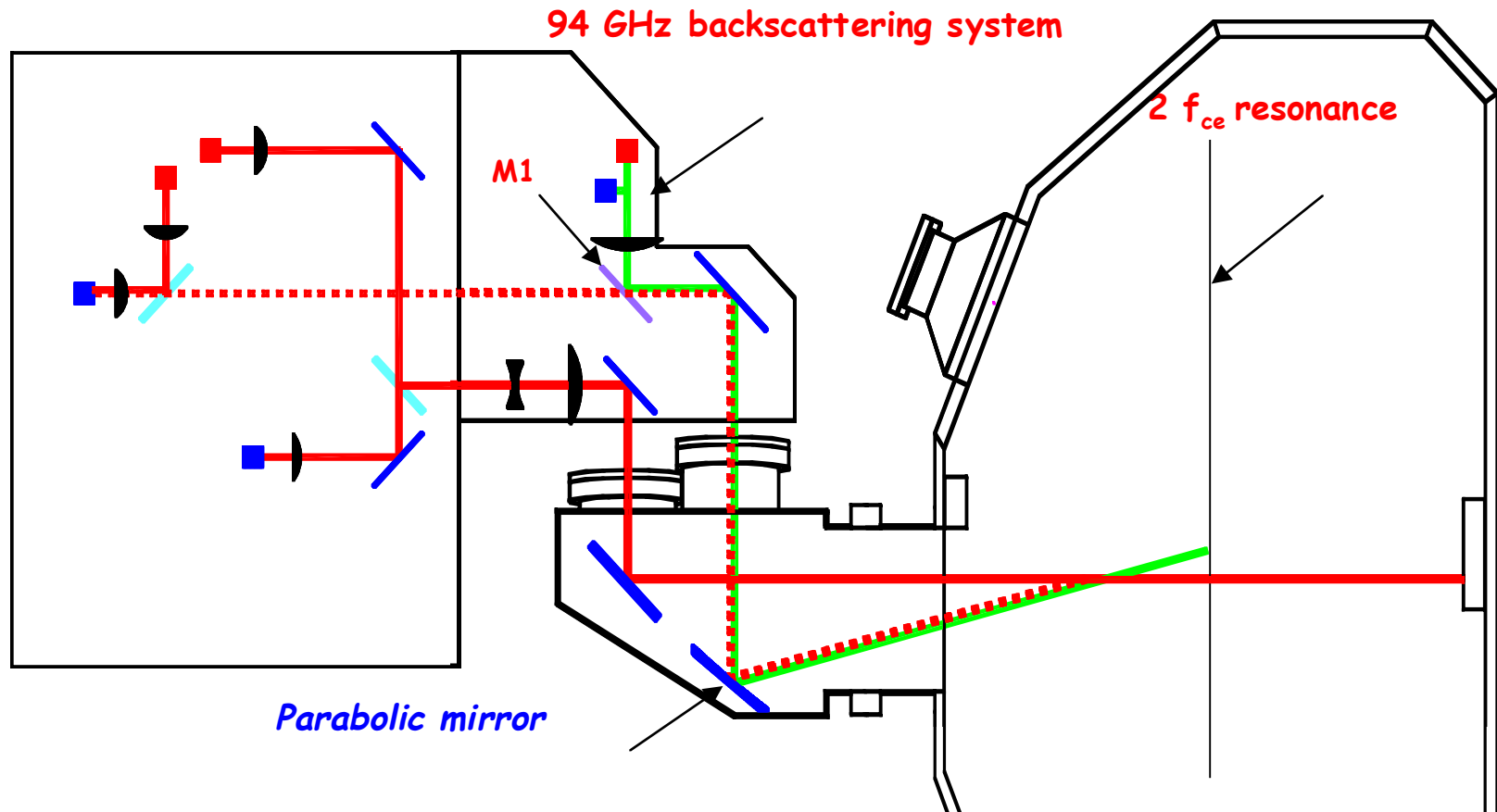


# Low and intermediate-k power spectra have different widths and no correlation



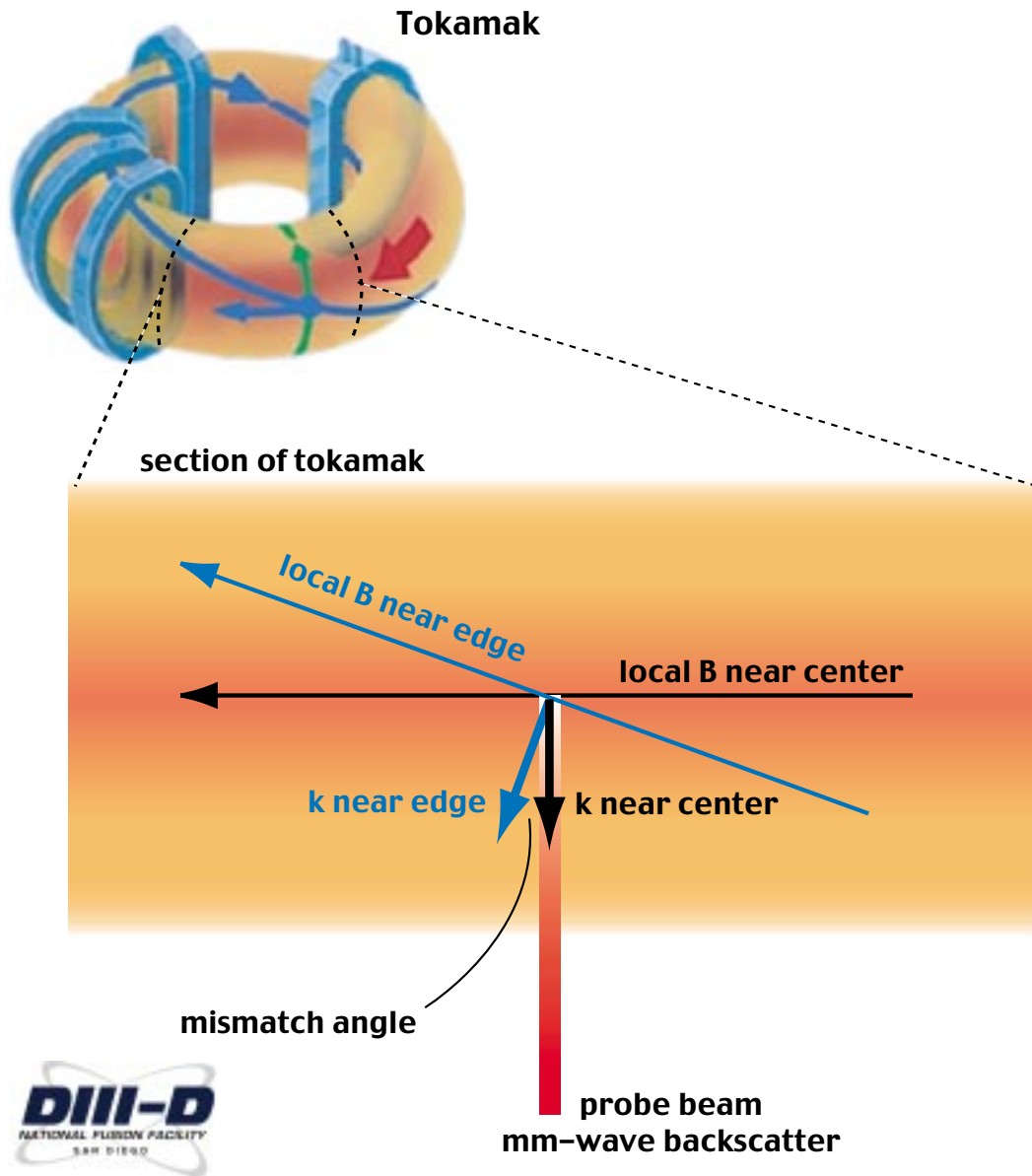
- Ohmic discharge, [FIR data](#).
- **Low-k** is chord averaged while intermediate-k from  $\rho \approx 0.4-0.8$ .
- **Intermediate-k** spectrum wider in frequency space.
- Important test: No cross-correlation between low and intermediate-k signals:  
 $\Rightarrow$  **low-k not contaminating intermediate-k**, and vice-versa

# 94 GHz backscattering to probe high-k



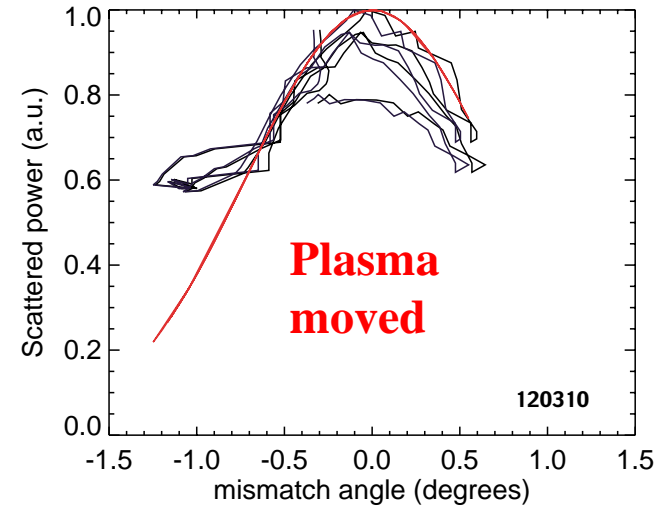
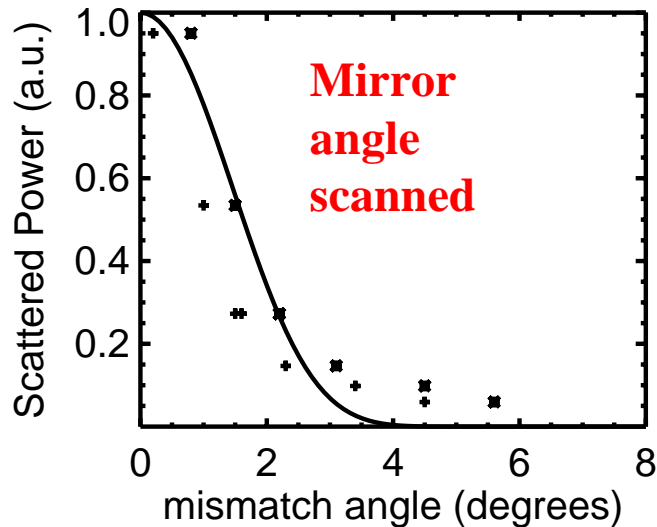
- 94 GHz radiation is shown in green and the 288GHz FIR in red.
- $2f_{ce}$  resonance layer used as beam dump for 94 GHz probe beam.
- High-k data passed multiple validity tests.

# Multiple tests of mm-wave backscattering performed



- Backscatter signal clearly different from lower-k signals, e.g. showing none of coherent modes often seen at low-k.
- No coherency was found between the low-k FIR and backscattered signal.
- Concept of wavenumber matching provided excellent test of system performance.

