

Modeling Edge Plasma Response to 3D Fields in DIII-D

by

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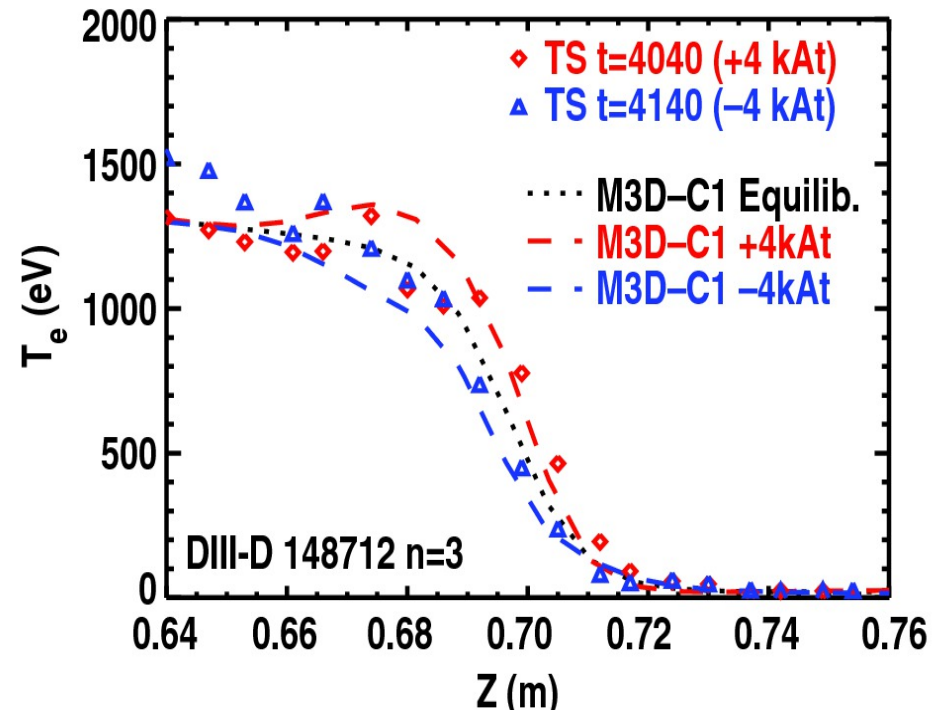
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Measurements of Edge Response to 3D Fields Are Generally in Good Agreement With Two-Fluid Modeling

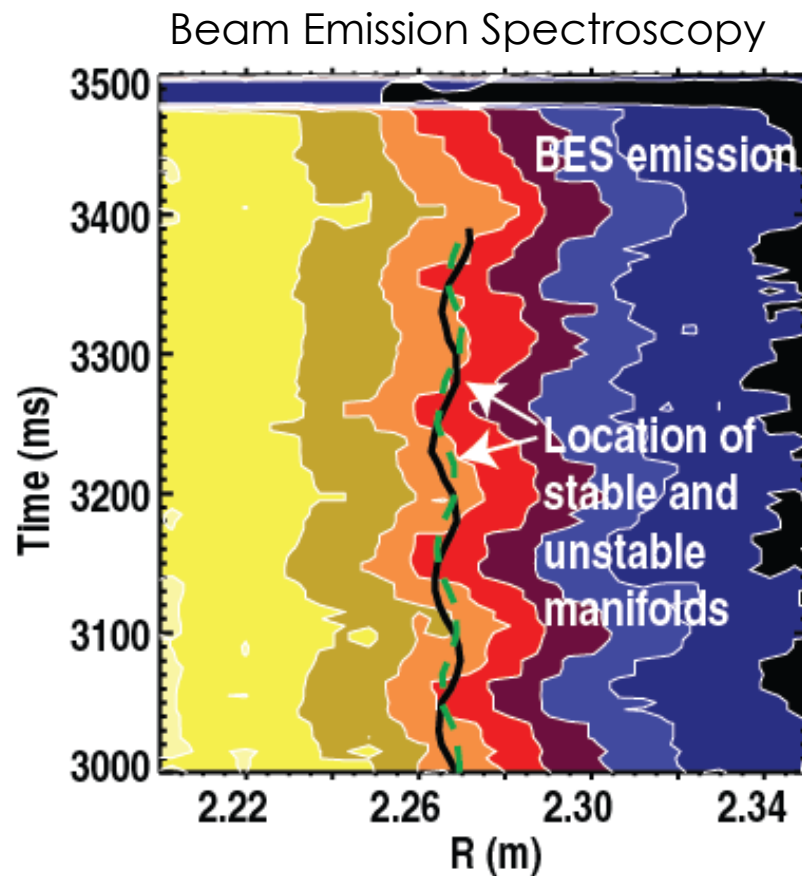
- **3D fields have significant impact on tokamak performance**
 - ELM suppression, pump-out, braking, etc.
- **Edge displacements are a robust feature of 3D plasma response**
 - Provide a measurement for validating codes
 - Provide an indication of internal plasma response
- **We find generally good agreement between two-fluid modeling (M3D-C1) and measurements of edge response**

