

# Measurement of Cross-Phase Angle Between Turbulent $\tilde{n}$ and $\tilde{T}_e$ and Comparison with Nonlinear GYRO Predictions

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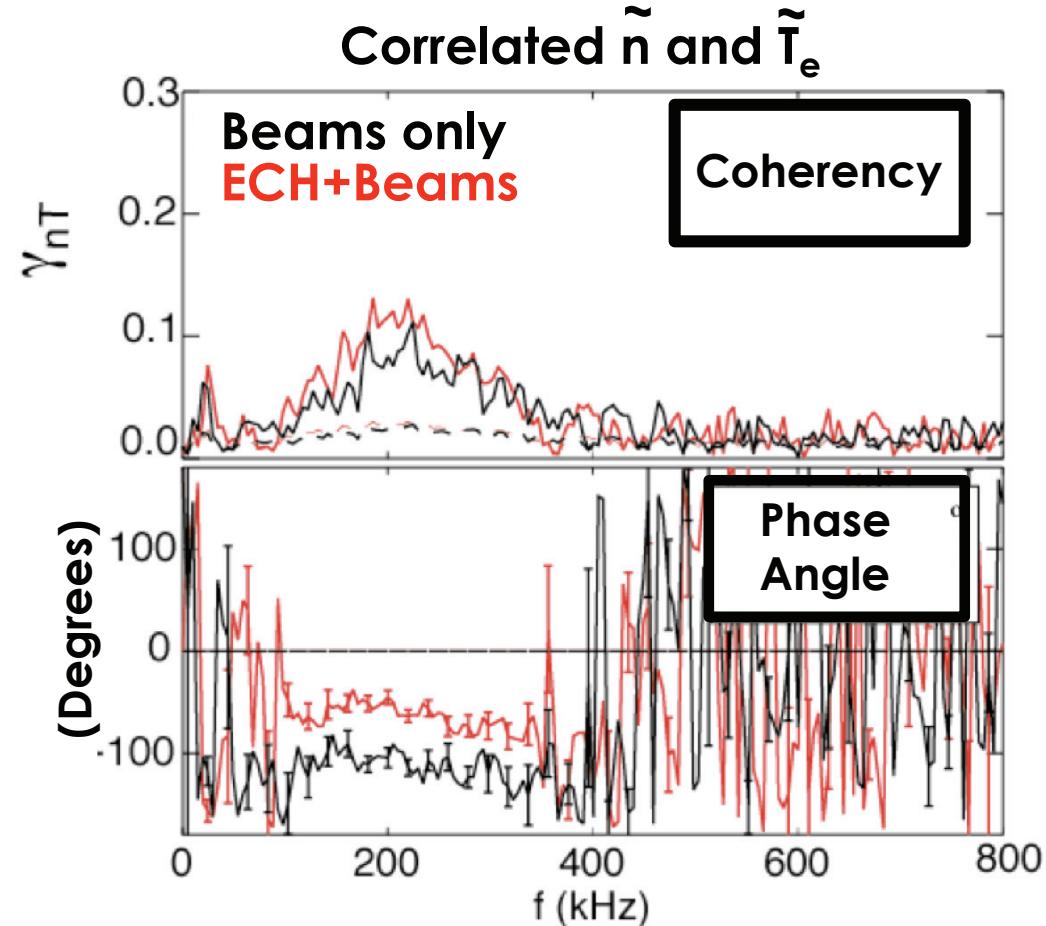
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51<sup>st</sup> Annual APS-DPP Division of Plasma Physics  
Atlanta, GA November 2-6 2009



# $\tilde{n}_e$ - $\tilde{T}_e$ Cross-Phase Angle has been Measured and is in Good Agreement with Nonlinear Gyrokinetic Simulations

- Nonlinear GYRO simulations used to design experiments, study changes in cross-phase angle between  $\tilde{n}_e$  and  $\tilde{T}_e$
- $\tilde{n}_e$ - $\tilde{T}_e$  cross-phase angle has been measured successfully using combined Correlation Electron Cyclotron Emission (CECE) and Reflectometry Diagnostics
- Density and electron temperature fluctuations are out of phase, But become more in phase as temperature is increased
- GYRO is used to model experimental discharges to qualitatively and quantitatively compare with trend in  $\tilde{n}_e$ - $\tilde{T}_e$  cross-phase angle

# Outline

- $\tilde{n}_e$ - $\tilde{T}_e$  cross-phase angle in theory and simulations
- $\tilde{n}_e$ - $\tilde{T}_e$  cross-phase angle via Reflectometry and CECE
- Experimental Results
- Comparison with local, nonlinear GYRO simulations
- Conclusions and Future Work

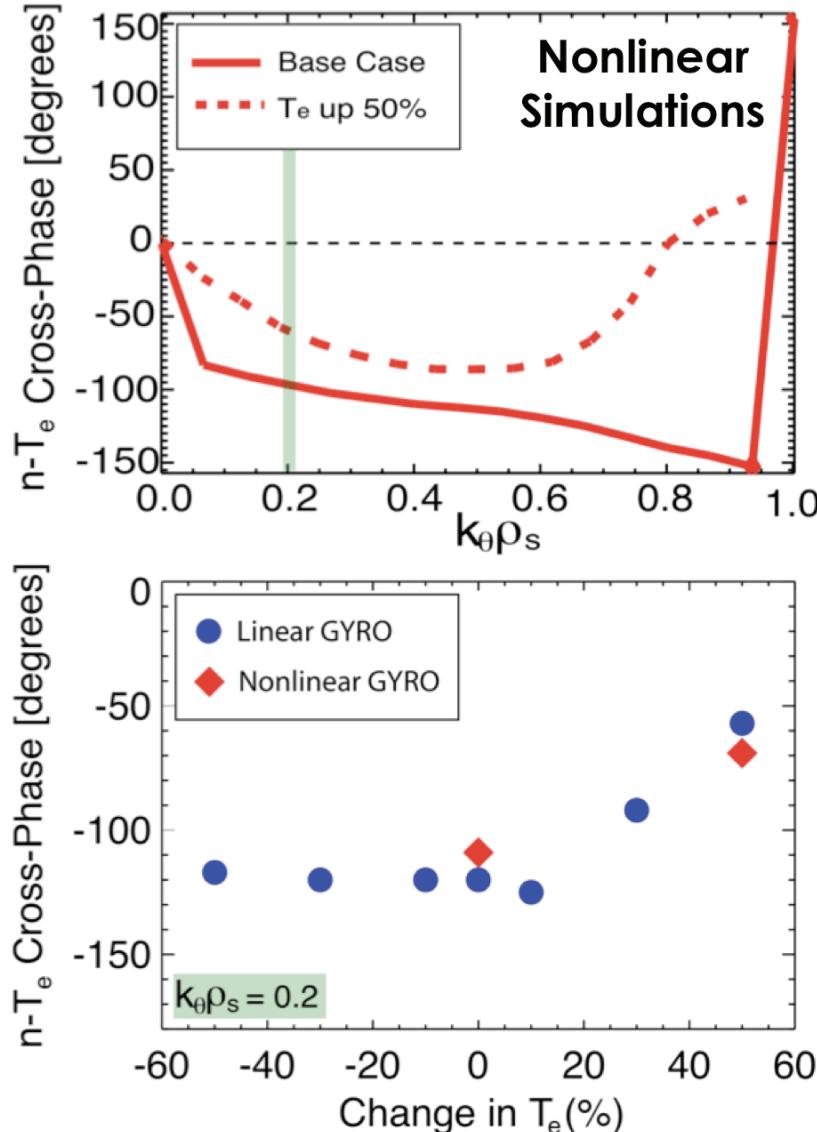
# Cross-Phase Angle is Important for Understanding Physics of Turbulence-Driven Transport