# k-matching requires both magnitude and direction to match

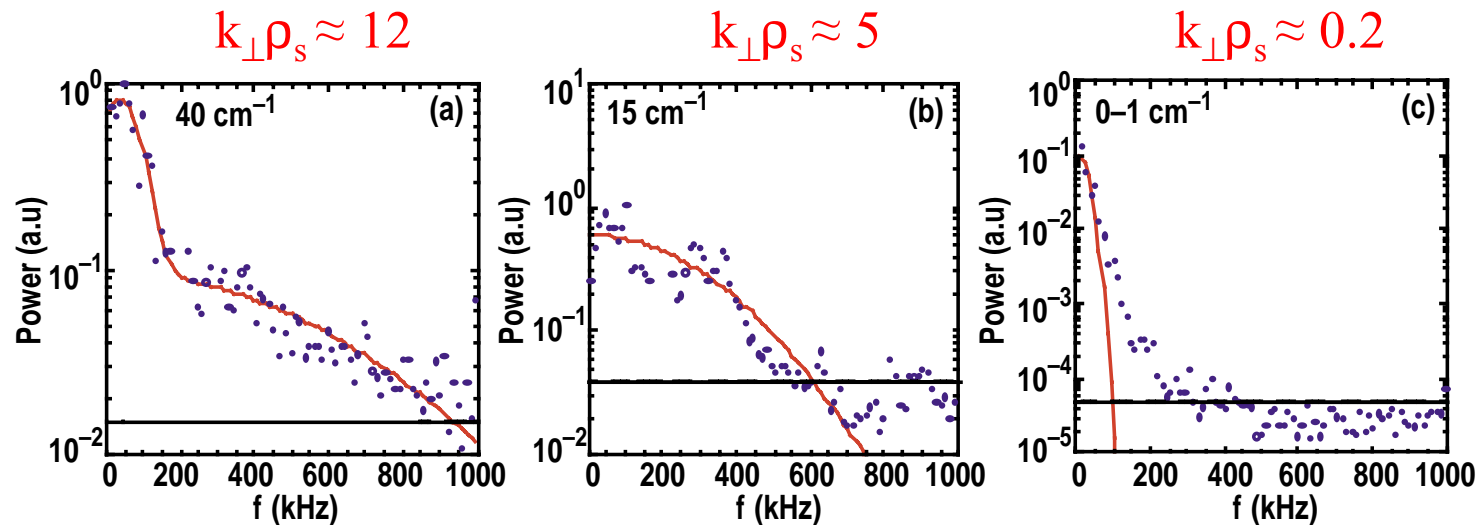


- In scattering theory, if wavenumber probed does not physically align in such a way as to satisfy the momentum balance then no scattering occurs.
- Instrument function given by [Slusher and Surko, PhysFluids1980]:

$$E_s(\mathbf{R}, t) = [\hat{R} \times (\hat{R} \times \hat{y})] \frac{a_0^2 r_0 E_0}{32\pi^3 R} \int d\omega d^3K dz \exp\left(-\frac{(K_x - k_x^s)^2 a_0^2}{4}\right) \exp\left(-\frac{(K_y - k_y^s)^2 a_0^2}{4}\right) \\ \times \{\exp[i(K_z + k_0 - k_z^s)z] \exp[-i\omega_*(t - R/c)]n(\mathbf{K}, \omega) + \text{c.c.}\}$$

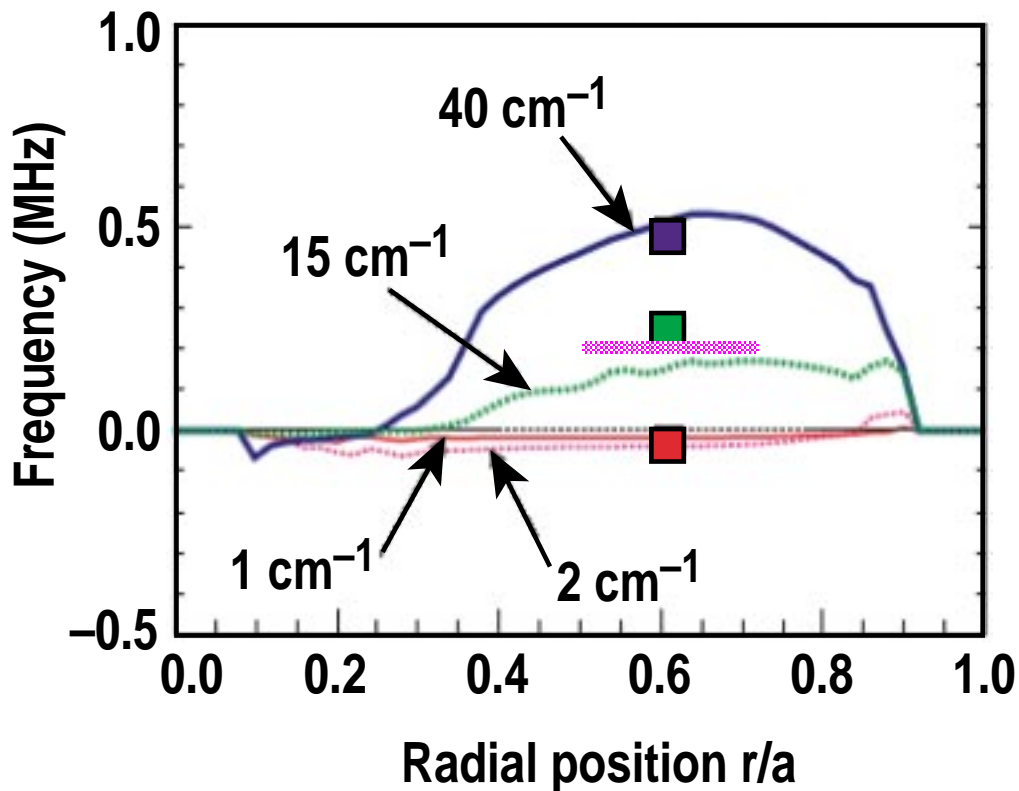
- Changed  $K_z$  by varying mirror angle and by moving plasma.
- **Good agreement with theory expectation further confirming diagnostic operation**

# Initial measurements of low ( $0\text{-}1\text{ cm}^{-1}$ ), intermediate ( $15\text{ cm}^{-1}$ ), and high-k ( $40\text{ cm}^{-1}$ ) density fluctuations performed



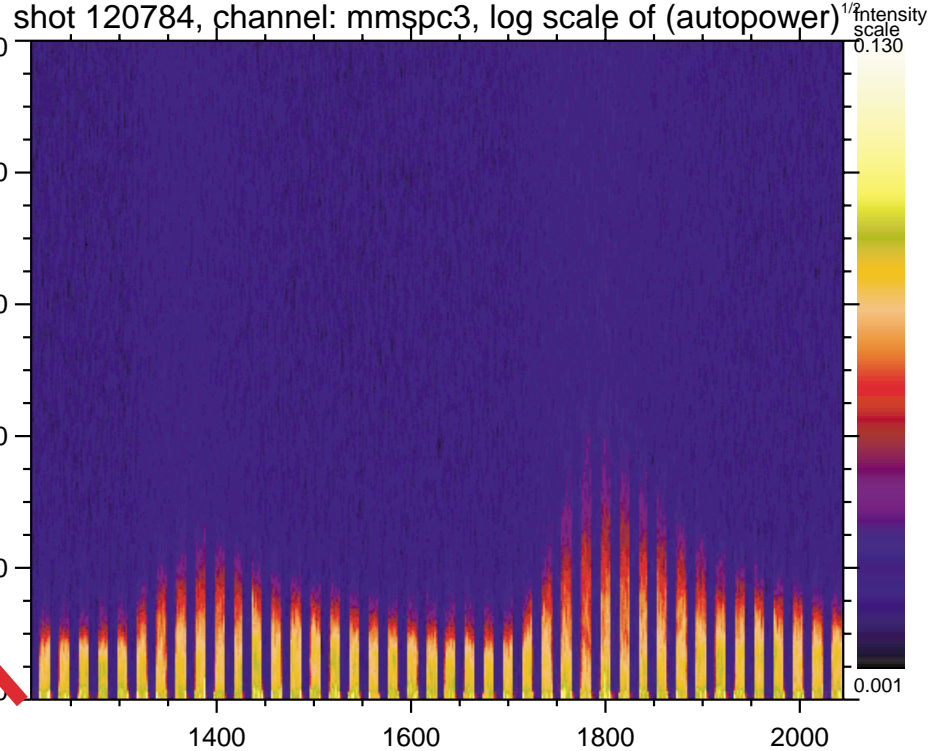
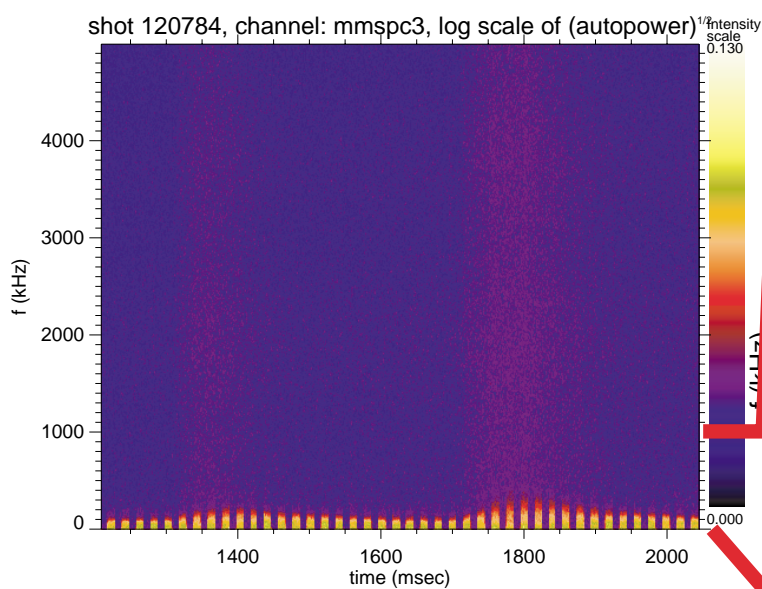
- Initial data in Ohmic, diverted plasma,  $I_p = 1\text{ MA}$ ,  $n_{e,\text{avg}} = 2.6 \times 10^{19}\text{ m}^{-3}$ ,  $B_T = 2.1\text{ T}$ .
- **$k$  range consistent with ITG, TEM and ETG type instabilities.**
- Gaussian fits give  $\sim 50\text{ kHz}$  and  $\sim 490\text{ kHz}$  for the high-k,  $260\text{ kHz}$  and  $24\text{ kHz}$  respectively for intermediate and low-k.
  - The observed trend is for increasing frequency width with increasing wavenumber.