T_e profile is “displaced” by 3D fields



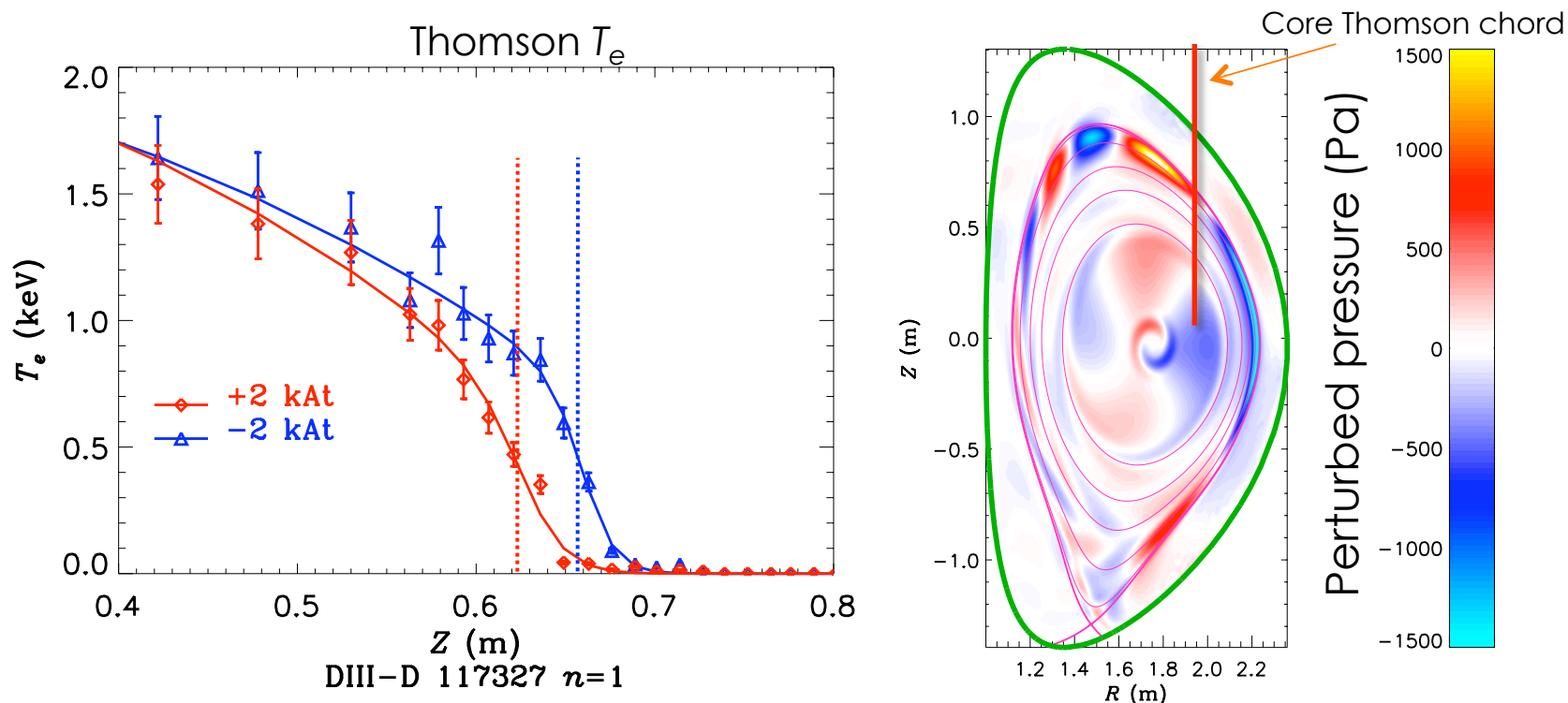
Rotating $n=1,2$ Fields Sweeps Structures Past Diagnostics

- On DIII-D, the toroidal phase of $n=1$ and $n=2$ fields can be smoothly rotated
- Displacement is phase dependent
- **Two possibilities**
 - Displacement is 3D
 - Displacement is 2D, but phase dependent (i.e. there are significant error fields)
- **Measured displacement is generally larger than calculated displacement of separatrix manifolds from vacuum fields**