- Turbulence-driven transport is believed to be well-described by models of drift-wave instabilities
- Direct comparisons between experiment and nonlinear turbulence simulations are possible
- Electrostatic electron energy flux expression expanded to show dependence on cross-phase angles and fluctuation levels

$$Q^{ES} = \frac{3}{2B} n_0 T_0 k_\theta (\tilde{n}_{rms} \tilde{\phi}_{rms} |\gamma_{n\phi}| \sin(\alpha_{n\phi}) + \tilde{T}_{rms} \tilde{\phi}_{rms} |\gamma_{T\phi}| \sin(\alpha_{T\phi}))$$

- Finite phase differences arise due to dissipation of parallel electron motion collisions and magnetic trapping effects
- Several types of instabilities can contribute to electron thermal transport
  - Ion temperature gradient (ITG) mode ( $k_\theta \rho_s < 1$ ),
  - Trapped electron mode (TEM) ( $k_\theta \rho_s < 2$ )
  - Electron temperature gradient (ETG) mode ( $k_\theta \rho_s > 2$ )

# GYRO: Predict a Change in $\tilde{n}_e$ - $\tilde{T}_e$ Phase Angle Using Nonlinear Simulations of Experimentally Accessible Conditions



- Nonlinear GYRO runs are performed before an experiment to aid in design

## 1) Base case:

Beam heated L-Mode DIII-D plasma parameters,  
**ITG-dominant**

## 2) High $T_e$ case:

L-mode plasma with 50% increase in  $T_e$  ( $a/L_{T_e}$  fixed);  
**electron mode drive increases at low-k**

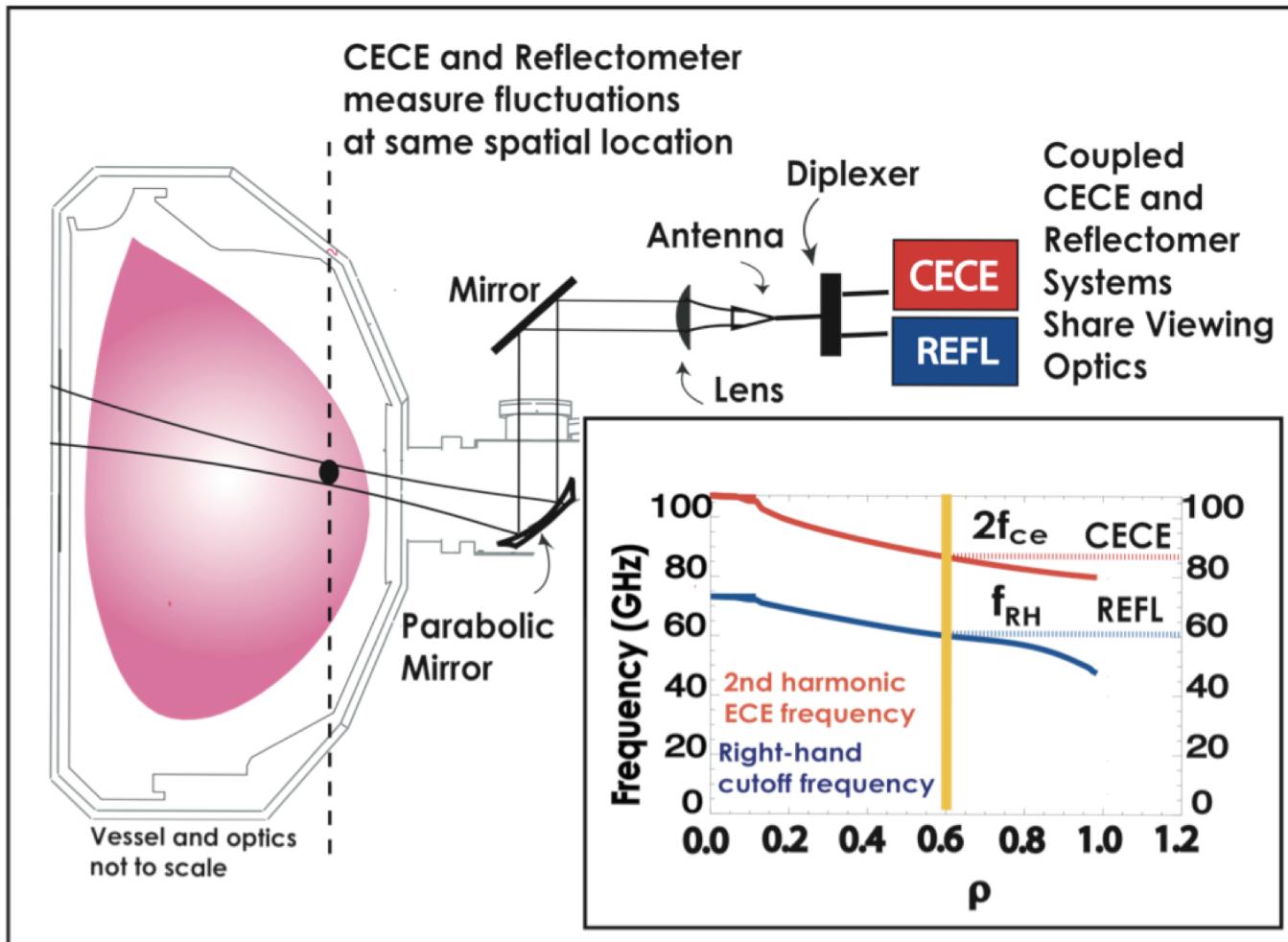
- Qualitatively compare predicted trend with experiment

- Perform post-experiment GYRO simulations to quantitatively compare with experiment

# Outline

- $\tilde{n}$ - $\tilde{T}$  cross-phase angle in theory and simulations
- $\tilde{n}_e$ - $\tilde{T}_e$  cross-phase angle via Reflectometry and CECE
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# Coupled Correlation Electron Cyclotron Emission (CECE) and Reflectometry for Cross-Phase Angle Measurement