# GKS linear stability code indicates these discharges unstable to a wide range of instabilities: ETG, ITG and TEM.

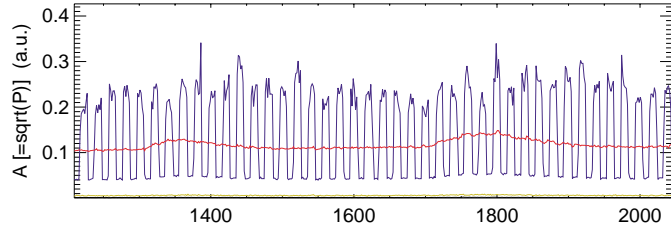


- Real frequency of unstable modes from GKS over radial range  $\rho = 0.1-0.9$ 
  - for different  $k$  values.
- Colored squares indicate Gaussian widths of measured fluctuation spectra.
- Magenta line is electron bounce frequency,  $\omega_b/2\pi \sim \epsilon^{1/2}V_e/Rq$
- **Data and predictions are seen to be similar.**

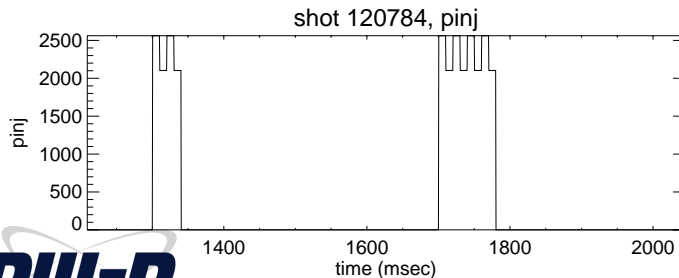
# Modulated probe beam shows signal is not due ECE



shot 120784, Point: mmspc3, time history of amplitude at f=1000.6 kHz



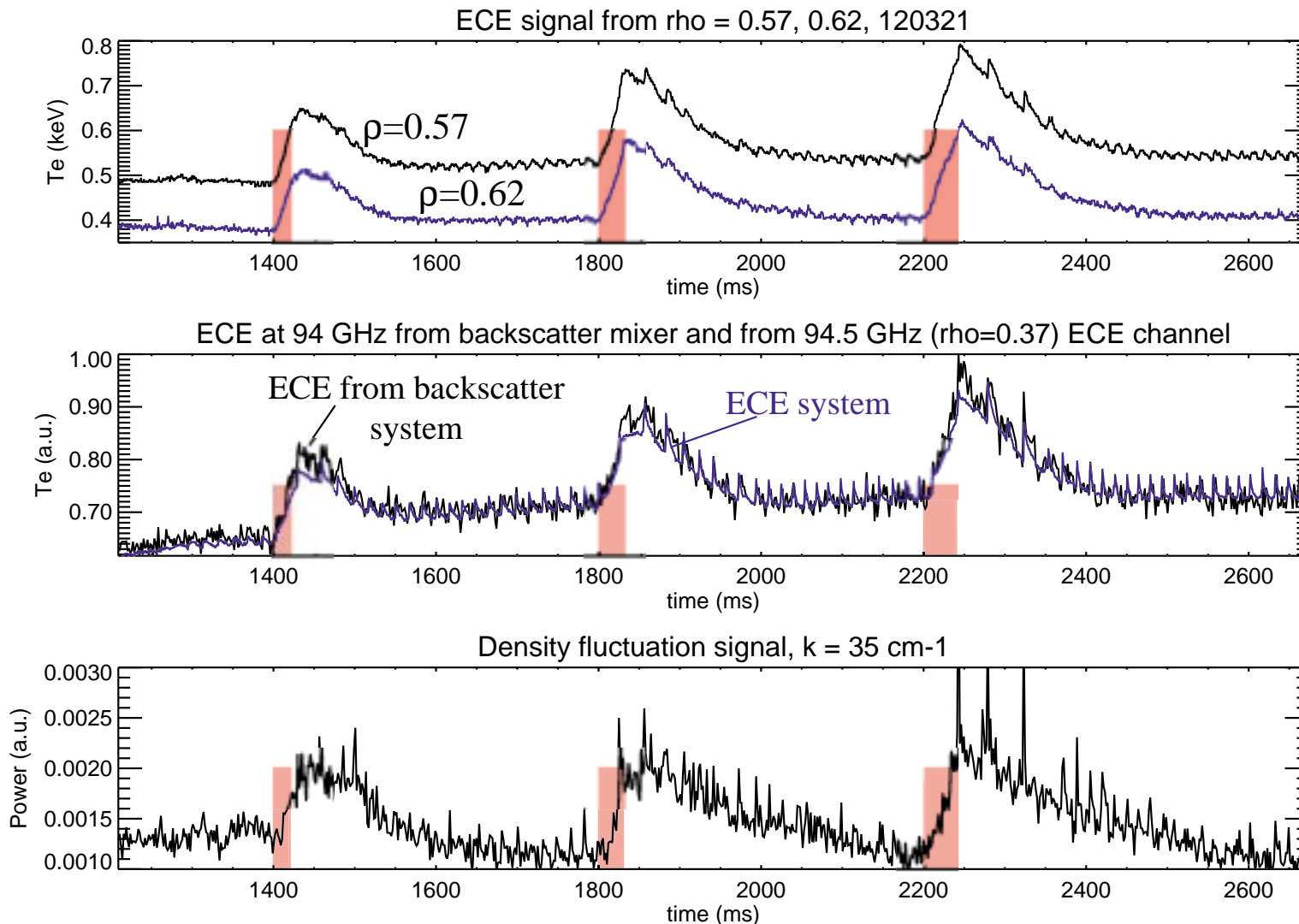
$A_{\omega}(12.8-500.6 \text{ kHz})$   $A_{\omega}(1000.6-4994.5 \text{ kHz})$   $A_{\omega}(4001.2-4011.6 \text{ kHz})$   $A=(\text{autopower})^{1/2}$



shot 120784, pinj  
nfft= 16384, fsmooth= 25.0000 kHz

- Backscatter is also a 94 GHz radiometer.
  - Some of signal is due to ECE
- Probe beam was modulated so that remaining signal is due to ECE.
- Turbulent signal clearly modulated while ECE signal is not.

# mm-wave backscatter signal not due to ECE



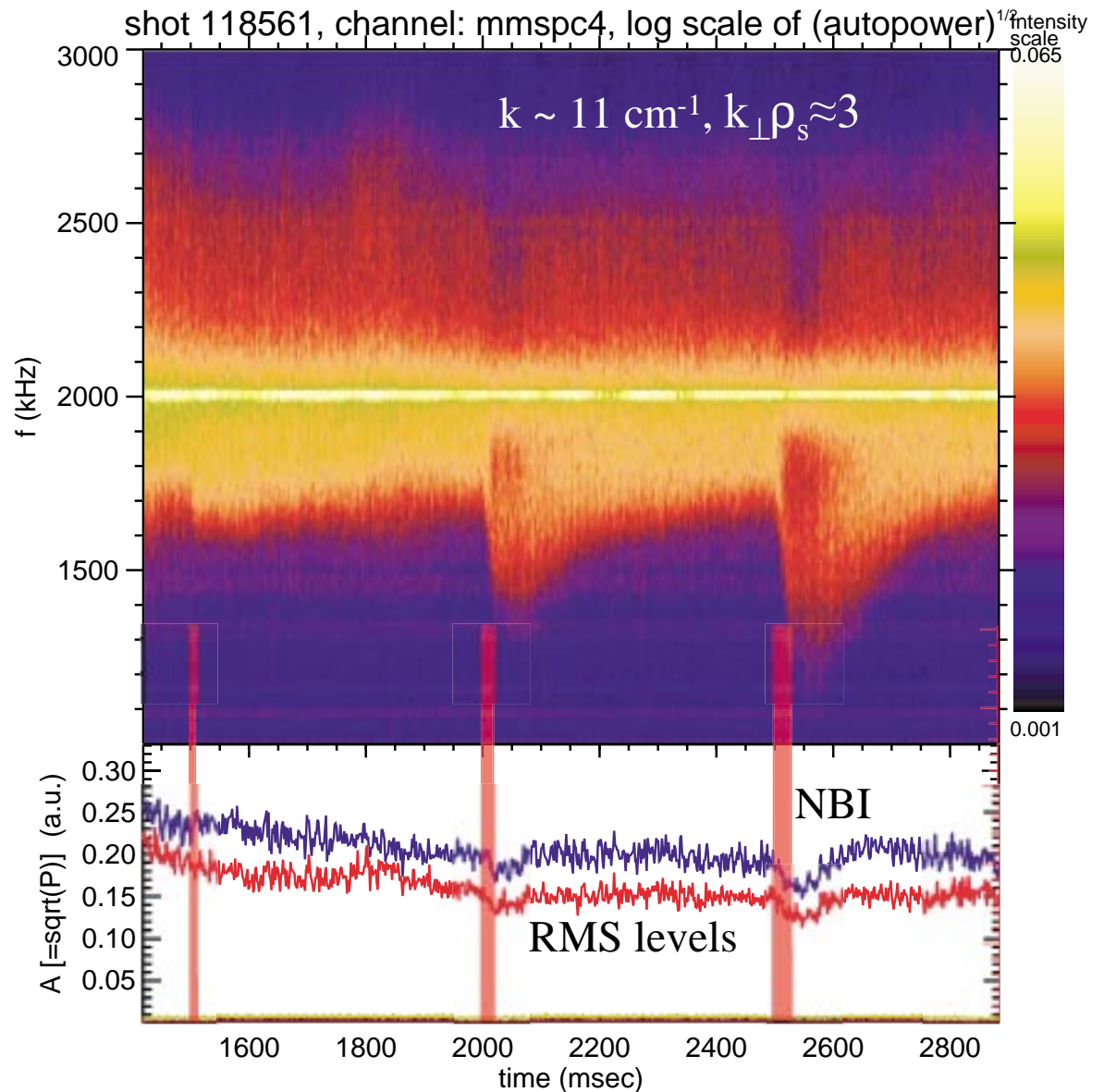
- ECE and mm-wave backscatter signals clearly different.
- mm-wave does see 94 GHz ECE which is similar to ECE system.