Large Displacements Also Observed Along Core Thomson Chord

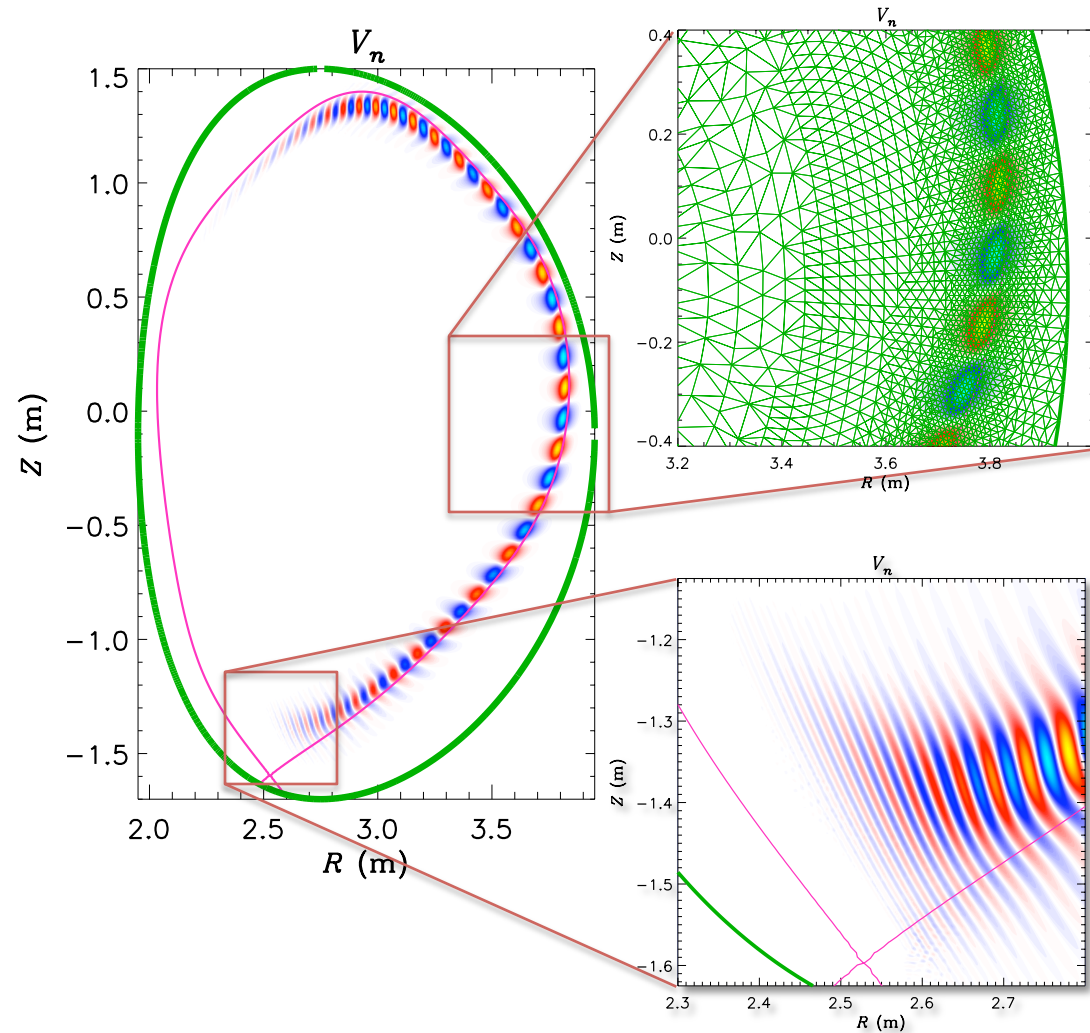
- Measurements show significant (2–4 cm) displacements of edge n and T profiles when $n=1$ 3D fields are applied



- Separatrix displacements due to vacuum fields are only ~few mm

Linear Plasma Response to 3D Fields is Modeled with M3D-C1

- **M3D-C1 \neq M3D**
- **Model includes**
 - Two-fluid effects
 - Realistic resistivity
 - Scrape-off layer
 - Diverted geometry
- **Mesh can be packed anisotropically**
- **Can solve linear or nonlinear response**
 - Here we consider linear response



Two-Fluid Model Implemented in M3D-C1

$$\frac{\partial n}{\partial t} + \nabla \cdot (n\mathbf{u}) = 0$$

$$n \left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right) = \mathbf{J} \times \mathbf{B} - \nabla p - \nabla \cdot \Pi$$

$$\frac{\partial p}{\partial t} + \mathbf{u} \cdot \nabla p = -\Gamma p \nabla \cdot \mathbf{u} - \frac{d_i}{n} \mathbf{J} \cdot \left(\Gamma p_e \frac{\nabla n}{n} - \nabla p_e \right) - (\Gamma - 1) \nabla \cdot \mathbf{q}$$