## X-mode Correlation ECE radiometer

- Low- $k$   $\tilde{T}_e$  ( $k_\theta \rho_s < 0.3$ )

## • Spot-Size

$$\Delta z \sim 3.2 \text{ cm}$$

$$\Delta r \sim 1.0 \text{ cm}$$

## X-Mode quadrature Reflectometer

- Low- $k$   $\tilde{n}_e$  ( $k_\theta \rho_s < 0.5$ )

## • Spot-size

$$\Delta z \sim 3.5 \text{ cm}$$

$$\Delta r \sim 1.0 \text{ cm}$$

$\rho_s = 2\text{-}3 \text{ mm}$  in plasmas of interest

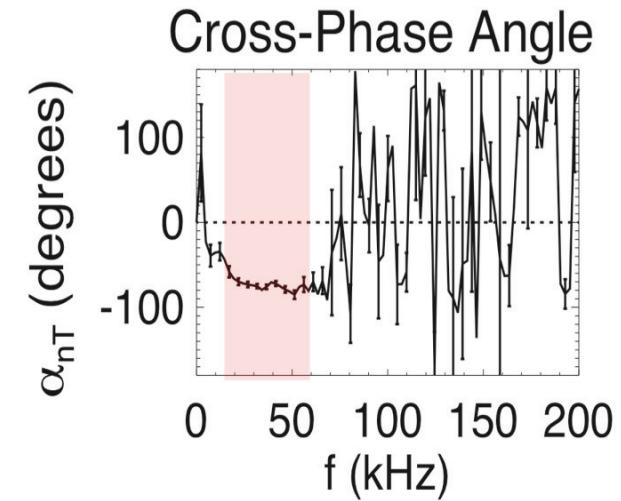
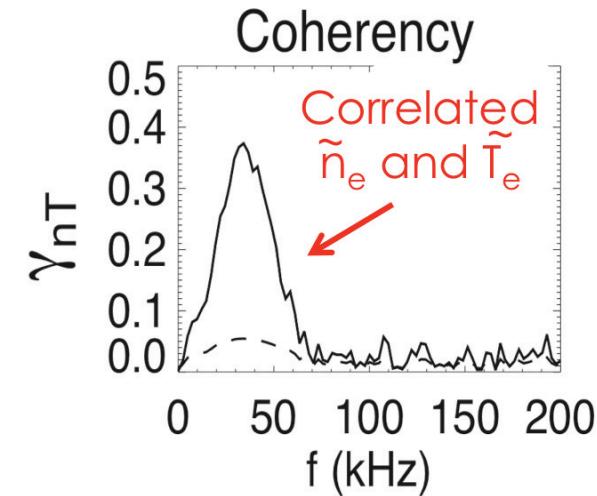
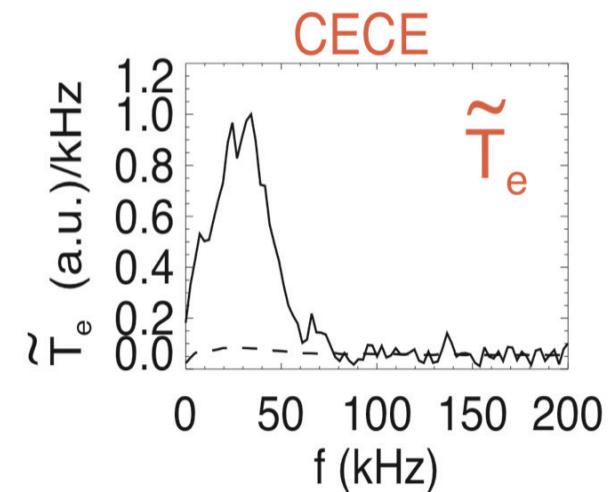
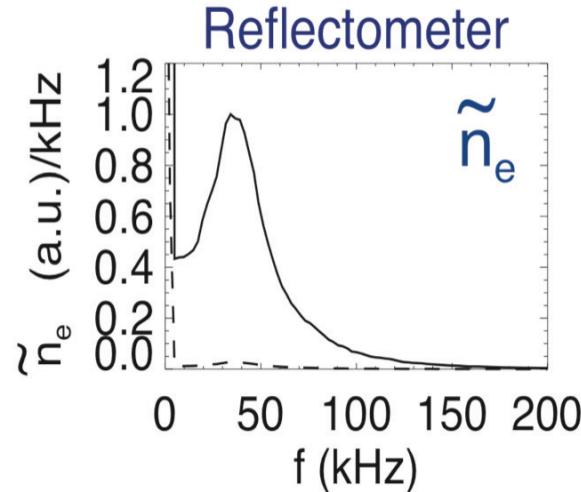
# Coupled CECE and Reflectometry: Standard Spectral Correlation Analysis is Used to Measure $\alpha_{nT}$

- Example of correlated  $\tilde{n}$  and  $\tilde{T}_e$  in core,  $\rho = 0.6$
- Shot 133626, Ohmic heating and ECH (no beams)
- Turbulence data averaged  $t = 1600-1900$  ms

$$G_{nT} = \langle S_{\text{REFL}}^* S_{\text{ECE}} \rangle$$

$$\alpha_{nT} = \arctan(Im(G_{nT}) / Re(G_{nT}))$$

- Density fluctuation signal is taken as reference



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# $n_e$ - $T_e$ Cross-Phase Angle Measured During Sawtooth Free, Quasi-Stationary L-Mode Plasmas

Compare predicted change in phase angle with experiments

- **Base Case (NBI only)**

- $I_p = 1$  MA,  $B_T = 2.0$  T
- upper single null
- Early 2.5 MW co-injected NBI

- **High  $T_e$  Case (NBI + ECH)**

- Add 2.4 MW ECH at  $\rho = 0.4$

Many turbulence diagnostics deployed:

$\tilde{n}_e$ - $\tilde{T}_e$  Phase Angle

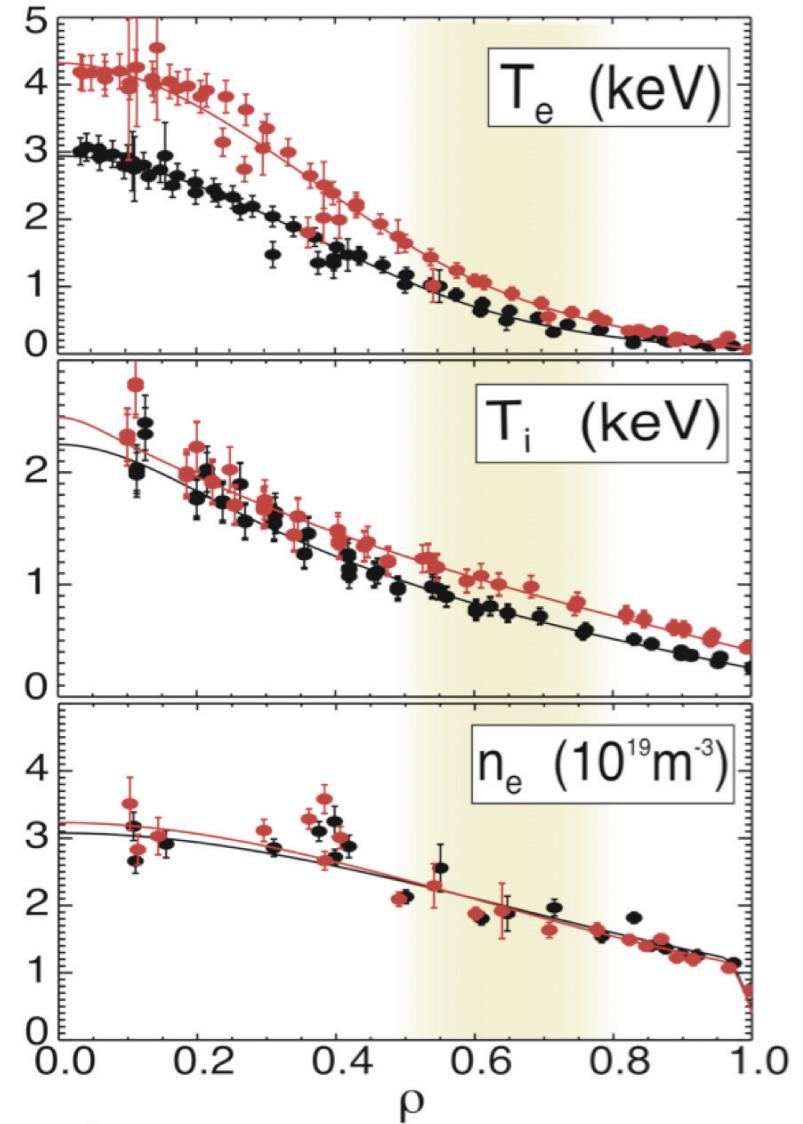
Low- $k$   $\tilde{n}/n$  (BES)

Low- $k$   $\tilde{T}_e/T_e$  (CECE)

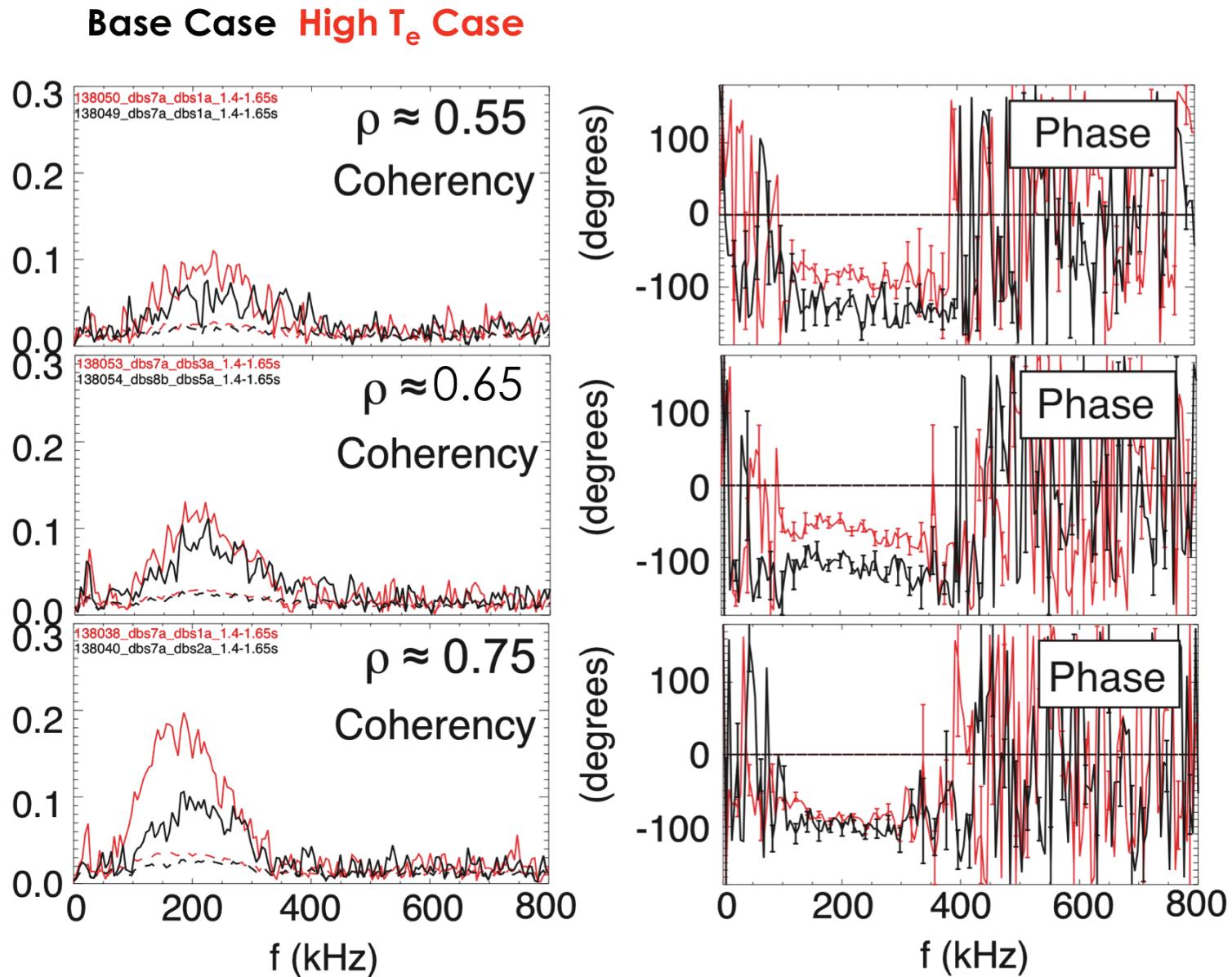
Intermediate- $k$   $\tilde{n}$  (Doppler Backscattering)

High- $k$   $\tilde{n}$  (Backscattering)

