

# Excitation of Alfvén Waves By Low Velocity Supra Thermal Ions in the DIII-D and JET Tokamaks

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in collaboration with

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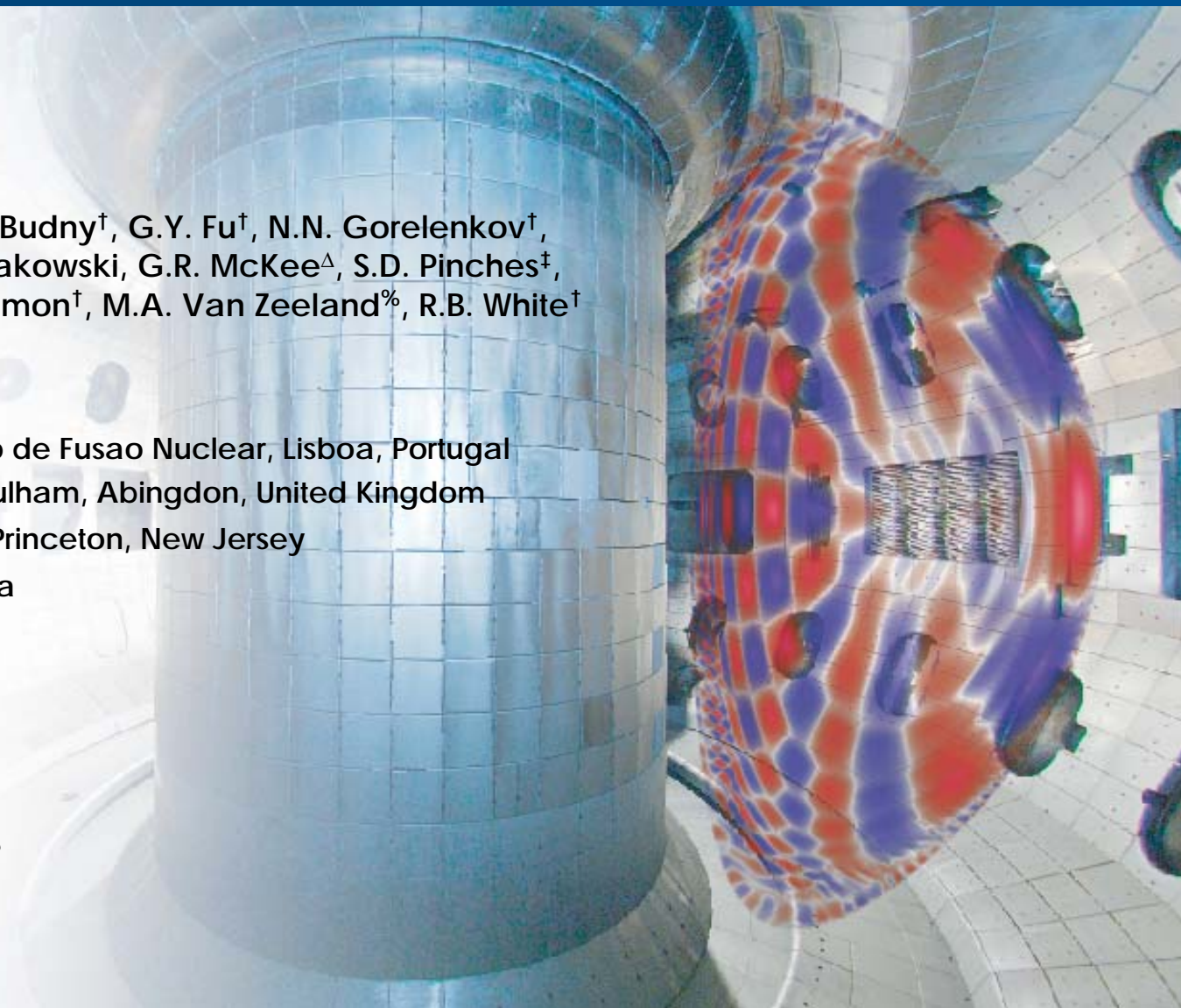
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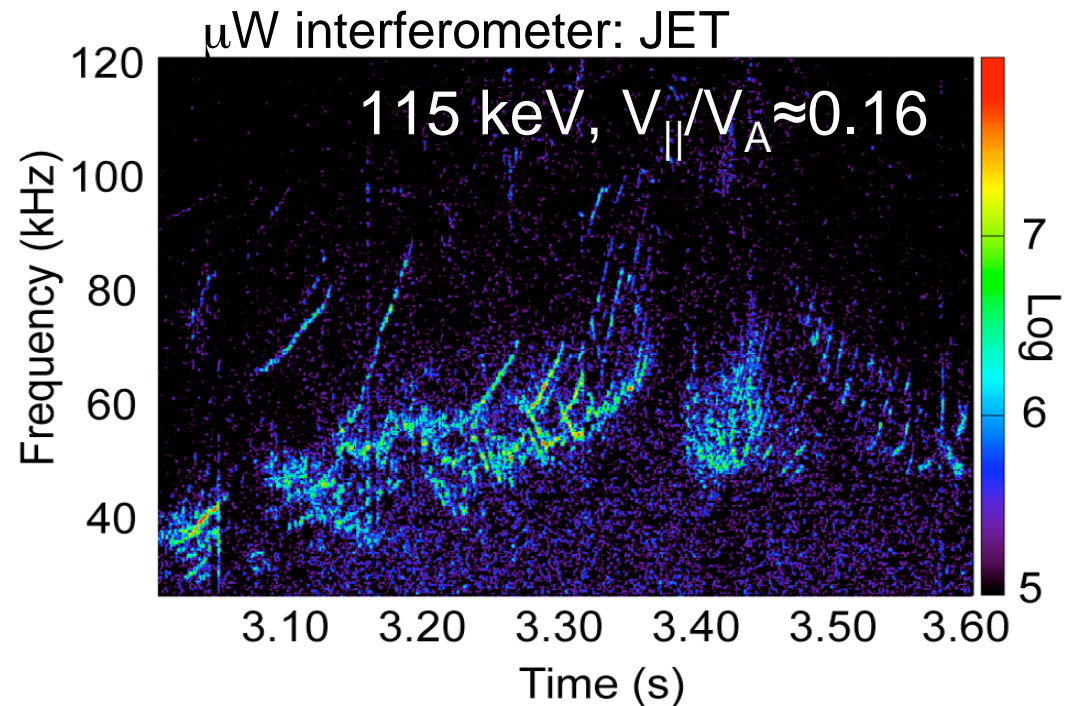
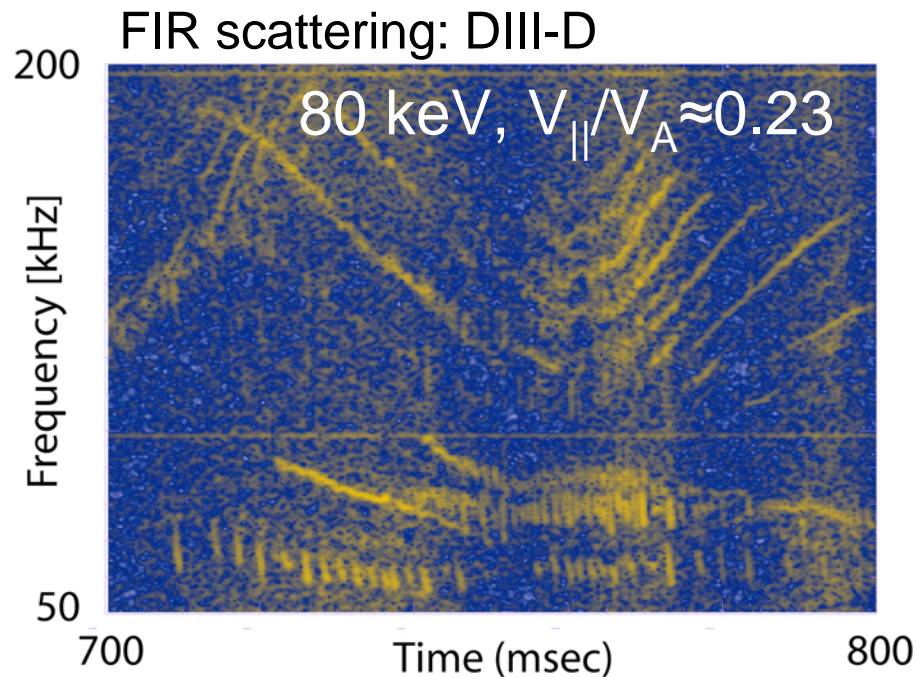
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# Recent Surprise : Rich Spectrum of Alfvén Waves Excited by Low Velocity Supra Thermal Ions in Fusion Plasmas