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

$$\mathbf{E} = -\mathbf{u} \times \mathbf{B} + \eta \mathbf{J} + \frac{d_i}{n} (\mathbf{J} \times \mathbf{B} - \nabla p_e)$$

$$\Pi = -\mu \left[\nabla \mathbf{u} + (\nabla \mathbf{u})^T \right]$$

$$\mathbf{q} = -\kappa \nabla p - \kappa_{\parallel} \mathbf{b} \mathbf{b} \cdot \nabla \left(\frac{p_e}{n} \right)$$

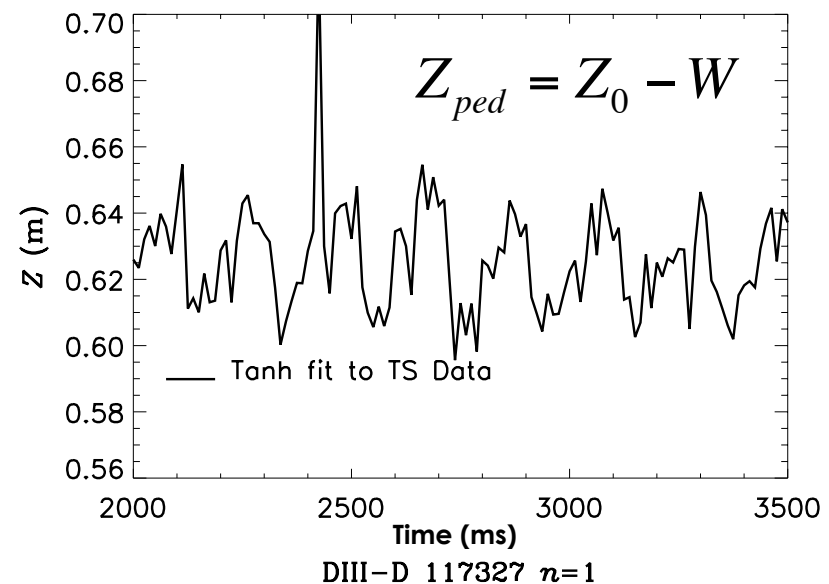
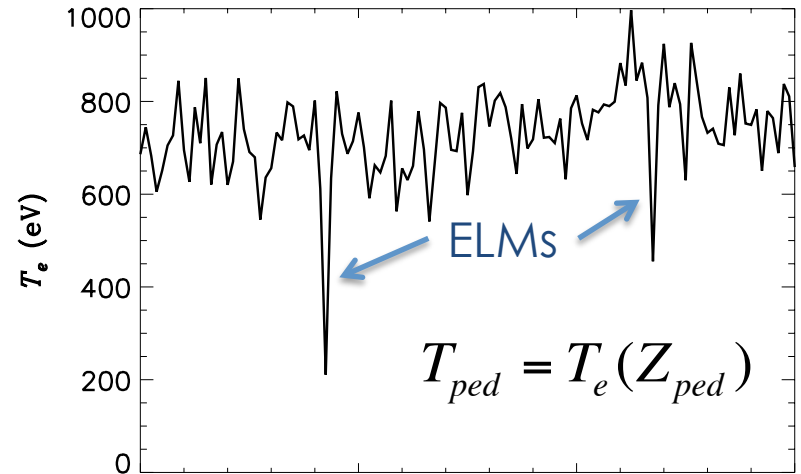
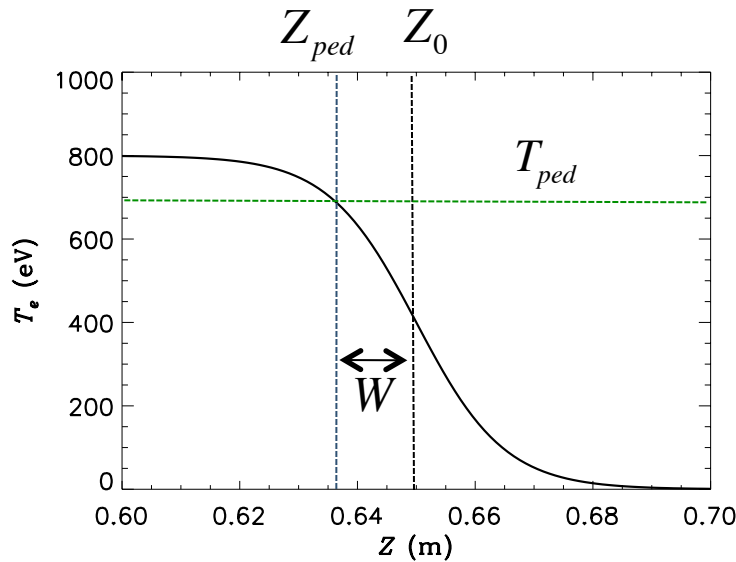
$$\mathbf{J} = \nabla \times \mathbf{B}$$

$$\Gamma = 5/3$$

$$p_e = p/2$$

- **Two-fluid** terms
- **Time-independent** equations may be solved directly for linear response
- **Boundary conditions:** normal \mathbf{B} from external coils is held constant at boundary