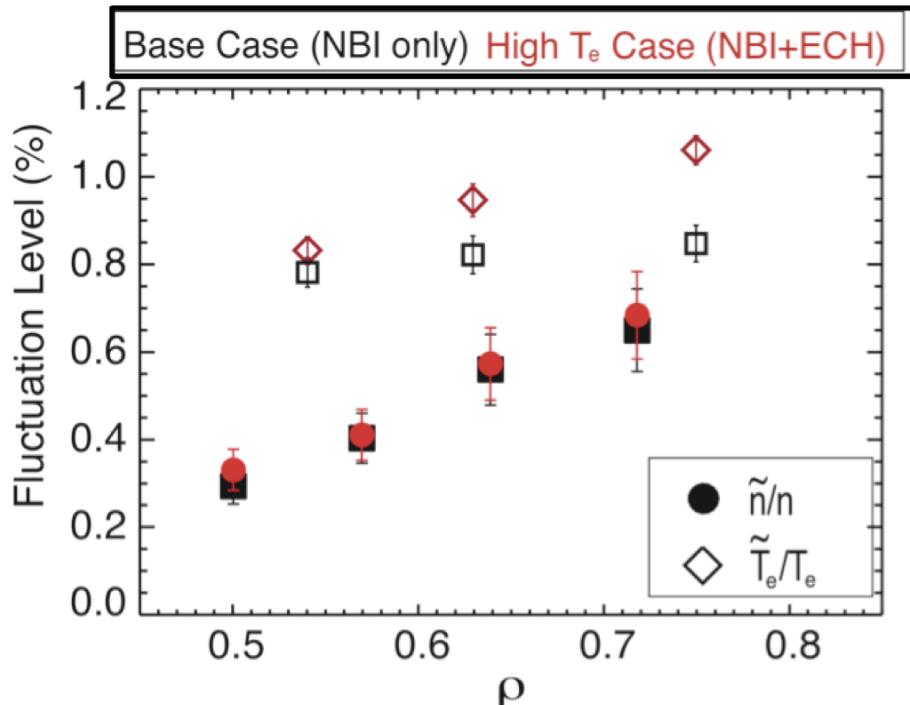
Turbulence measured  
 $0.5 < \rho < 0.8$



# Predicted Trend is Observed at $\rho = 0.55$ and $0.65$ but not At $\rho = 0.75$ in the High $T_e$ Case



# Turbulence Across Wide Range of ITG/TEM/ETG Scales – Largest Changes seen in low-k $\tilde{T}_e/T_e$ and Phase Angle



## Measured Changes in High-k (ETG scale) Turbulence

- Backscattering:

Increase in high-k  $\tilde{n}$  of 6%

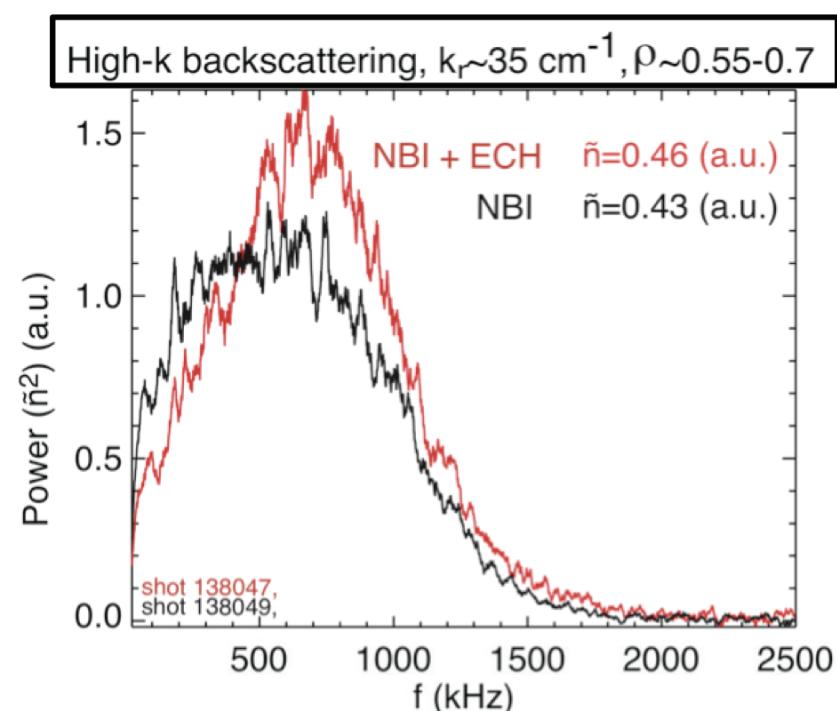
## Measured Changes in Low-k (ITG/TEM scale) Turbulence

- CECE:

Increase in low-k  $\tilde{T}_e/T_e$  of 10-30%

- BES:

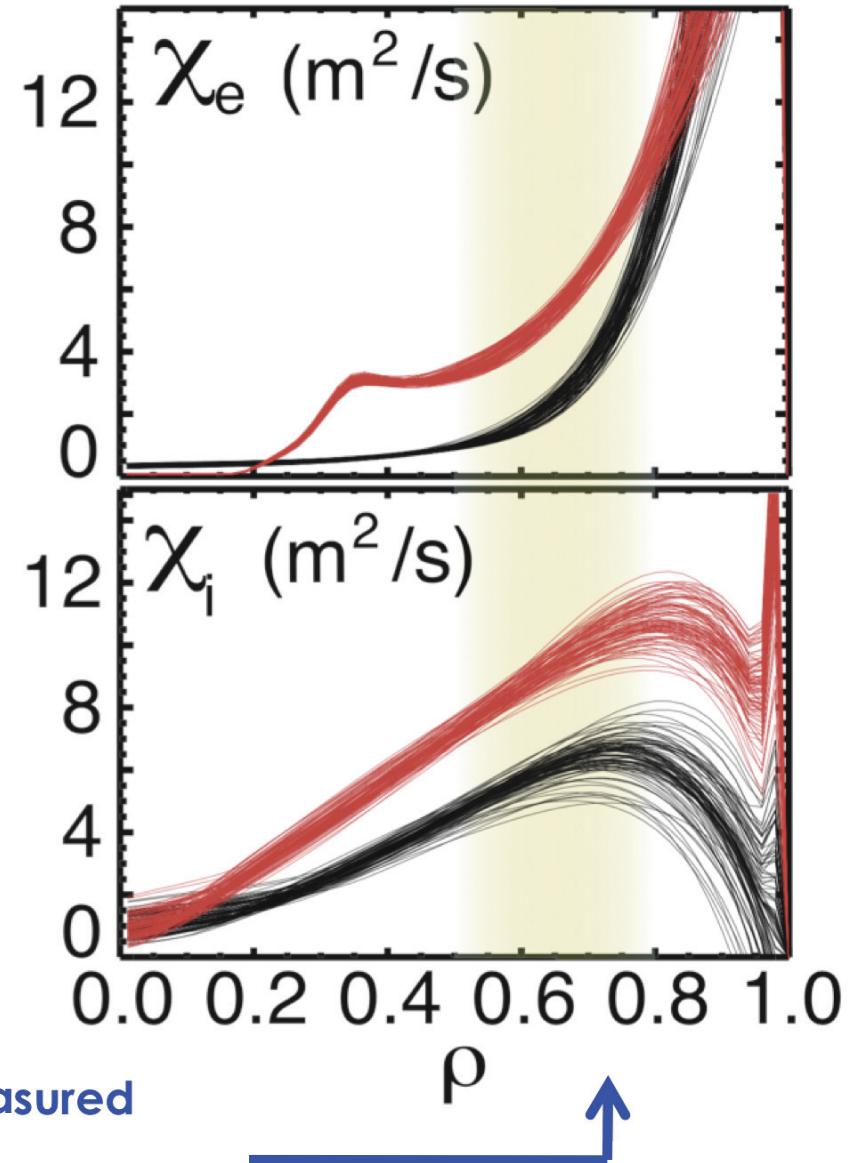
Increase in low-k  $\tilde{n}/n$  of 5-10%