- Excitation of Alfvén waves previously explored for  $V_{\parallel} \sim V_A$ 
  - Requires high ion energies ( $> 1$  MeV) or low  $V_A$  (low - B)
- However, many Alfvén waves now seen for  $V_{\parallel}$  well below  $V_A$
- Rapid progress made in mode identification
  - the challenge is to understand the excitation mechanism

# Fundamental Resonance Condition Cannot Explain Many Alfvén Waves Driven by Low Energy Ions

- Shear Alfvén wave

$$\omega \approx k_{\parallel} V_A$$

- common varieties

**RSAE** : single  $m$

**TAE** : couples  $m, m+1$

**EAE** : couples  $m, m+2$

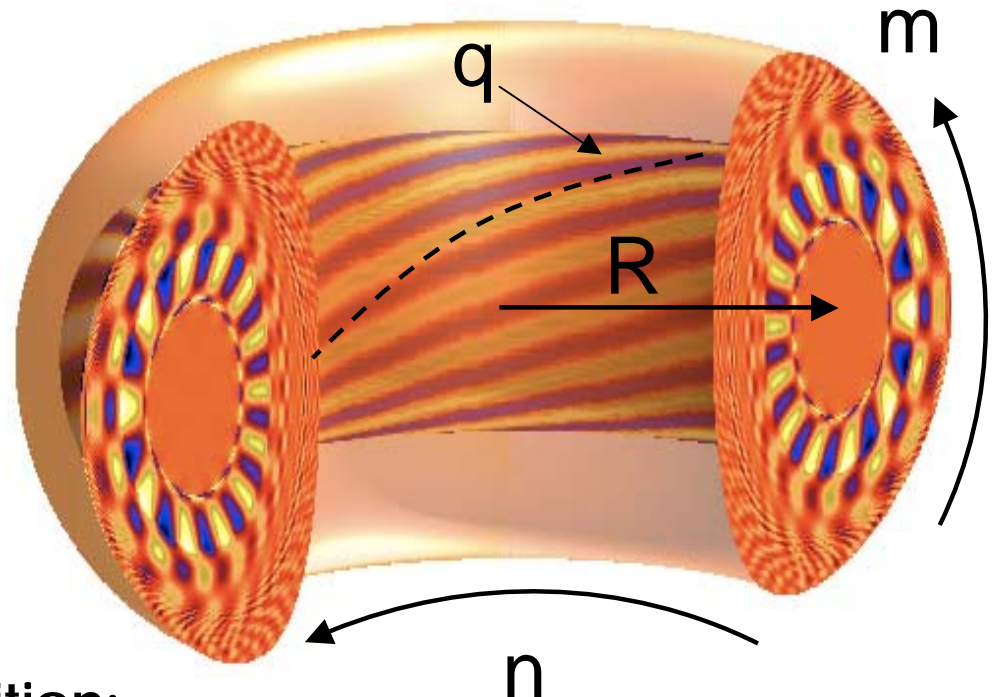
- Fundamental resonance condition:

$$\omega_{\text{MHD}} \approx (k_{\parallel} \pm 1/qR) V_{\parallel} ; V_{\parallel} = 0.23 V_A \text{ in DIII-D and } 0.16 V_A \text{ in JET}$$