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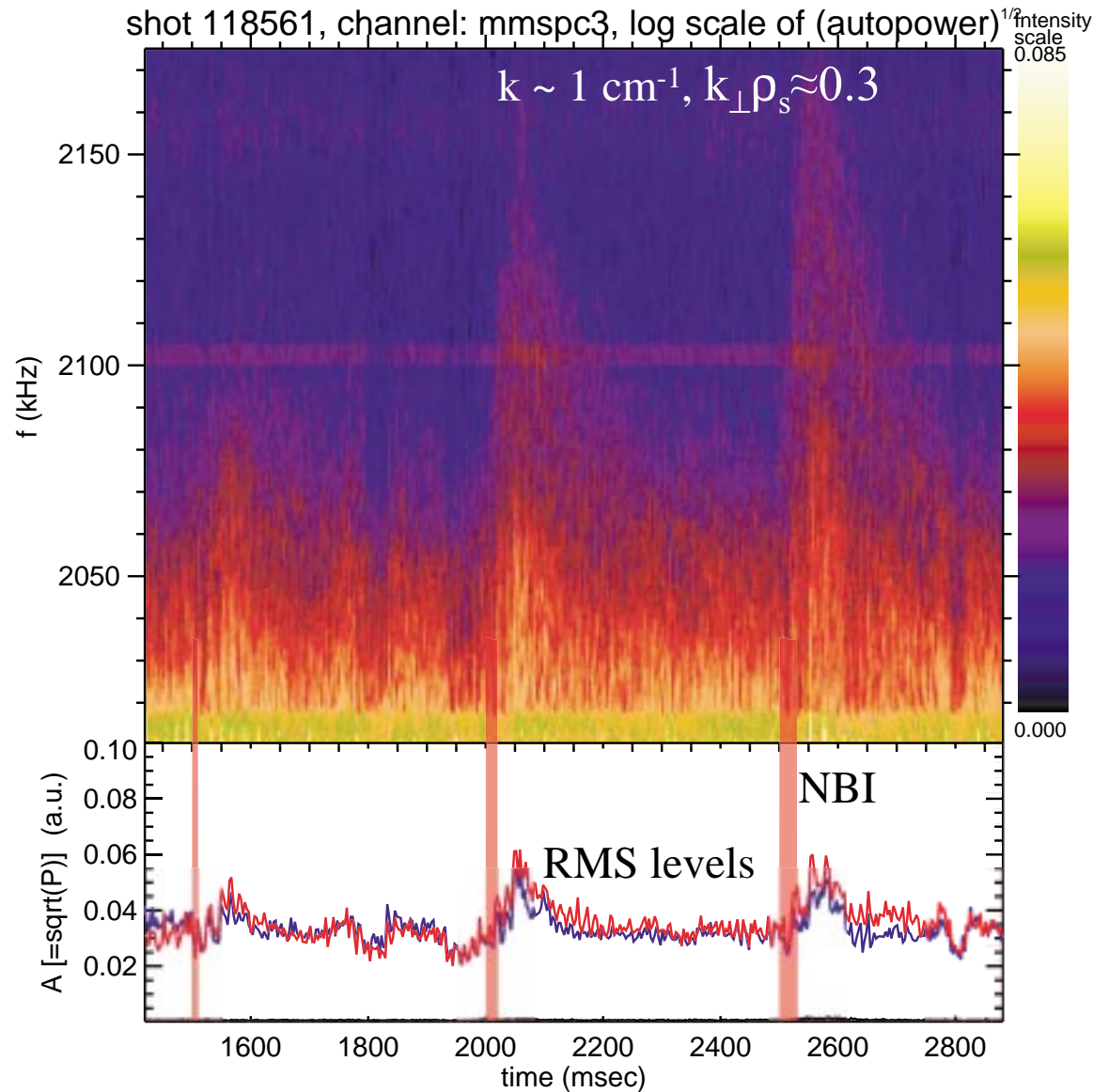
# Short duration NBI used to affect turbulence and $T_e$

- Intermediate-k ( $11 \text{ cm}^{-1}$ ,  $k_{\perp}\rho_s \approx 3$ ) turbulence **decreases** with NBI.
- Low-k ( $\sim 1 \text{ cm}^{-1}$ ,  $k_{\perp}\rho_s \approx 0.3$ ) and high-k ( $35 \text{ cm}^{-1}$ ,  $k_{\perp}\rho_s \approx 10$ ) turbulence **increase** with NBI.
- NBI increases  $T_e$  but little affect on other parameters.



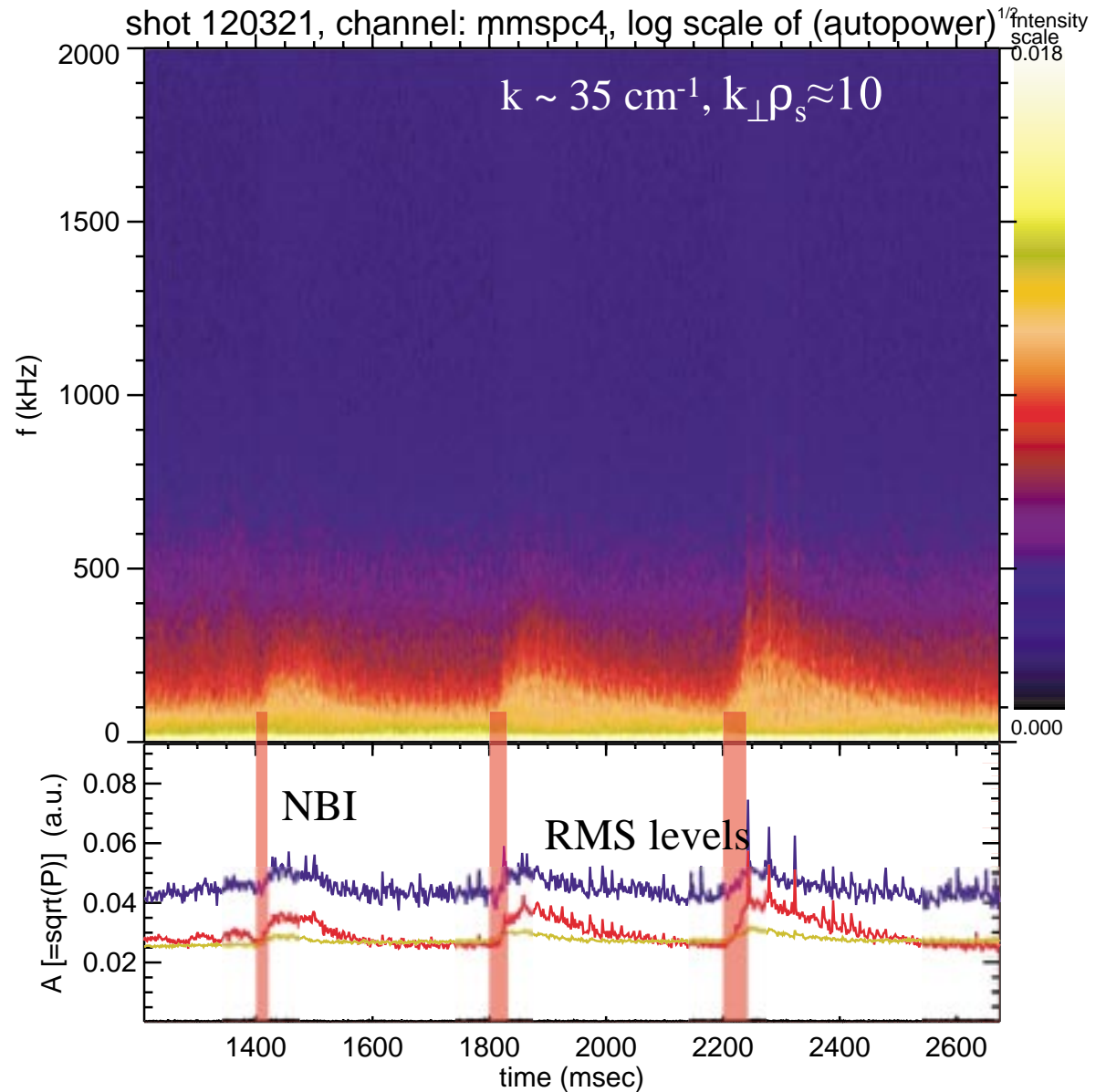
# Short duration NBI used to affect turbulence and Te

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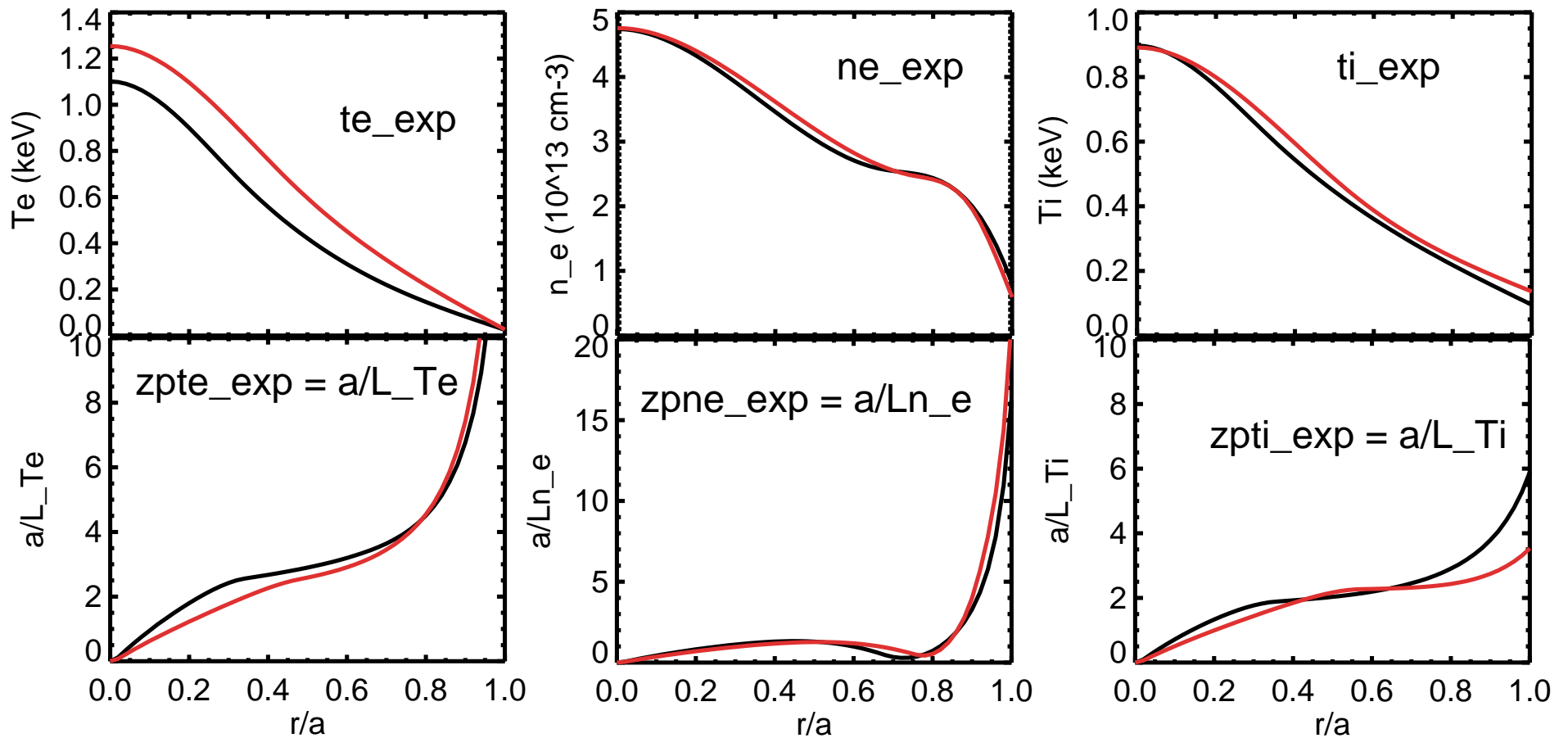


# Short duration NBI used to affect turbulence and $T_e$

- High-k ( $35 \text{ cm}^{-1}$ ,  $k_{\perp}\rho_s \approx 10$ ) turbulence **increases** with NBI.