# Increase in Transport and Linear Growth Rate Observed in High $T_e$ case

- With ECH:
  - ONTEWO: Transport increases
  - Uncertainty is estimated using a Monte-Carlo Analysis
  - Electron mode linear growth rate Increases
  - ITG mode growth rate decreases
  - Growth rate of most unstable mode increases

Turbulence measured  
 $0.5 < \rho < 0.8$



# Increase in Transport and Linear Growth Rate Observed in High $T_e$ case

- With ECH:

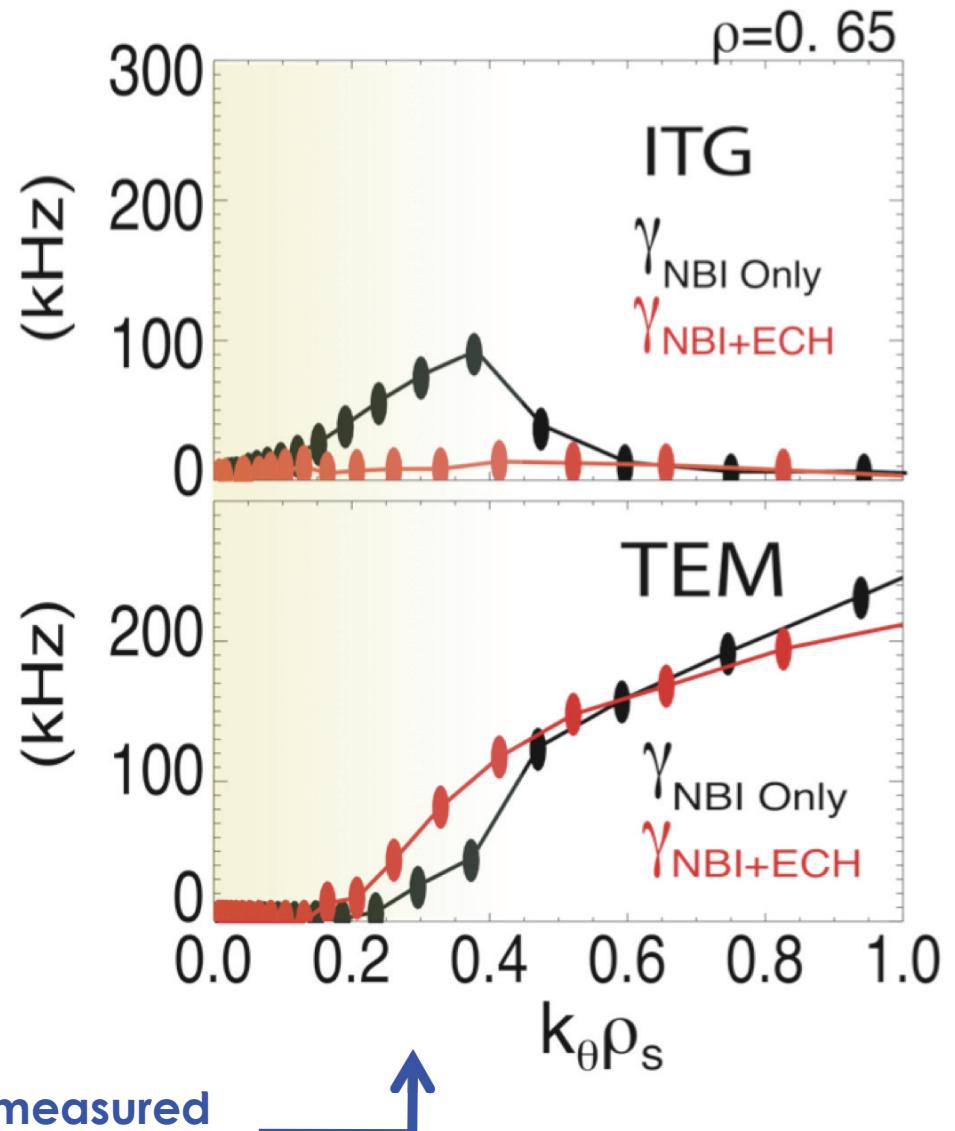
- Transport increases
- Uncertainty is estimated using a Monte-Carlo Analysis