**RSAE** :  $V_{\parallel} \approx \pm 1/5 V_A$  or  $\pm 1/3 V_A$

**TAE** :  $V_{\parallel} = \pm 1/3 V_A$  or  $\pm V_A$

**EAE** :  $V_{\parallel} = \pm 1/2 V_A$



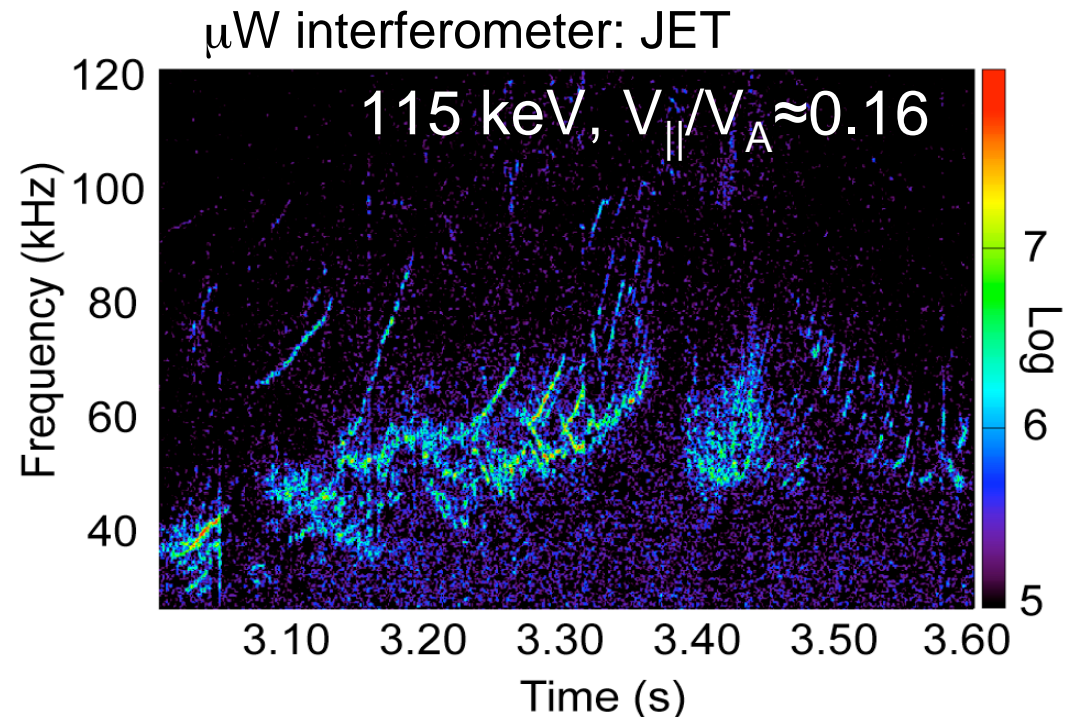
# Excitation can be Explained by Invoking Higher Order Resonances, relevant for Advanced Tokamak Regimes

- Advanced tokamak regimes have high central  $q$ 
  - High  $k_{\perp}$  ( $\approx q n / r$ )
  - High  $\Delta_b$  ( $\approx q \rho_b$ )

Higher order resonances:

$$\omega_{\text{MHD}} \approx (k_{\parallel} \pm p/qR) V_{\parallel}$$
$$p = 2, 3, 4, \dots$$

- Resonant velocity strongly decreases for large  $p$ 
  - $V_{\parallel} \propto V_A/p$
- **Importance:** In high- $q$ , steady state regimes, multiple high order resonances can greatly enhance instability drive and affect fast ion transport



# Outline

- Observation of Alfvén wave excitation below the fundamental resonance condition in DIII-D and JET
- Ideal MHD analysis of radial mode structure, location
- Stability analysis and coupling to high order resonances
- Implications

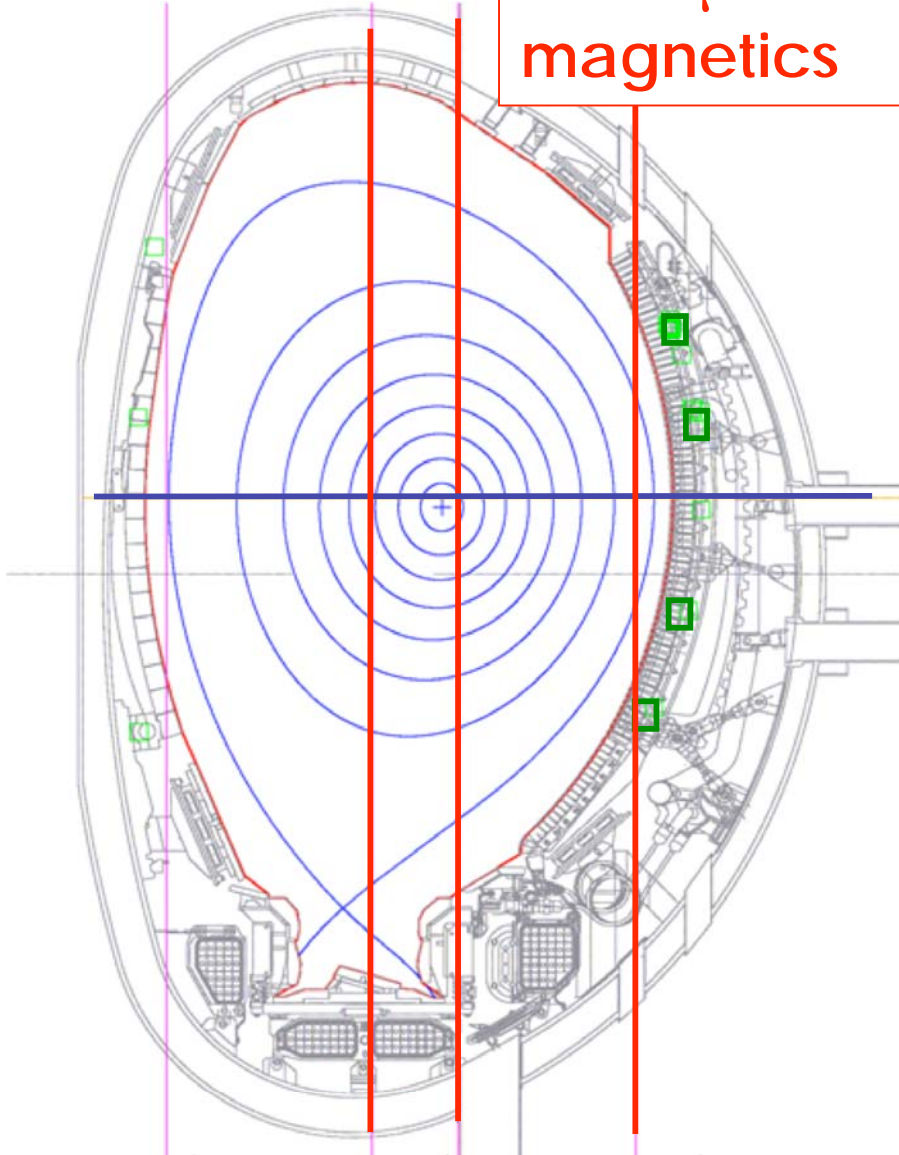
# JET and DIII-D Have Comparable Diagnostics and Complementary Parameters for Alfvén Wave Studies