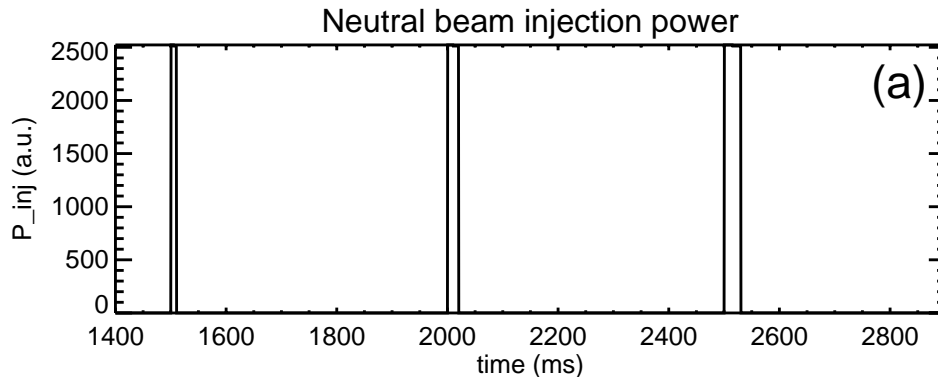


# Short duration NBI affects mostly Te

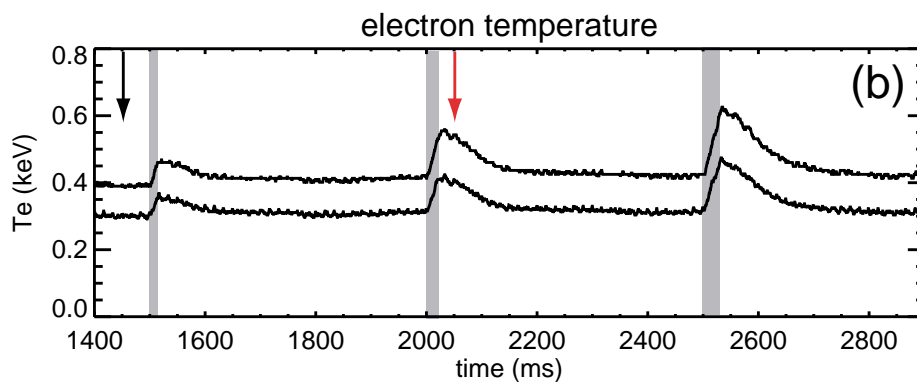


- Little change in  $L_{Te}$  or other parameters with short duration NBI

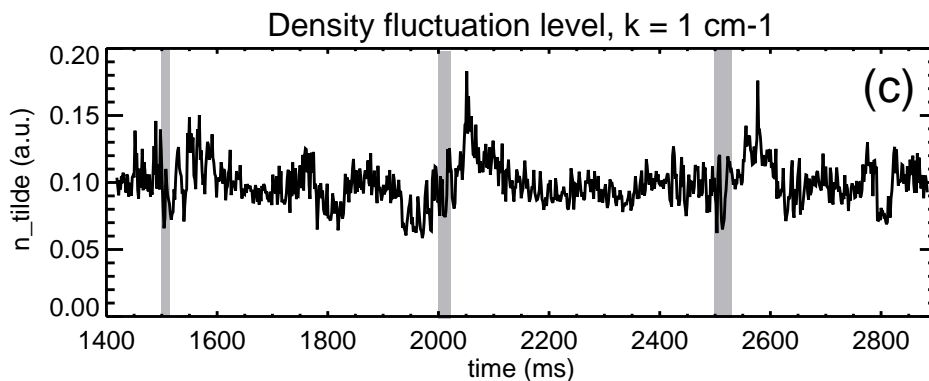
# Short duration neutral beams used to modify profiles and fluctuations



**NBI**

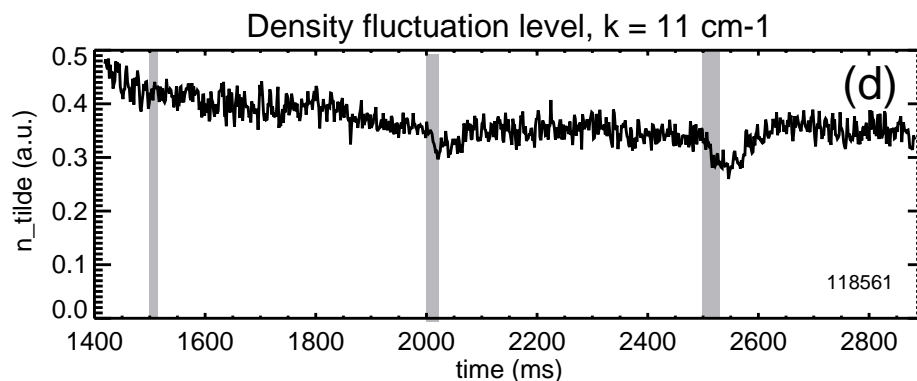


**Te**



**$\tilde{n}(k = 1 \text{ cm}^{-1})$**

**$k_{\perp} \rho_s \approx 0.3$**

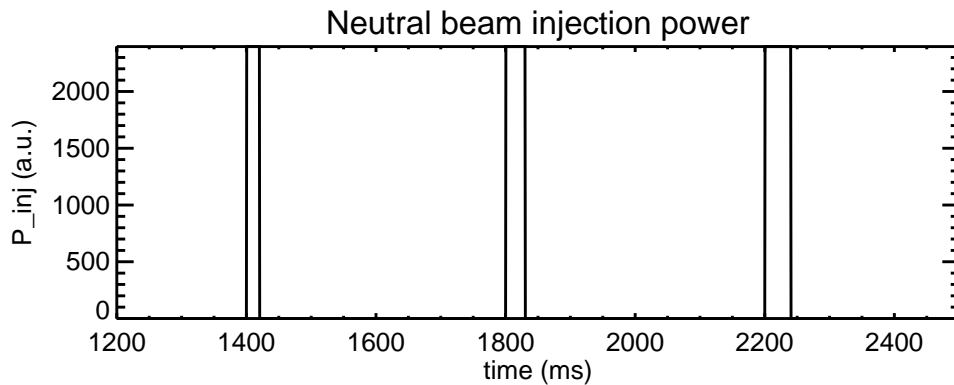


**$\tilde{n}(k = 11 \text{ cm}^{-1})$**

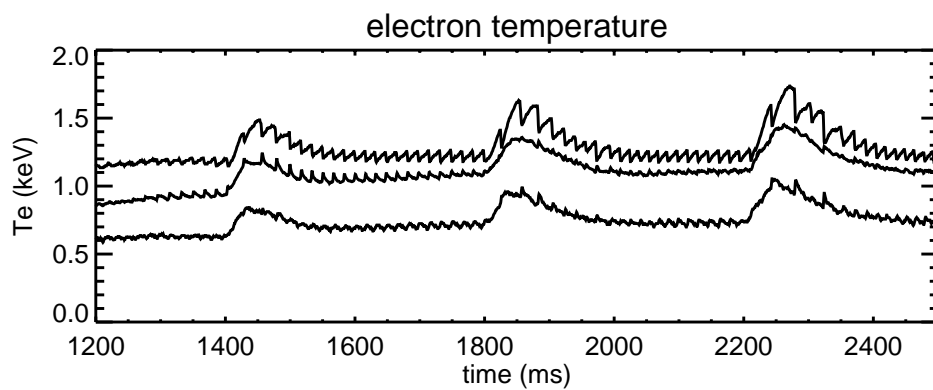
**$k_{\perp} \rho_s \approx 3$**

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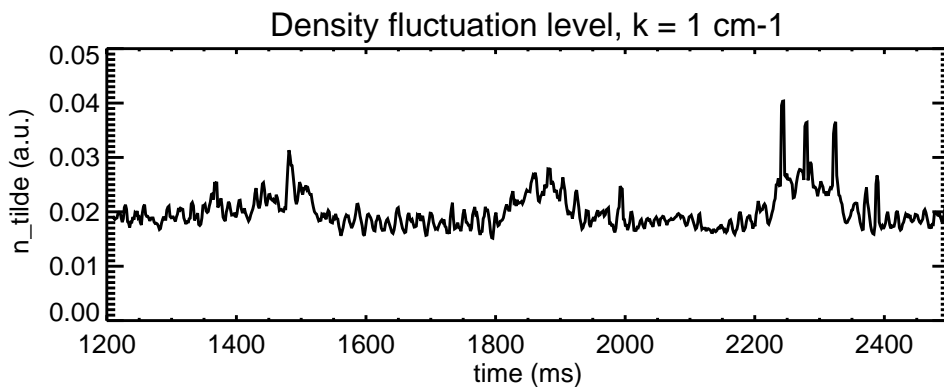
# Different discharge showing high-k