Displacement Can Be Quantified By The Change In The Location Of The Pedestal Top



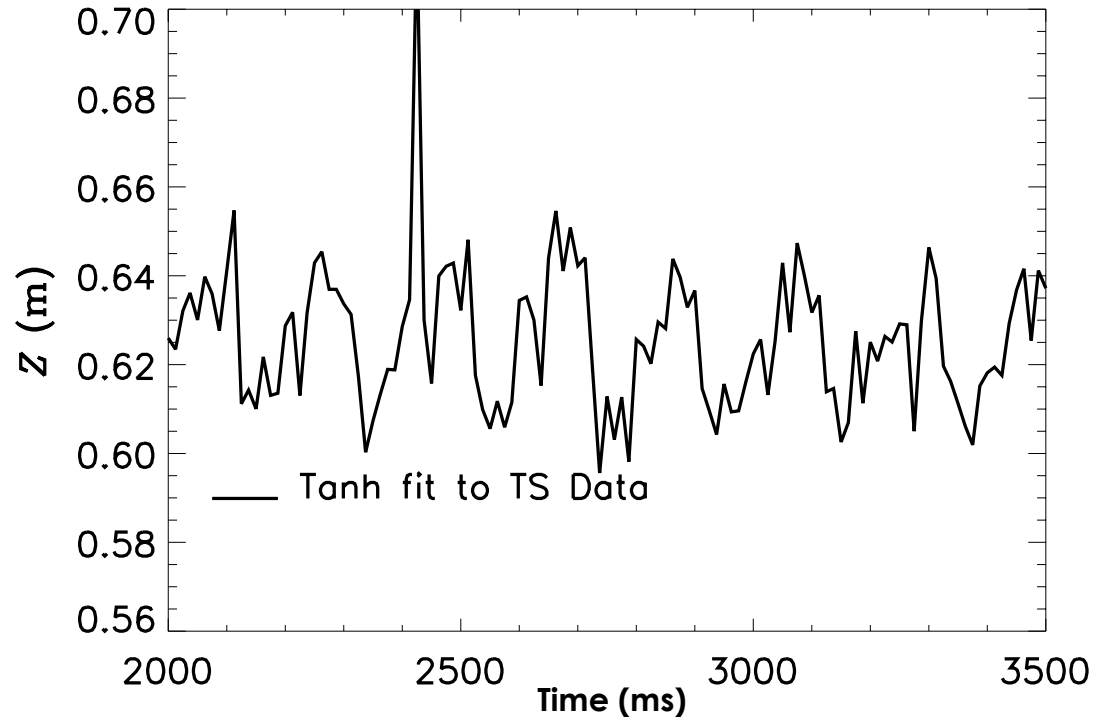
- Pedestal top Z_{ped} is defined by tanh fit to data

$$T_e(Z) = \frac{T_0}{2} \left[1 - \tanh\left(\frac{Z - Z_0}{W}\right) \right]$$

- Z_{ped} oscillates with phase of applied field (5 Hz)
- Little change in T_{ped}