- TGLF:  
**Electron mode linear growth rate Increases**

**ITG mode growth rate decreases**

**Growth rate of most unstable mode increases**

Phase Angle measured at Low-k



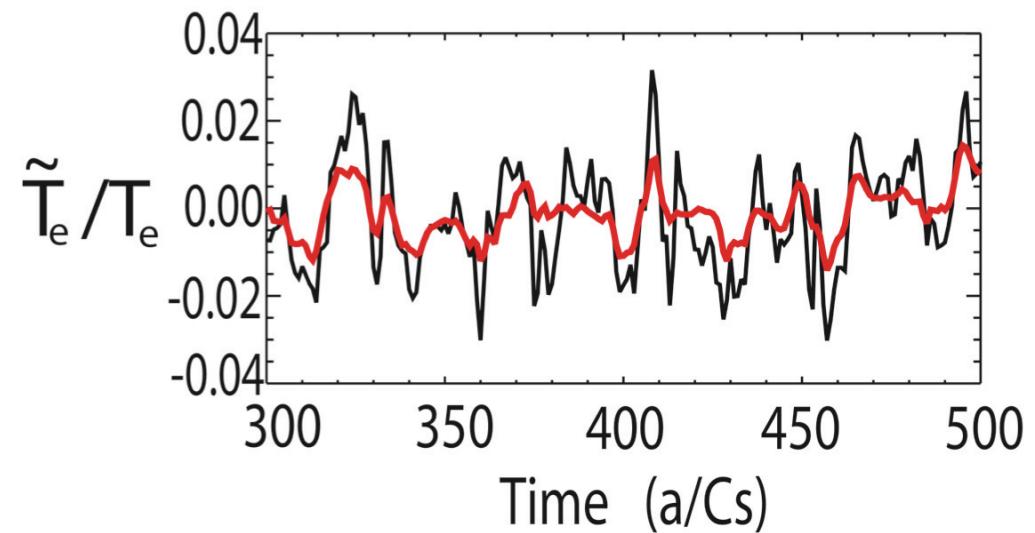
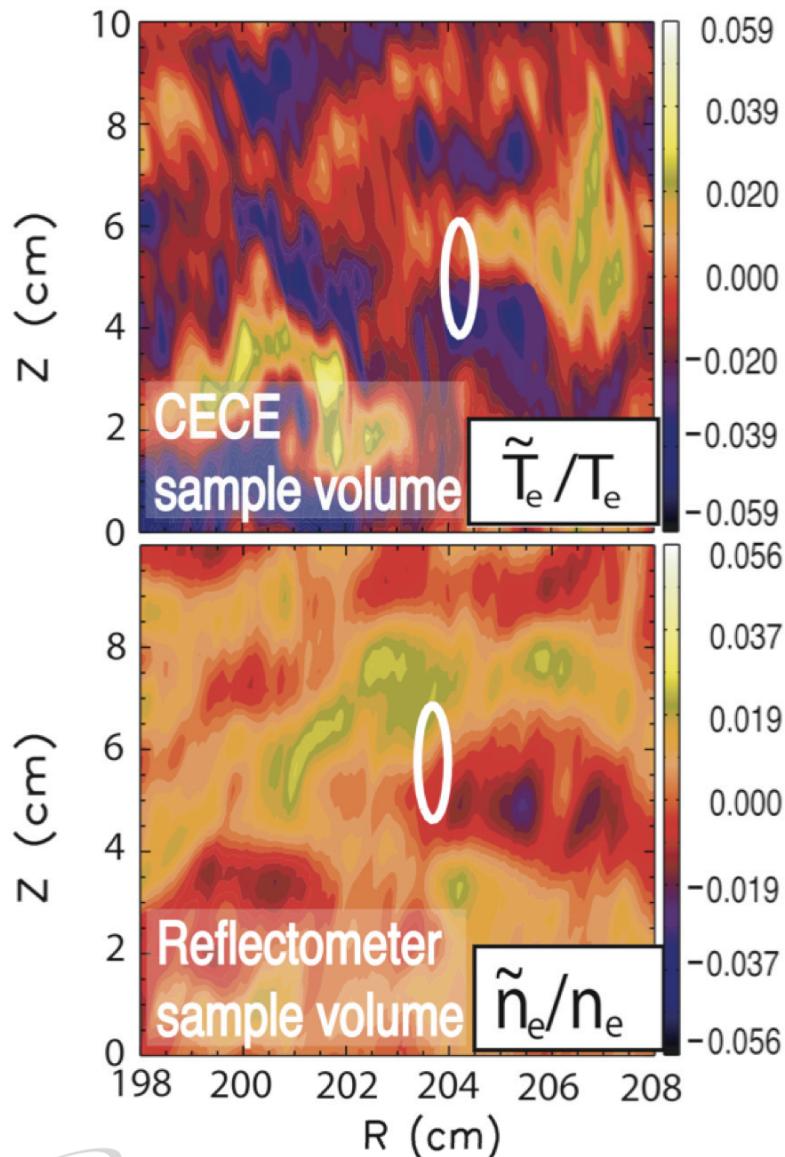
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# Compare Measured $\tilde{n}_e$ - $\tilde{T}_e$ cross-phase angle With Results From Local, Nonlinear GYRO Simulations

- GYRO is an initial value, Eulerian (Continuum) 5-D gyrokinetic transport code [Candy and Waltz PRL 91, 045001 (2003)]
- Local simulations include real geometry, drift-kinetic electrons, e-i pitch-angle collisions,  $(M_i/m_e)^{1/2} = 40$ , electromagnetic effects, dynamic Carbon ions and equilibrium ExB flow
- Take experimental profiles ( $T_e$ ,  $T_i$ ,  $n_e$ ,  $E_r$ ) as input
  - Need quantitative comparisons (post-experiment) in addition to qualitative trend comparisons (pre-experiment)
  - Difficult to obtain convergence for Base Case (138040)
  - **High  $T_e$  Case Simulation has been completed (138038)**

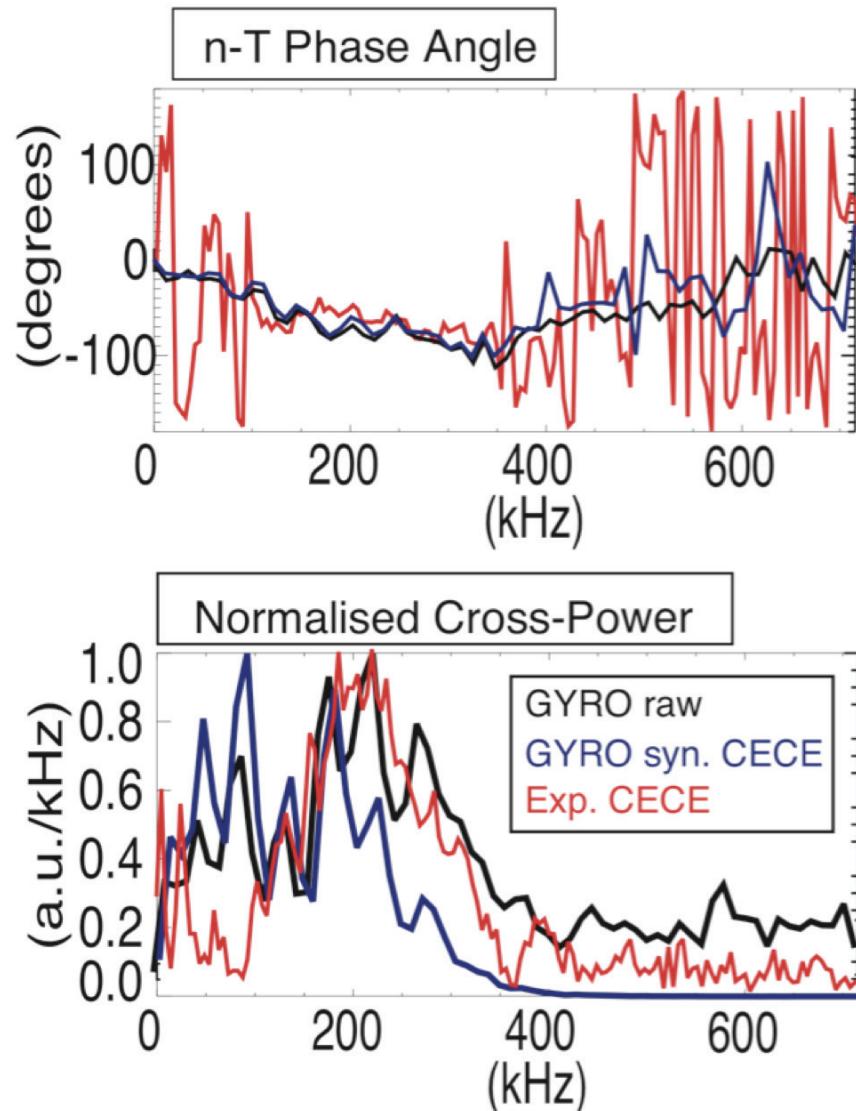
# Synthetic Diagnostics Used to Compare with Cross-Phase Angle and Two-Field Fluctuation Level Measurements