JET

FIR &  $\mu\text{w}$  Interf. magnetics

$\text{CO}_2$  Interf. magnetics

DIII-D

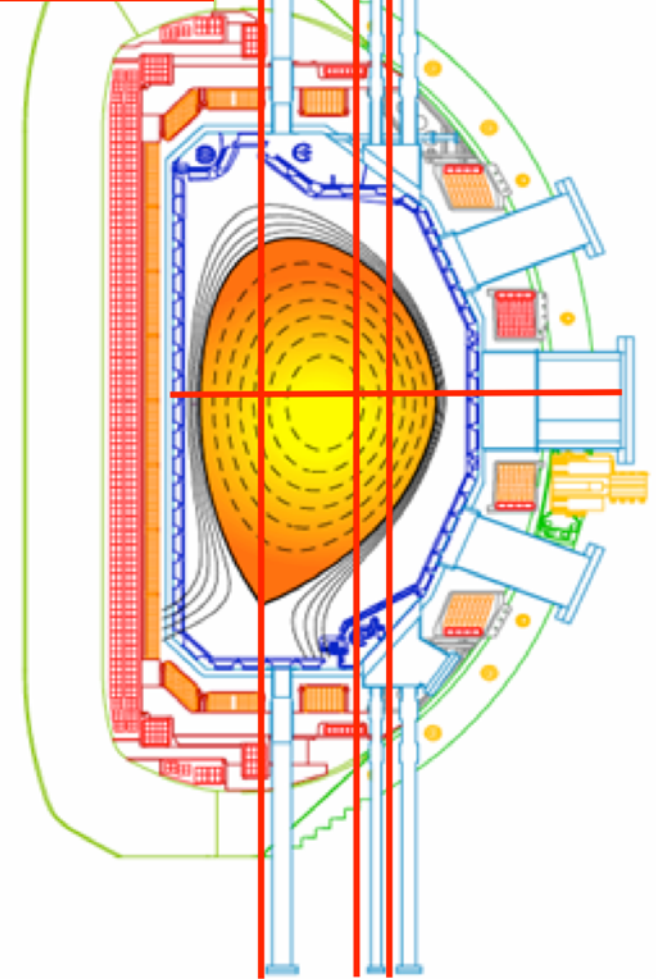


for same  $n, q$

$$\rho^{\text{JET}} = 0.7 \rho^{\text{DIII-D}}$$

$$k_{\perp}^{\text{JET}} = 0.5 k_{\perp}^{\text{DIII-D}}$$

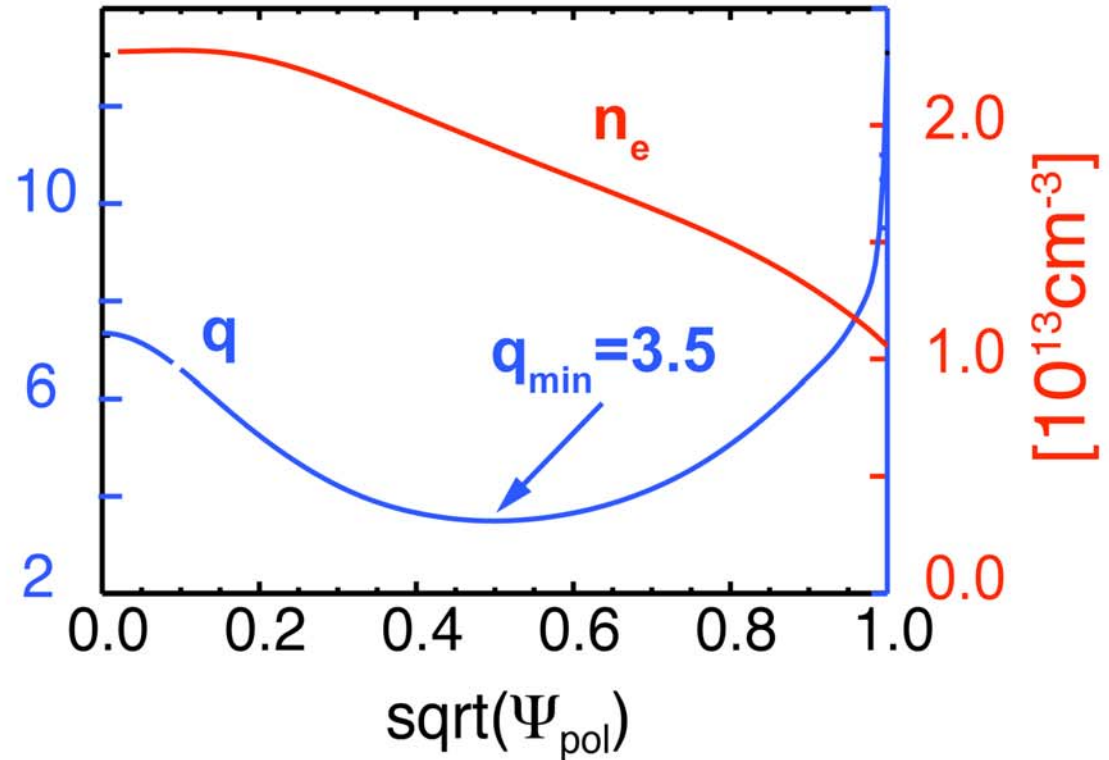
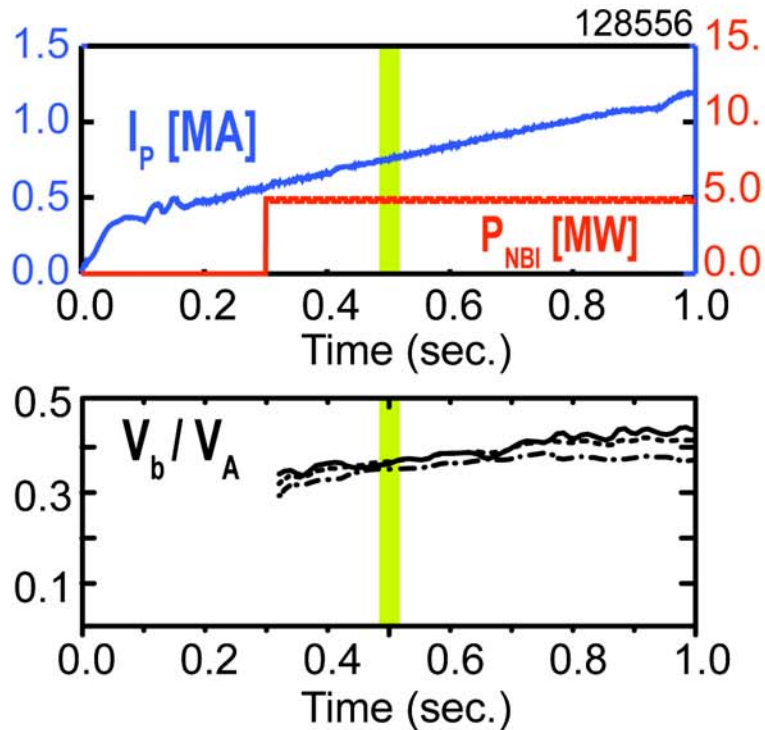
$$V_A^{\text{JET}} \approx 2 \times V_A^{\text{DIII-D}}$$