Two-Fluid Modeling Reproduces Phase and Magnitude of Displacement

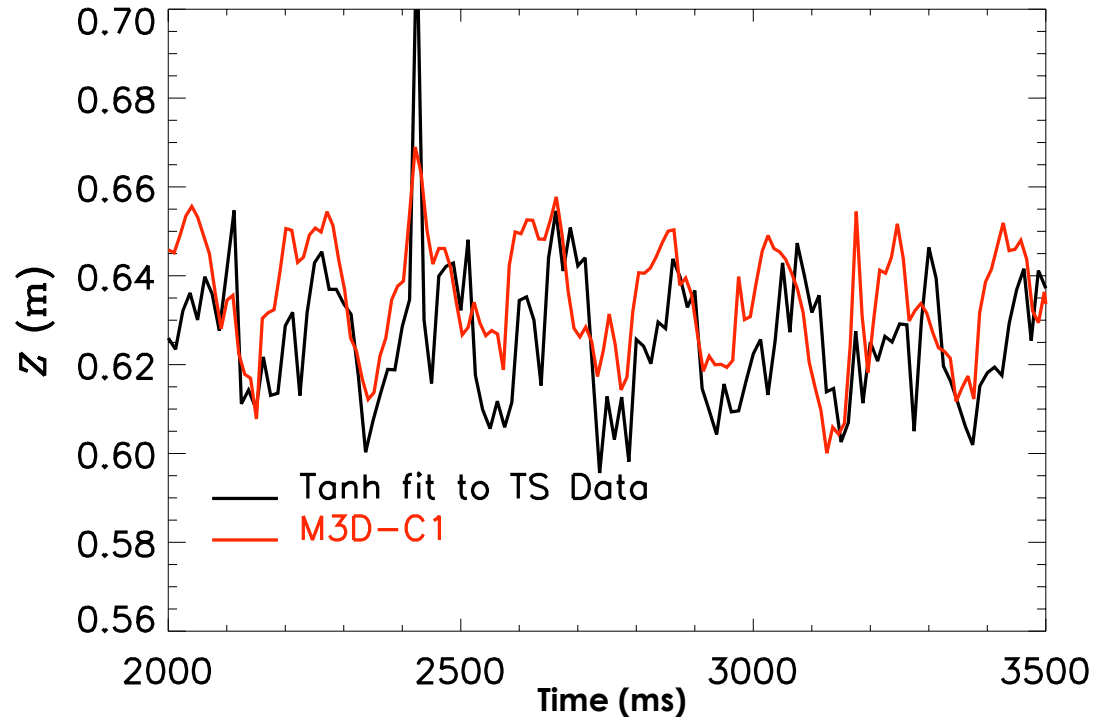
- In the experiment, the peak-to-peak displacement is ~ 4 cm
- Vacuum modeling finds few mm



DIII-D 117327 $n=1$

Two-Fluid Modeling Reproduces Phase and Magnitude of Displacement

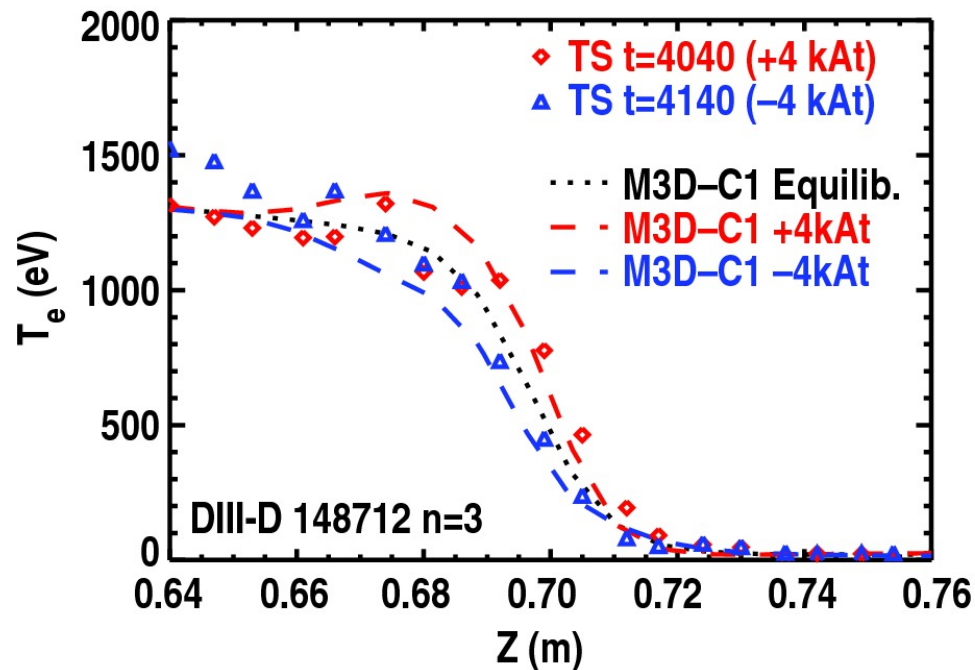
- In the experiment, the peak-to-peak displacement is ~4 cm
- Vacuum modeling finds few mm
- M3D-C1 Modeling finds good agreement in phase and magnitude of displacement



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$n=3$ Fields Yield Smaller Displacements Than $n<3$