**NBI**

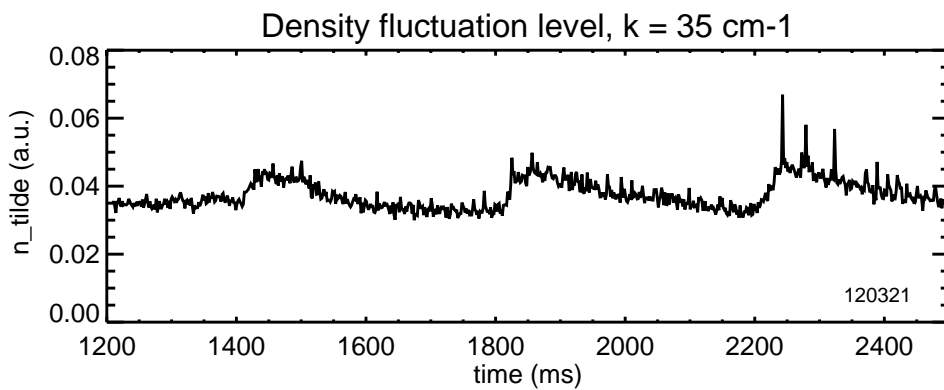


**Te**



**$\tilde{n}(k = 1 \text{ cm}^{-1})$**

**$k_{\perp} \rho_s \approx 0.3$**



**$\tilde{n}(k = 35 \text{ cm}^{-1})$**

**$k_{\perp} \rho_s \approx 10$**

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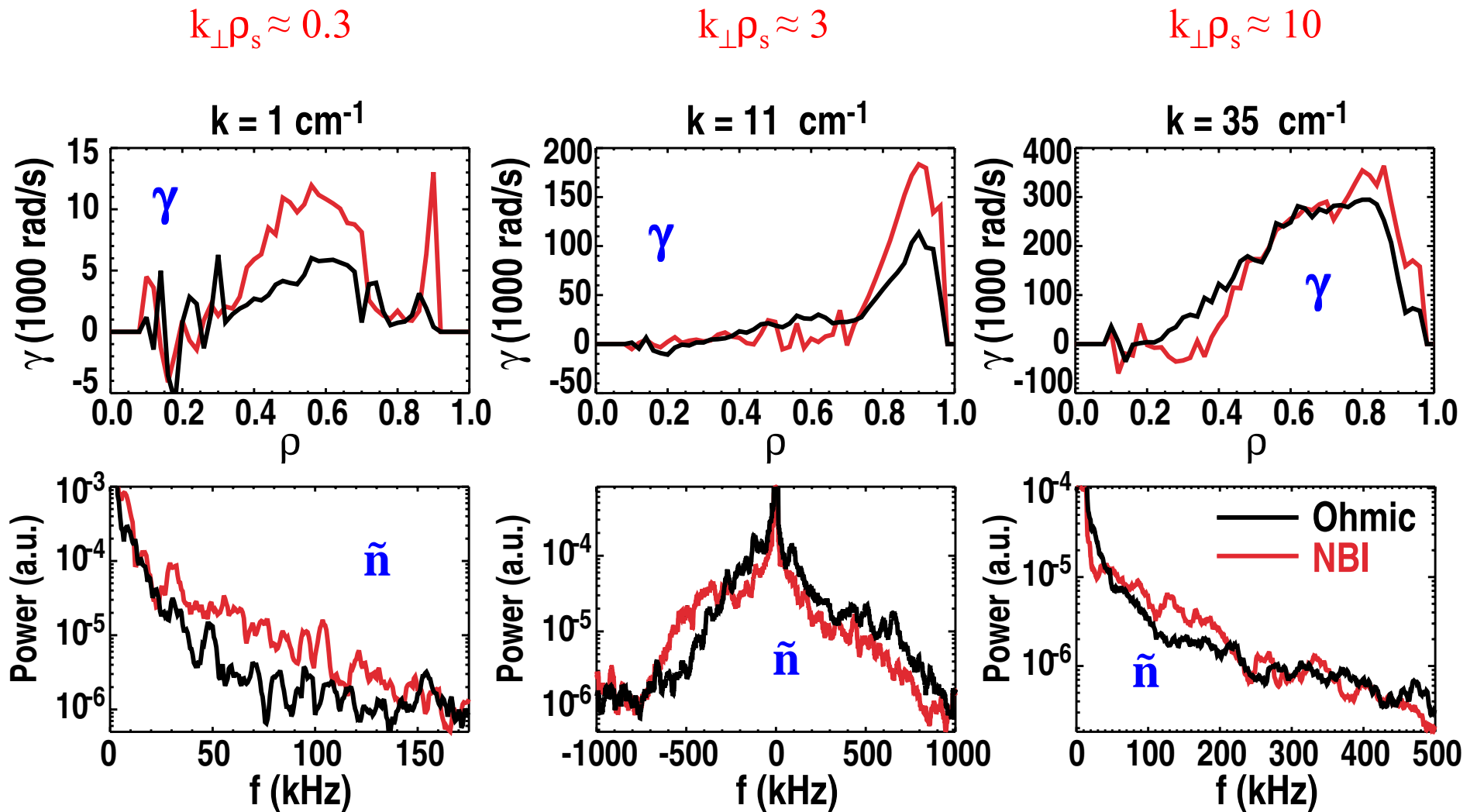
## Fluctuations respond differently depending upon wavenumber

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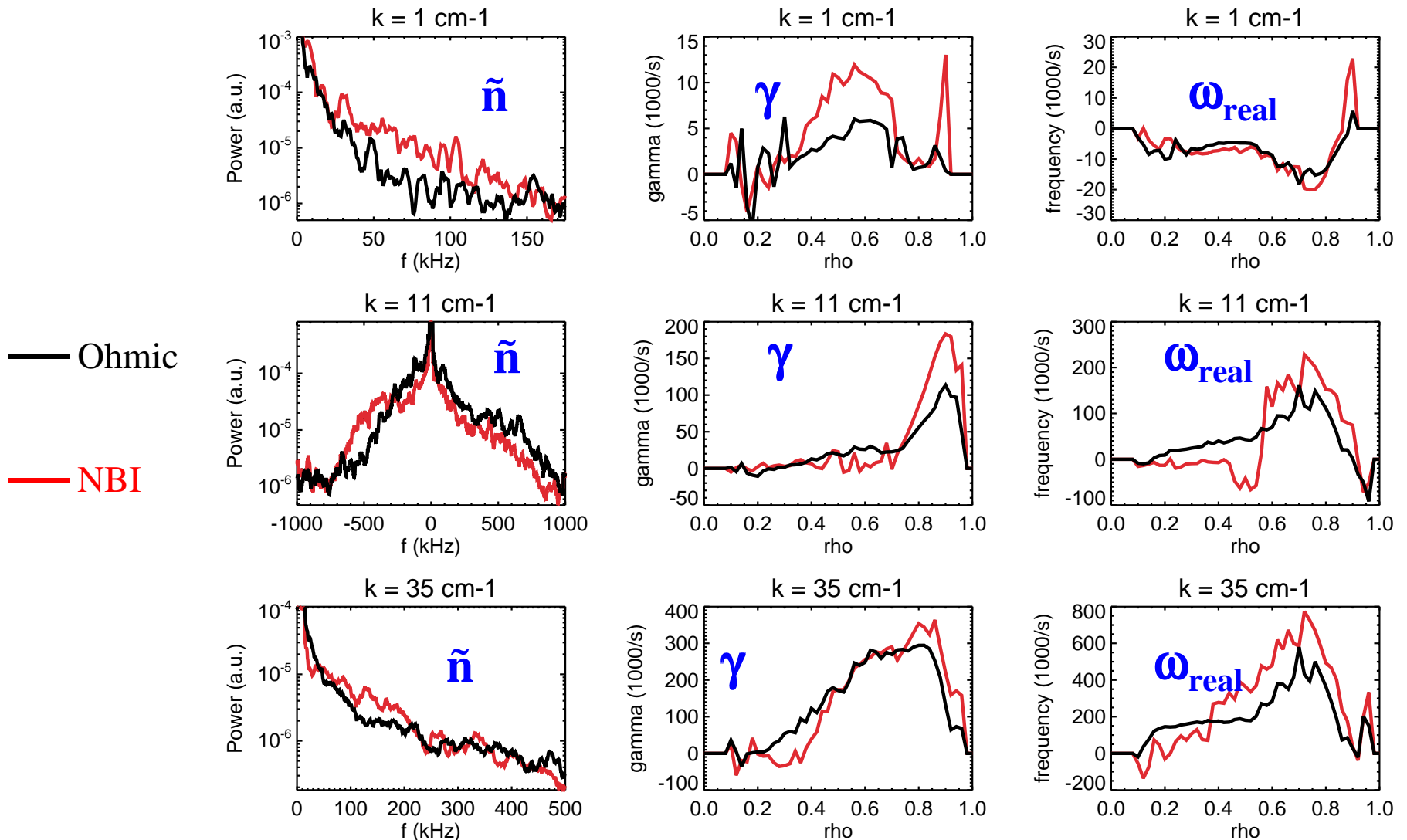
- RMS levels are integrated across the frequency range where the fluctuations appear.
- **RMS levels are seen to respond quite differently,**
  - with the low-k increasing to a maximum after the beam turns off
  - intermediate-k decreases to a minimum.
  - Interestingly the high-k fluctuations also increase

# Response to short duration NBI: both $\tilde{n}$ measurements and GKS predictions vary with wavenumber





# Response to short duration NBI: both $\tilde{n}$ measurements and GKS predictions vary with wavenumber



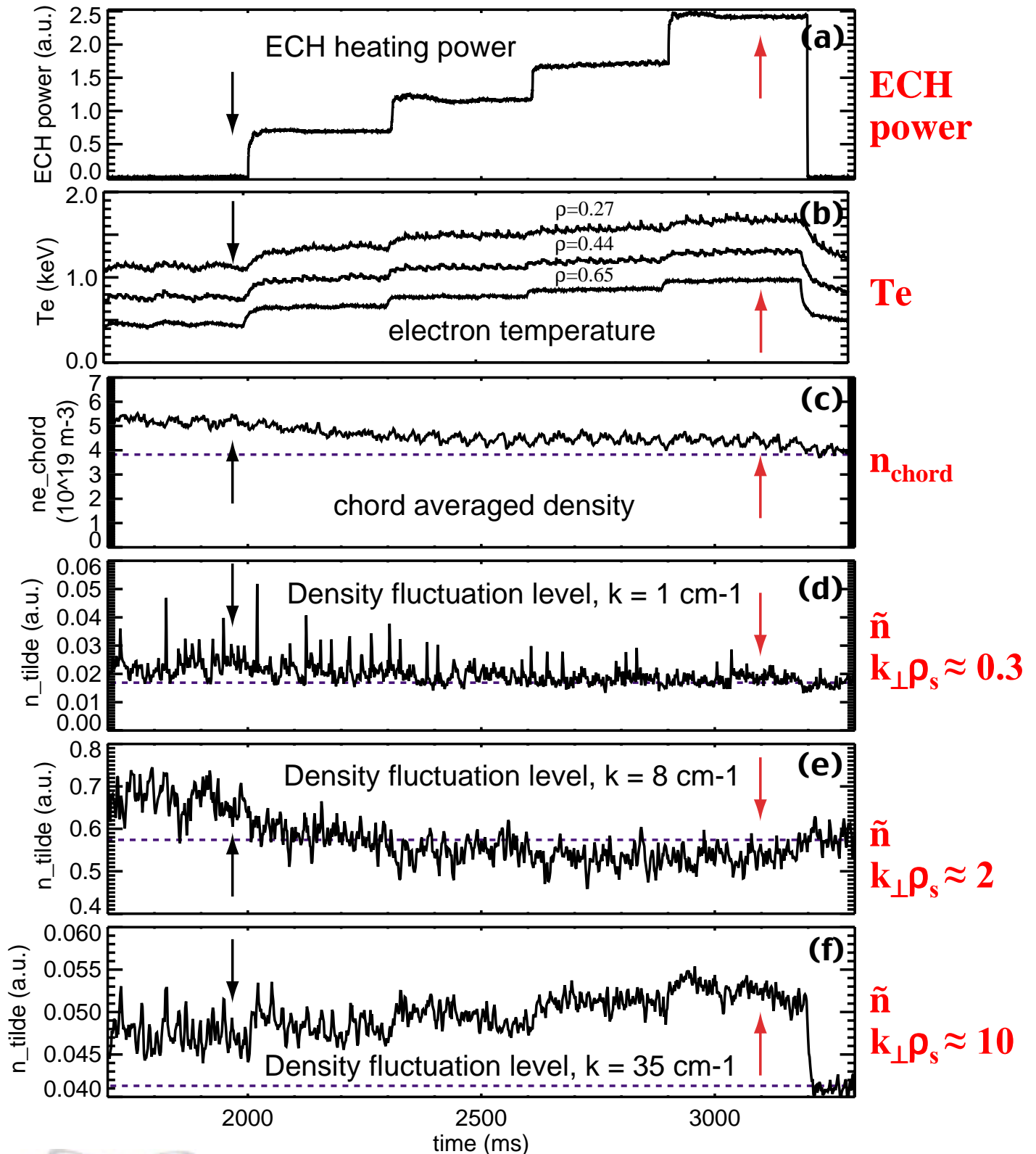
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# Response to short duration NBI: high and intermediate k measurements differ from expectation

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- GKS calculations for low-k ( $k_{\perp}\rho_s \approx 0.3$ ) show an increase in growth rate over much of radius consistent with observed fluctuation increase.
- Intermediate-k ( $k_{\perp}\rho_s \approx 3$ ) decreases with NBI but GKS predicts increase at edge and possible decrease in core.
- High-k ( $k_{\perp}\rho_s \approx 10$ ) increases with NBI but GKS shows little change.
  - Only change in plasma is increase in  $T_e$  so that increase in high-k seemingly contrary to expectation.