$E_b \leq 120 \text{ keV}$   $B_T = 3.45 \text{ T}$ ,  $R = 3.0 \text{ m}$

$E_b \leq 80 \text{ keV}$   $B_T = 2.10 \text{ T}$ ,  $R = 1.7 \text{ m}$

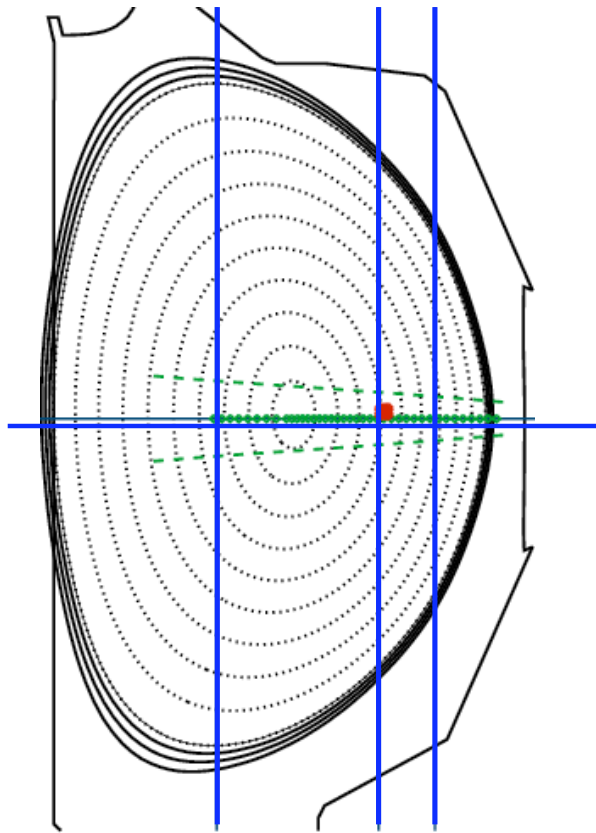
# Experimental Scenario on DIII-D for Alfvén Eigenmode Study in Reverse Magnetic Shear Plasmas