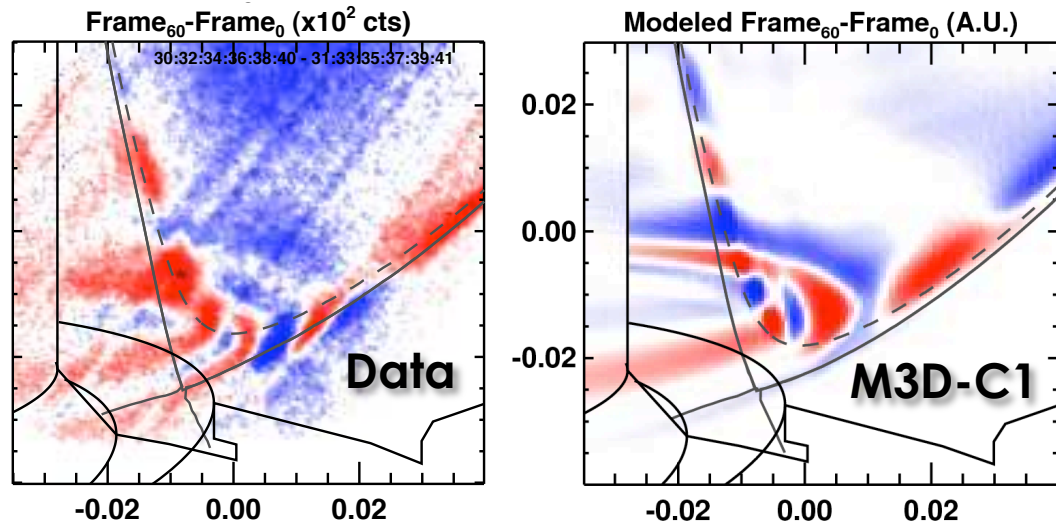
- $n=3$ fields cannot be rotated on DIII-D, but can be flipped
- Flipping $n=3$ fields yields displacement of $\sim 1\text{--}2$ cm



- M3D-C1 finds agreement through much of pedestal

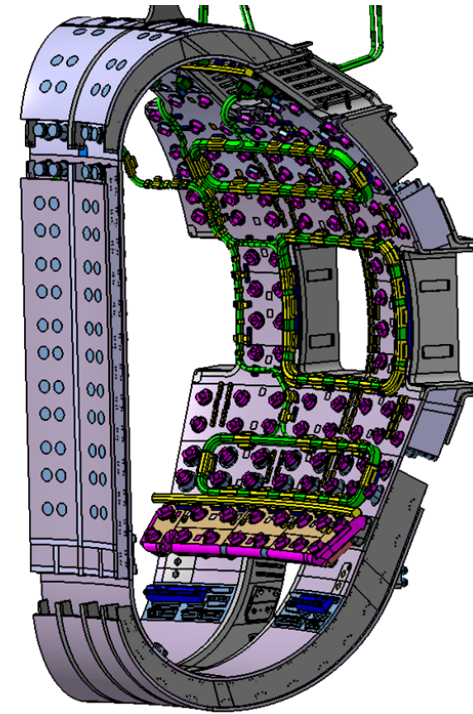
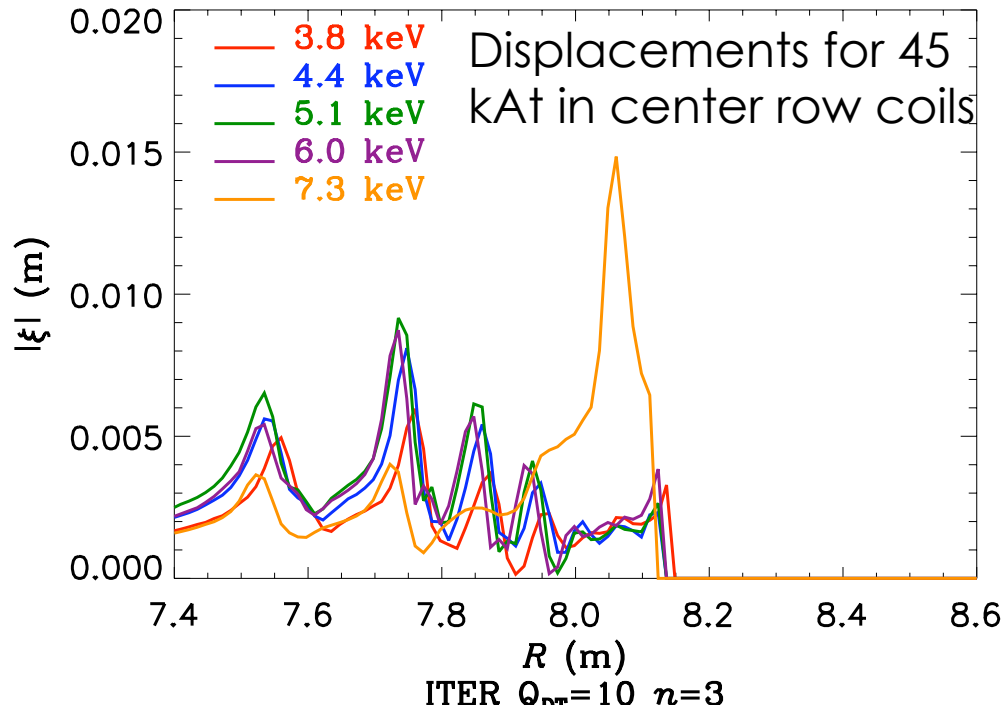
X-Ray Data Reveals Field-Aligned 3D Structure