- Spatial Filter in synthetic diagnostics models sample volume size
- Fluctuation levels and spectral shape depend on details synthetic sample volume

[Holland, POP, 2009]

# In Contrast to Fluctuation Levels and Spectra, the Cross-Phase Angle Is Found to Be Insensitive to Sample Volume Size



## • Nonlinear GYRO results

- Local Simulation at  $\rho = 0.65$
- Exp. High  $T_e$  Case, #138038

**GYRO raw Phase =  $-70^\circ \pm 2^\circ$**

**GYRO syn. Phase =  $-71^\circ \pm 1^\circ$**

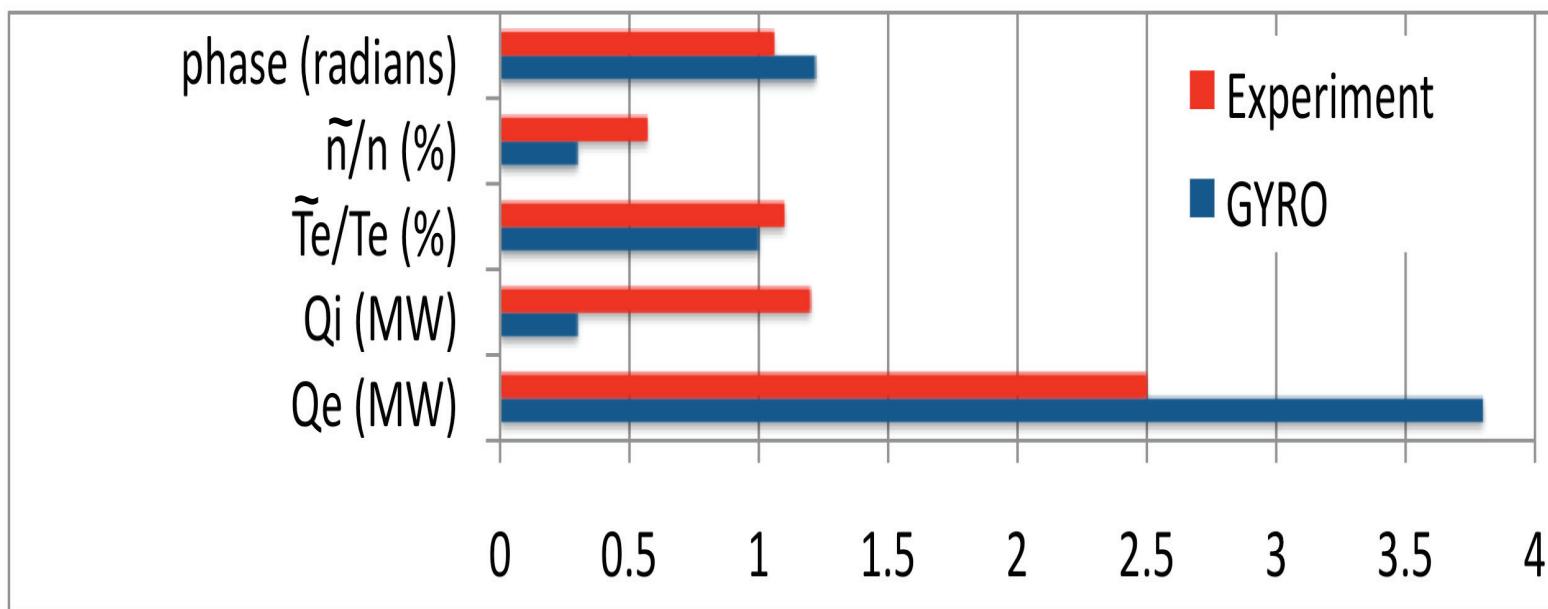
**Exp. n-T phase =  $-61^\circ \pm 12^\circ$**

• Synthetic spot-size has little effect on n-T cross-phase

• Higher frequencies in n-T cross-power spectrum are filtered by sample volume size

# New Experiment Quantitatively Tests GYRO at Multiple Levels

- Nonlinear GYRO results (post-experiment)
  - Local Simulation at  $\rho = 0.65$
  - Exp. High  $T_e$  Case, #138038
- Quantitative comparisons between phase angle, fluctuation levels and power flows are performed
  - Measured Phase Angle is in good agreement with GYRO results



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- Preliminary quantitative agreement between measured  $\alpha_{nT}$  and GYRO in the High  $T_e$  Case is very good, but Base Case simulation not yet completed

# Ongoing Work at DIII-D Focuses on Multi-Field Multi-Scale Fluctuation Measurements for Rigourous Code Comparisons

- **University of Wisconsin:** Measurements of  $\tilde{T}_i$  will provide important new constraint on models of ITG transport  
**(I.U. UzunKaymak – Poster JP8.00116)**
- **UCLA:** Multi-channel Intermediate-k Doppler Backscattering for GAM/Zonal Flow studies **(J. C. Hillesheim – Contributed Oral CO4.00008)**
- **UCSD:** Kappa Dependence of Transport and Turbulence  
**(Holland –Poster TP8.00012 )**
- **GA:**  $a/L_T$  Turbulence Drive Modification and Multi-field, Multi-Scale Turbulence Response **(DeBoo-Invited Talk KI3.00003)**
- **GA Theory :** Gyrokinetic transport solver TGYRO used to predict kinetic plasma profiles consistent with energy and particle fluxes in the DIII-D tokamak **(J. Candy - Invited Talk DI3.00002 )**

*Simultaneous measurements of multiple fluctuating fields improve understanding of turbulence and transport, provide the opportunity for challenging comparisons with nonlinear gyrokinetic simulations*

# Ongoing work with Quantitative GYRO comparisons: Complete Simulations for the Base Case and High $T_e$ Case

- Only High  $T_e$  Case has been simulated, Base Case is difficult
  - Sensitivity scans/reduced models do not recover low-k turbulence
  - Do not achieve convergence, even including  $k_\theta \rho_s < 3$
  - Impact of high-k on transport using ITG/TEM – ETG runs

- Use TGYRO (TGLF+NEO) power matching profiles as input

**Self-consistently captures effects of sensitivity to input profiles  
when gradients are near threshold**

[See Candy Invited Talk, this conference]