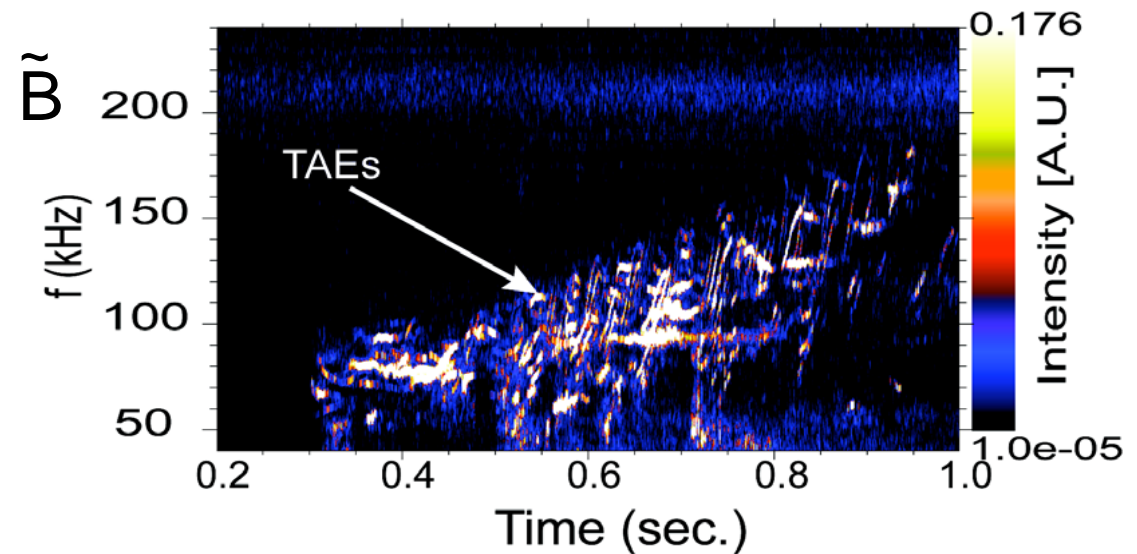
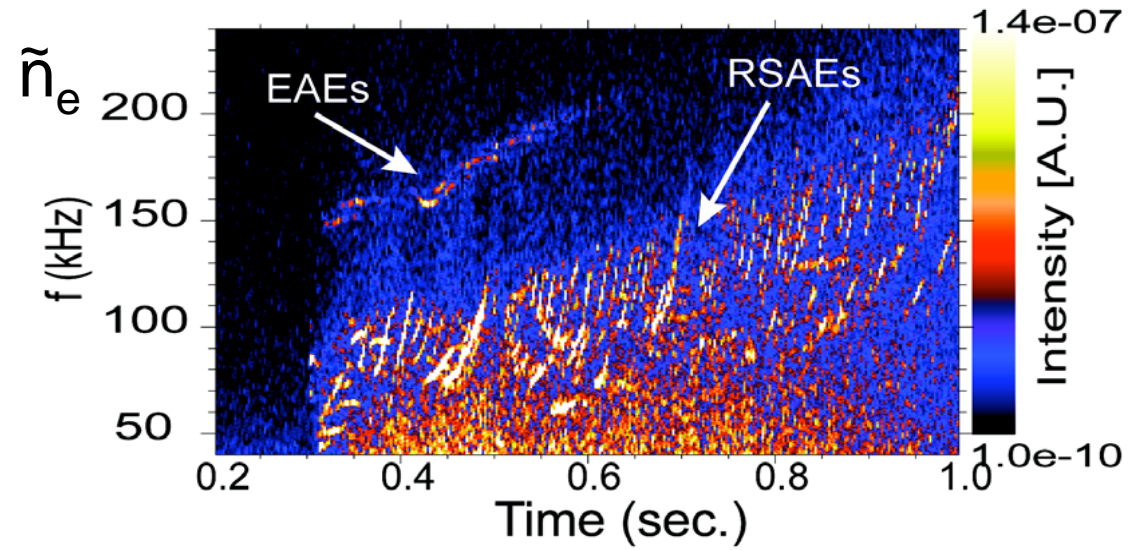
- Early beam heating is used to delay current penetration and create reverse magnetic shear

# DIII-D Measurements in Reverse Magnetic Shear Plasmas Indicate Many Unstable Alfvén Eigenmodes

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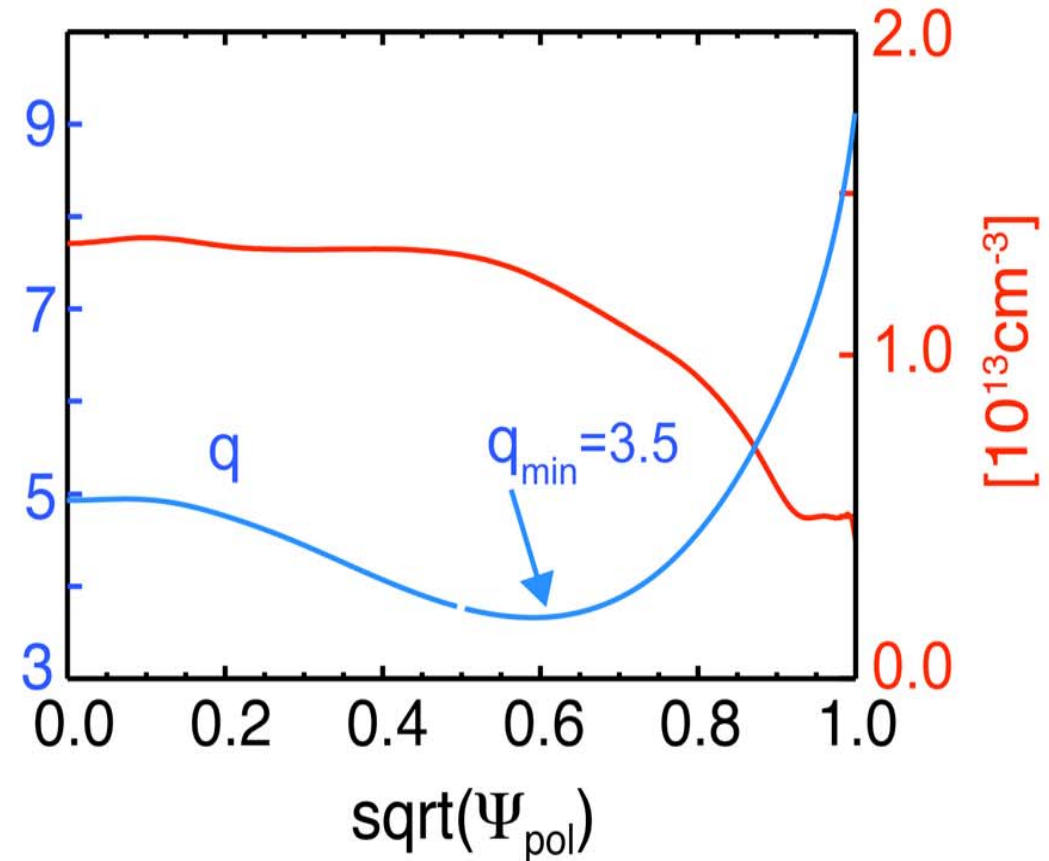
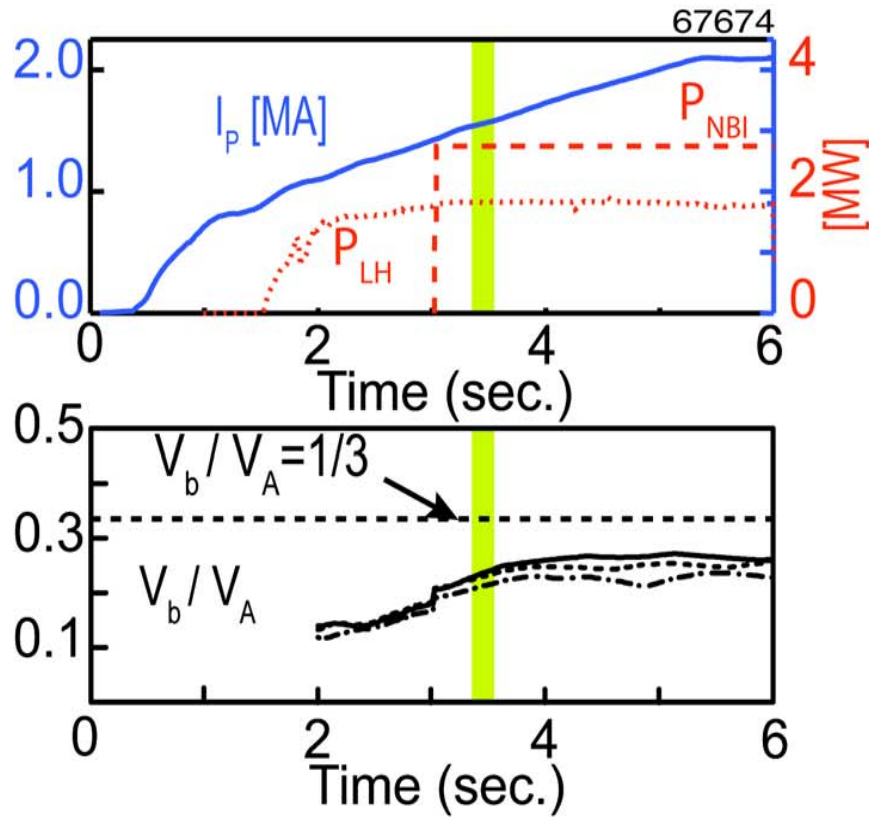