# Electron cyclotron heating (ECH) modifies profiles ( $n_e$ and $T_e$ ) and fluctuations



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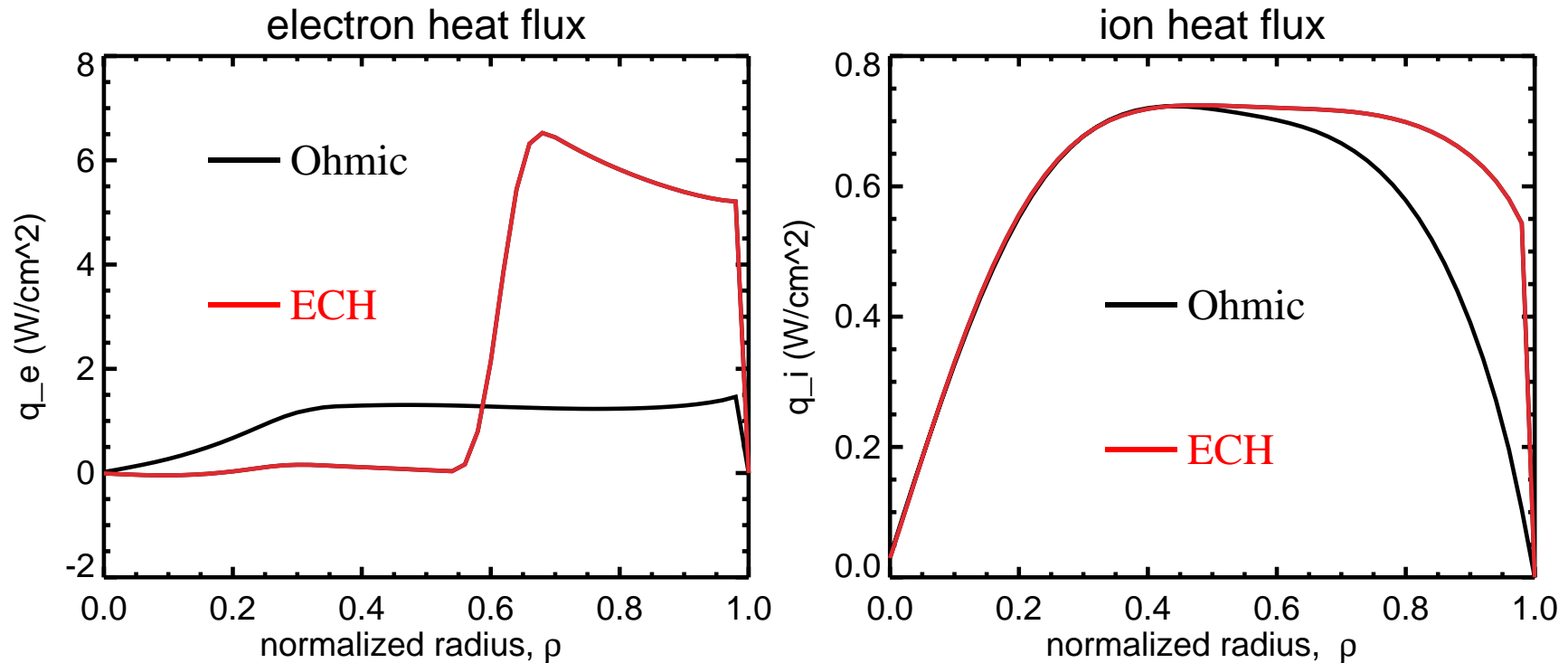
## Electron cyclotron heating (ECH) resulted in different changes for different wavenumbers

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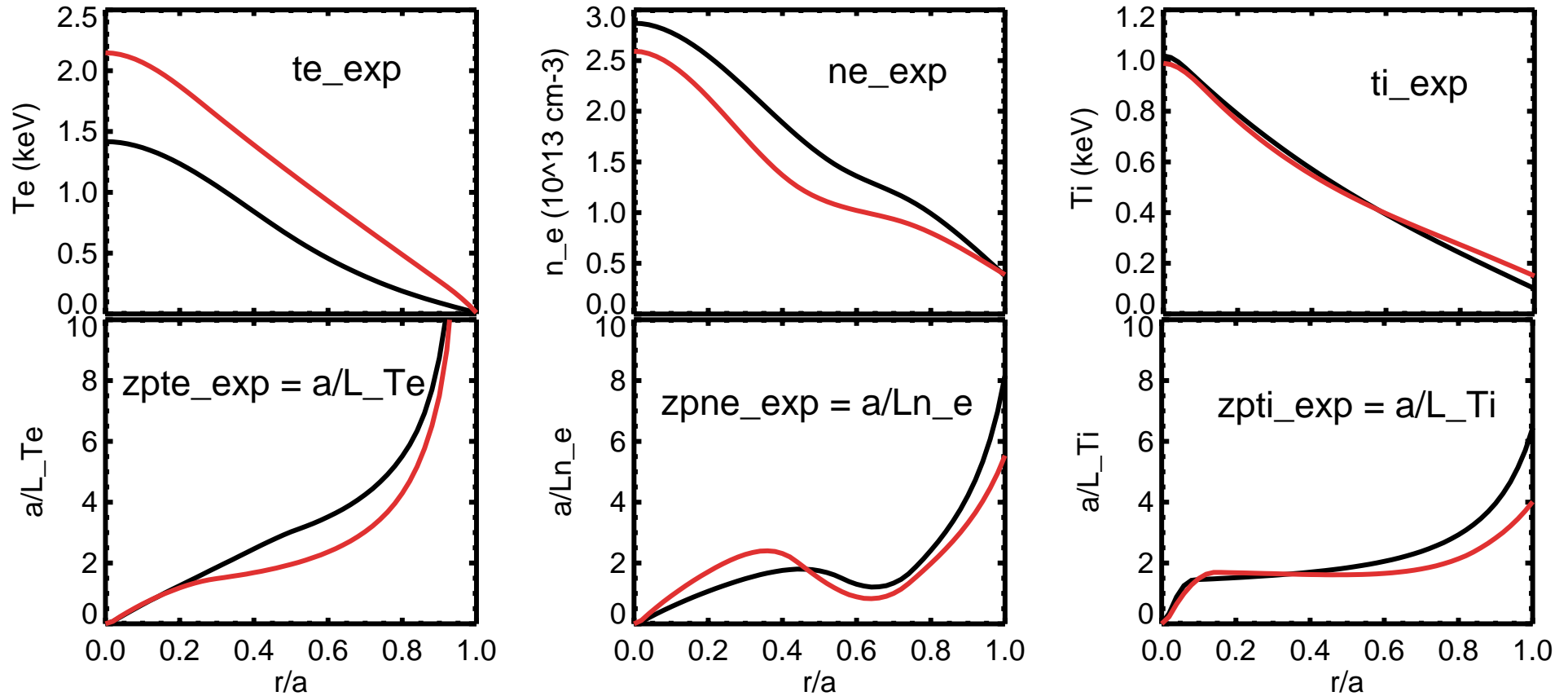
- Integrated fluctuation signals from low-k did not change appreciably with ECH
- Intermediate-k decreases ( $\sim 10\%$ )
- high-k increases ( $\sim 10-15\%$ ).
- The high-k fluctuation level decreases rapidly after ECH turn-off, similar to the Te signal from the outer part of the plasma
- It should be noted that Ti did not change appreciably during the ECH.

## With ECH electron heat flux increases for $\rho \geq 0.55$



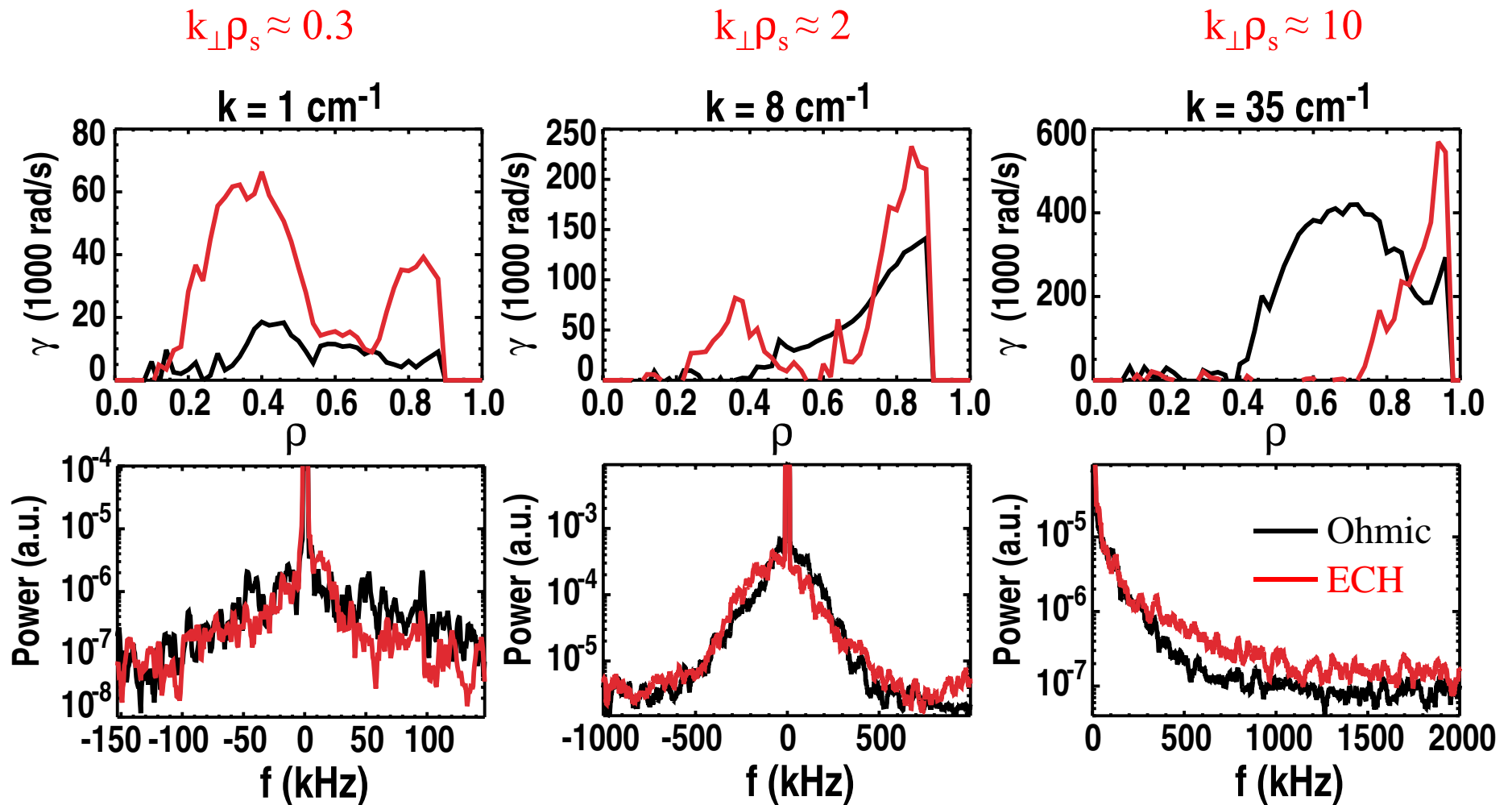
- Increase in  $q_e$  correlates with increase in high-k fluctuations, intermediate-k centered at  $\rho=0$  so decrease in  $q_e$  might also be consistent.
- Ion heat flux also increases, but to a smaller extent, doesn't appear to correlate well with little or no change in low-k fluctuations.