- Data is obtained by flipping I-coil fields and taking difference between signals



- The poloidal structure is strongly indicative of a field-aligned helical response
- Modeling agrees qualitatively with poloidal structure of response
- Radial localization indicates driven peeling-ballooning response

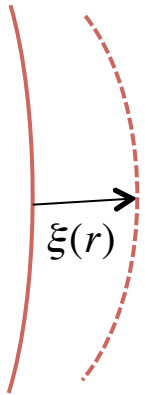
Preliminary Results Show ~1 cm Midplane Displacements for ITER



- **Midplane edge displacements are found to be ~1/2 cm in $Q_{DT}=10$ scenarios with 45 kAt in the center row**
 - Only center row considered (found to have strongest coupling)
 - ITER $Q_{DT}=10$ scenarios have ~10 cm outer gap

Linear Results Appear to be Valid In These Cases

- “Displacement” may be defined by movement of isotherms



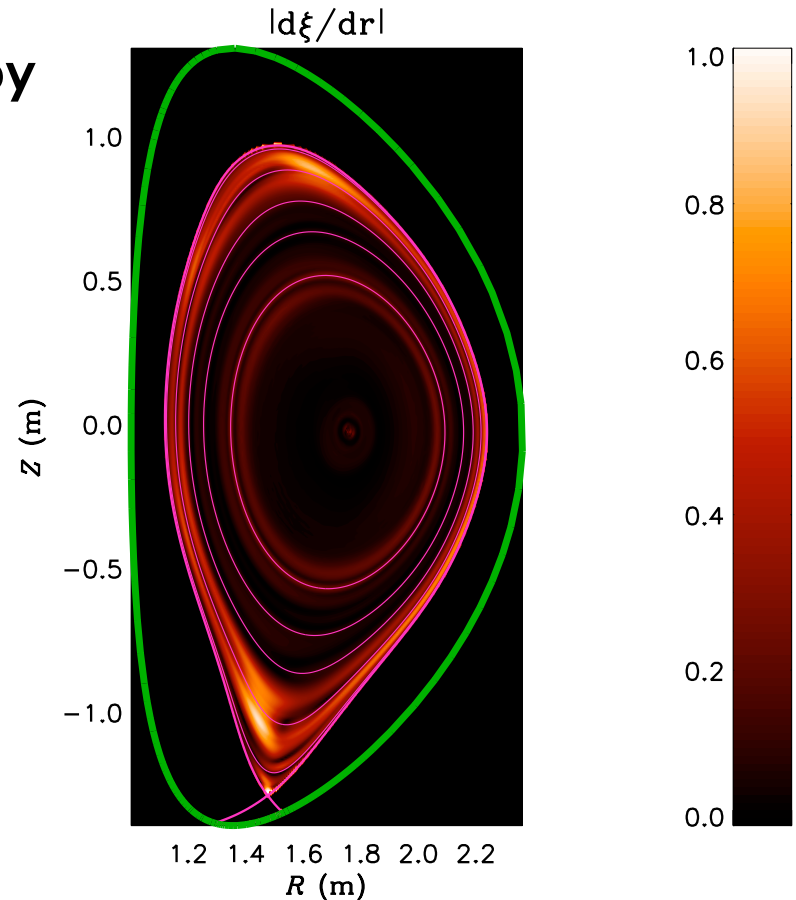
$$T_0(r + \xi) + \delta T(r + \xi) = T_0(r)$$

$$\left[T_0(r) + \frac{dT_0}{dr} \xi \right] + \delta T(r) = T_0(r)$$

$$\xi = -\frac{\delta T}{dT_0/dr}$$

- Overlap of adjacent surfaces is possible, especially near mode-rational surfaces, edge, & x-point

Overlap criterion: $\left| \frac{d\xi}{dr} \right| > 1$



DIII-D 117327 $n=1$

Summary

- **Plasma response calculations yield good agreement with experimental measurements of edge displacement**
- **Edge displacements are largely helical, not (just) axisymmetric**
 - M3D-C1 response is purely helical, and agrees with experiment
 - X-ray data shows clear helical response
- **Displacements may be strongly enhanced by plasma response (*i.e.* stable mode driven to finite amplitude)**
- **This tool will help us extrapolate to ITER with some confidence**