- Difficult to go below  $V_{||} = 0.25$  V in DIII-D



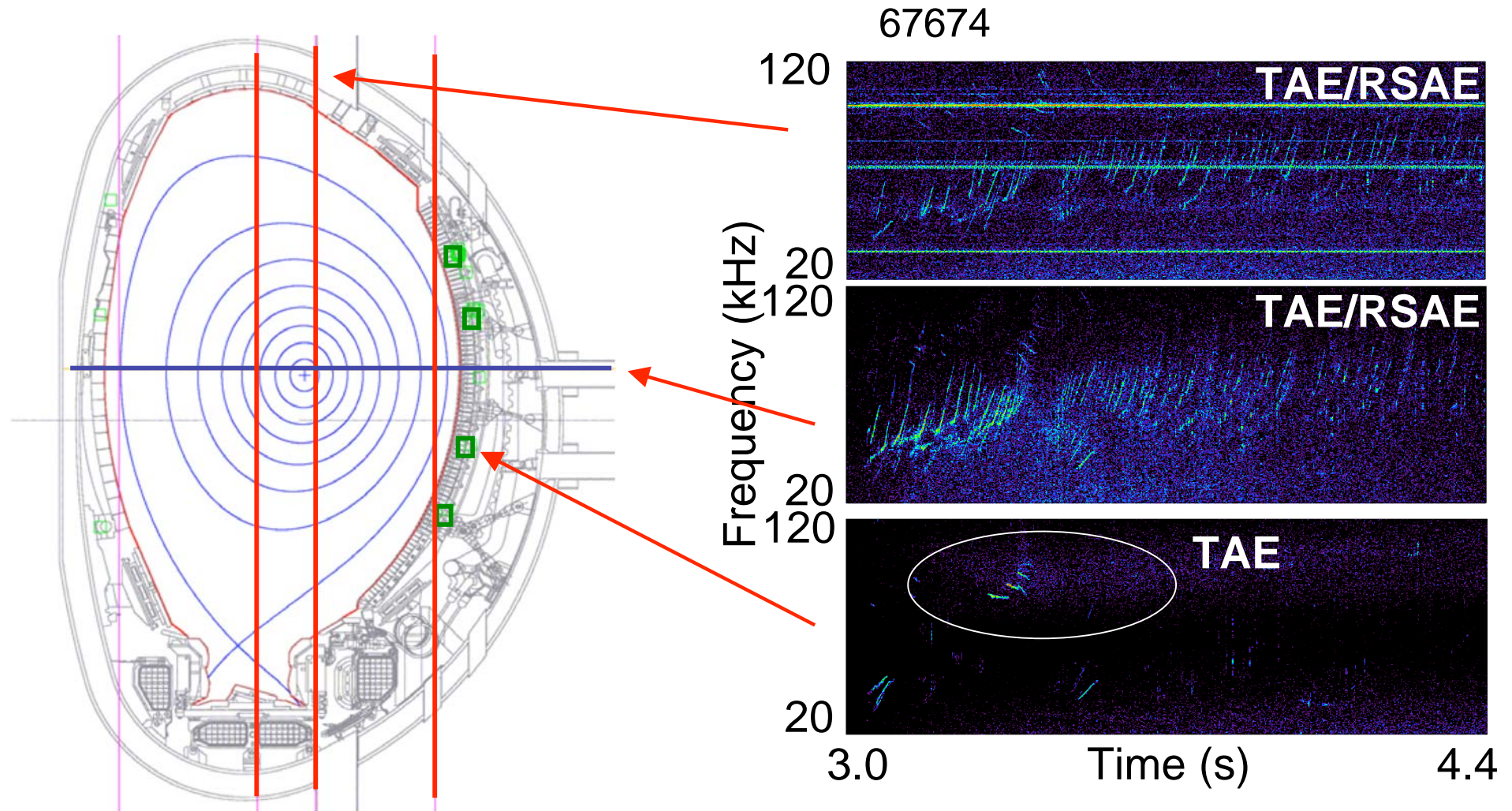


# Experimental Scenario on JET Alfvén Eigenmode Study in Reverse Magnetic Shear plasmas



- Lower Hybrid Current drive is used to obtain reversed shear ( $P_{\text{LHCD}} = 2 \text{MW}$ )

# JET in Reverse Magnetic Shear Plasmas Indicate Many : Unstable Alfvén waves even for $V_{\parallel} \approx 0.16 V_A$



- RSAEs have been observed in JET down to  $V_{\parallel} \approx 0.11 V_A$  in JET