# ECH affects both $n_e$ and $T_e$ and their scale lengths

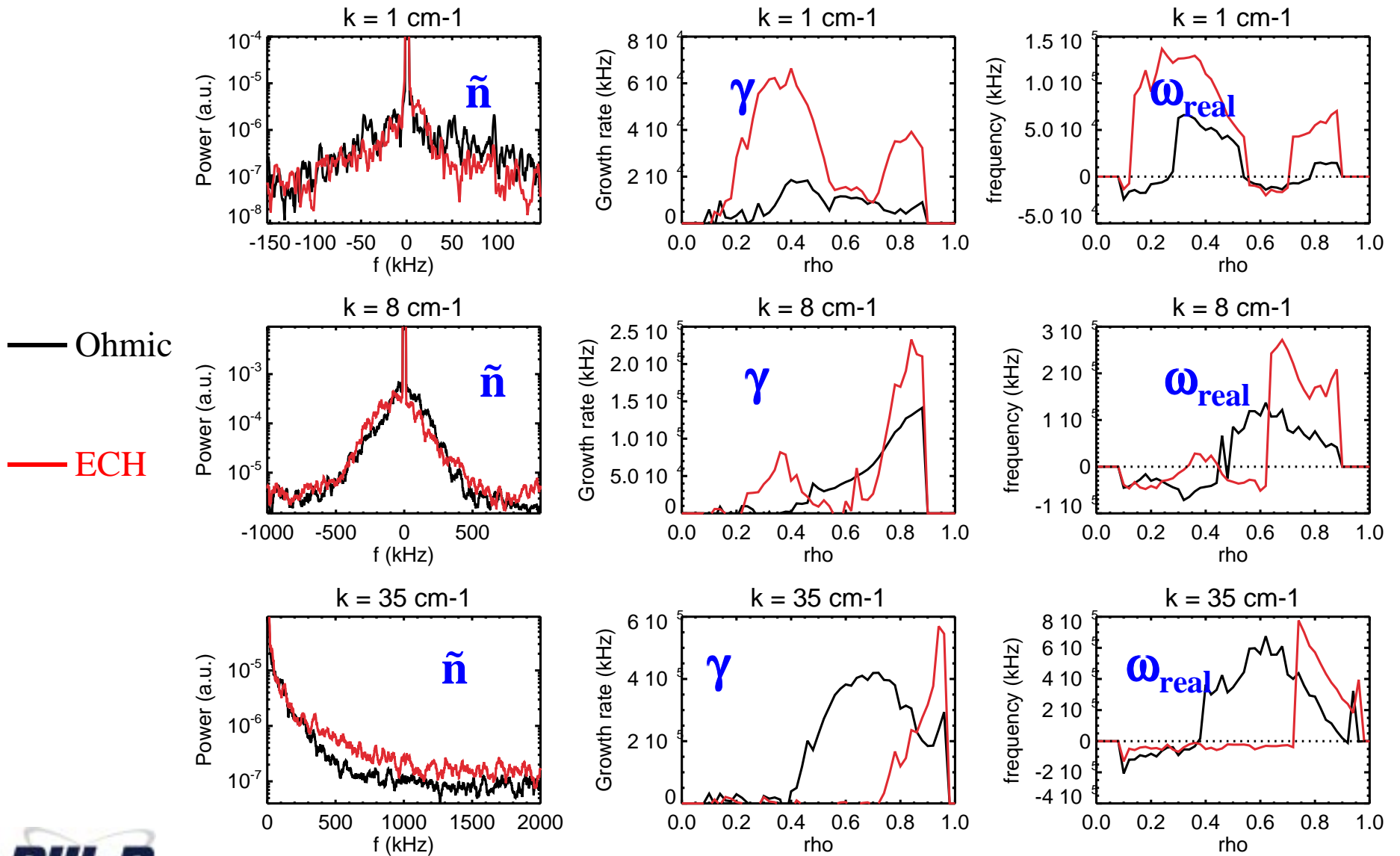


- Little change in  $T_i$  with ECH

# Response to ECH: both $\tilde{n}$ measurements and GKS predictions vary with wavenumber



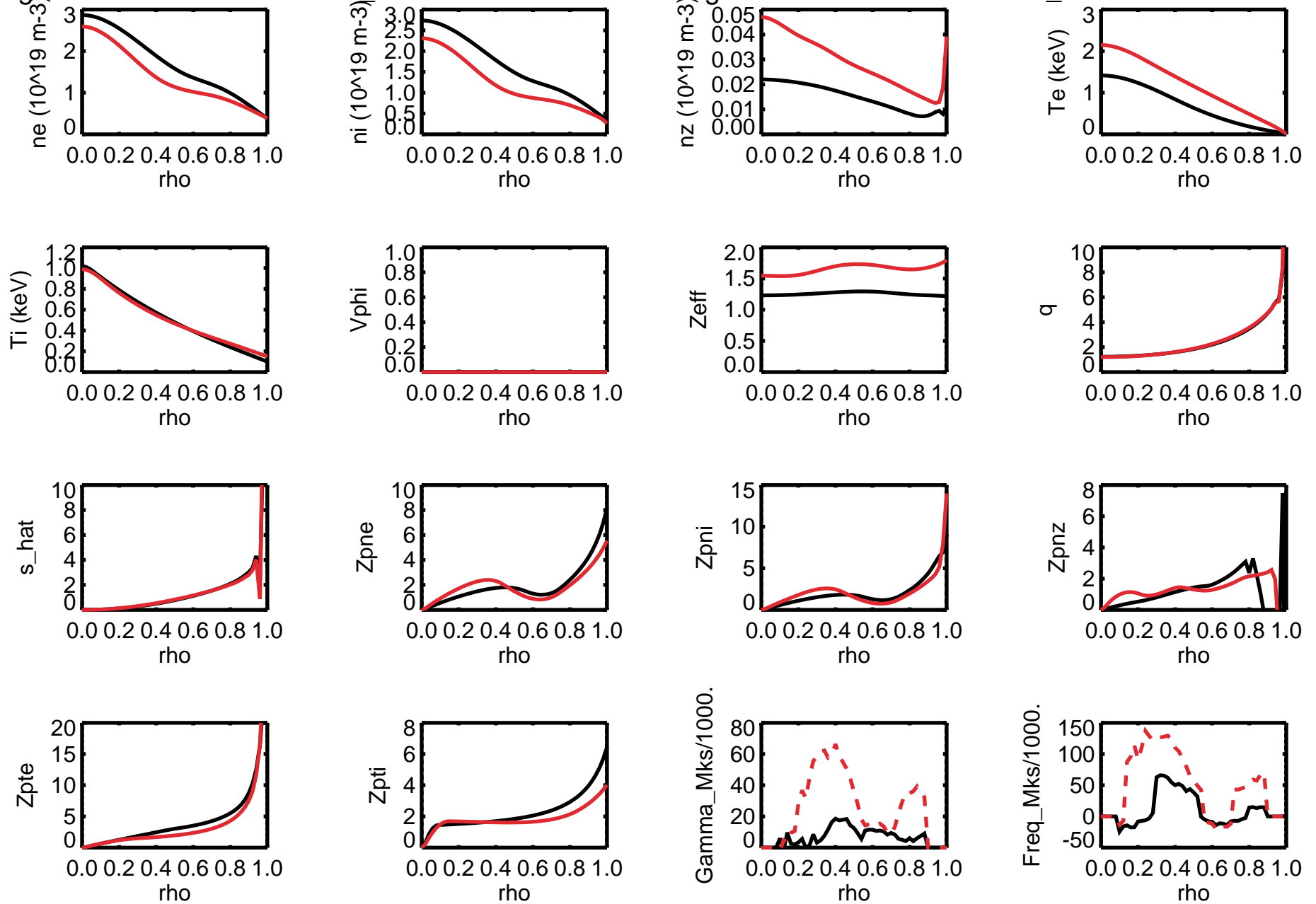
# Response to ECH: both $\tilde{n}$ measurements and GKS predictions vary with wavenumber





odes/gks/120327/120327.1975.k\_1.v2.nc

.../u/rhodes/gks/120327/120327.3100.k\_1.v2.nc



# Response to ECH: both $\tilde{n}$ measurements and GKS predictions vary with wavenumber

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- GKS calculations for low-k ( $k_{\perp}\rho_s \approx 0.3$ ) appears different from observations but  $E_r'$  needs to be accounted for.
- Growth rates for intermediate-k ( $k_{\perp}\rho_s \approx 2$ ) both decrease and increase with ECH.
  - Observed signal comes from different radii so different frequencies may be associated with different radial positions, indicating a radial variation in fluctuation response.
- Growth rates for  $k = 35 \text{ cm}^{-1}$  ( $k_{\perp}\rho_s \approx 10$ ) decrease in core and increase near edge.
  - Experimental data shows an increase which appears inconsistent with the signal coming from a radial extent of  $\rho = 0.4$  to  $1.0$ .
  - Very interesting observation with more work needed to fully understand it.
- Changes in electron heat flux roughly correlate with high-k fluctuation changes.
  - Ion heat transport does not appear to correlate with low-k fluctuations.

# Summary

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- First measurements of high-k turbulence ( $k \sim 35 \text{ cm}^{-1}$ ,  $k_{\perp} \rho_s \approx 10$ ) on DIII-D have been made.
  - Combined with low and intermediate-k measurements, these provide a new, more complete picture of turbulence behavior on DIII-D.
  - Clear turbulence signals at  $k \sim 35 \text{ cm}^{-1}$ ,  $k_{\perp} \rho_s \approx 10$  using new mm-wave backscatter.
  - $k_{\perp} \rho_s \sim 0.2-10$  a range relevant to ITG, TEM and ETG instabilities.
- GKS code shows plasma unstable to ITG, TEM, and ETG consistent with observed turbulent activity
  - however some differences between GKS and observations found.
  - High-k ( $k \sim 35 \text{ cm}^{-1}$ ,  $k_{\perp} \rho_s \approx 10$ ) turbulence increases with  $T_e$  increase (with  $L_n$ ,  $L_{Te} \sim \text{constant}$ ) seemingly contrary to expectation.
- Both measured and calculated response to perturbations (NBI, ECH) varied with wavenumber, supporting need for broad wavenumber comparisons.