# Modes Observed Below the Fundamental Resonance Condition in DIII-D and JET

	Fundamental resonance	JET $V_{\parallel} \approx 0.16 V_A$	DIII-D $V_{\parallel} \approx 0.23 V_A$
RSAE	$V_{\text{RES}} \geq 0.2 V_A$	✓	✓
TAE	$V_{\text{RES}} \geq 0.33 V_A$	✓ ✓	✓ ✓
EAE	$V_{\text{RES}} \geq 0.5 V_A$		✓ ✓

✓ =mode observed

✓ ✓ =mode observed below fundamental resonance

# Modes Observed Below the Fundamental Resonance Condition in DIII-D and JET

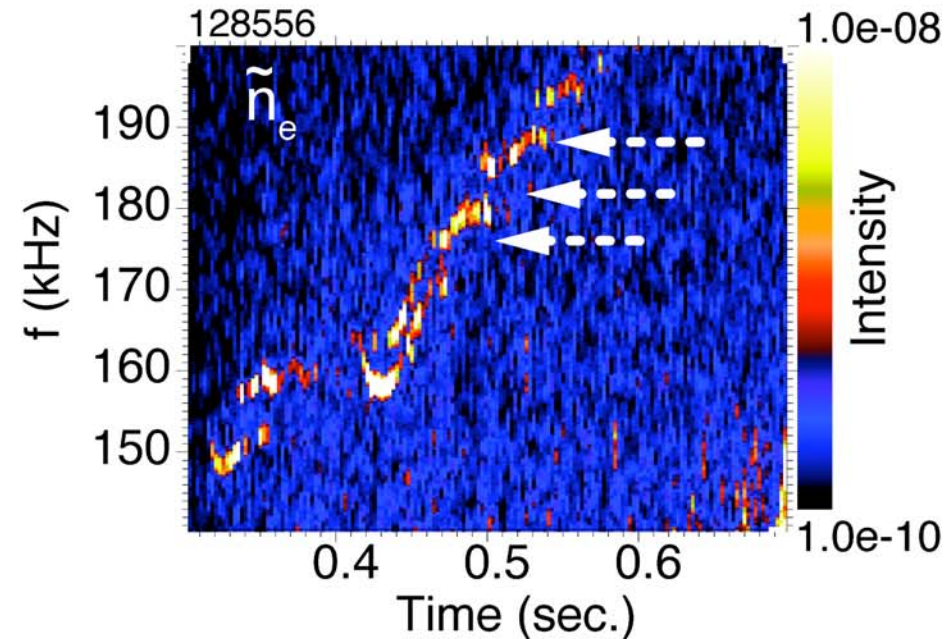
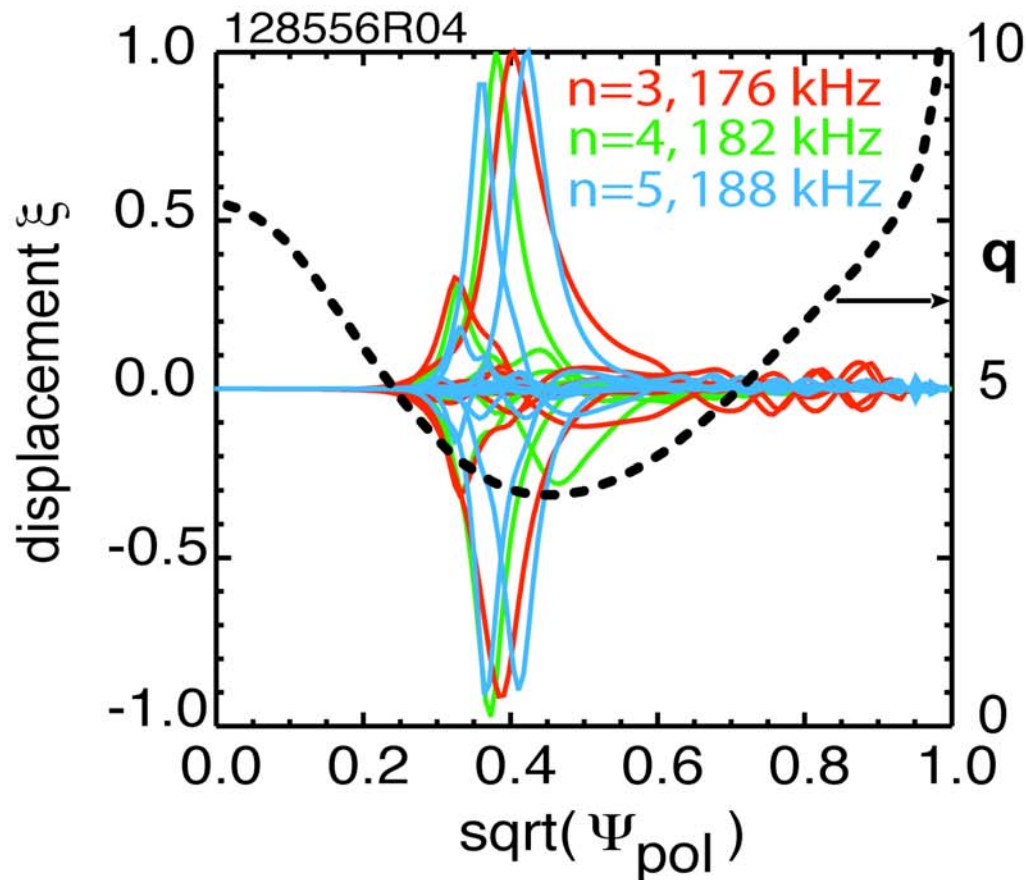
	Fundamental resonance	JET $V_{\parallel} \approx 0.16 V_A$	DIII-D $V_{\parallel} \approx 0.23 V_A$
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TAE	$V_{\text{RES}} \geq 0.33 V_A$	✓ ✓	✓ ✓
EAE	$V_{\text{RES}} \geq 0.5 V_A$		✓ ✓

- TAE in JET and EAE in DIII-D are well matched:  $V_{\parallel}/V_{\text{RES}} \approx 0.5$

# Outline

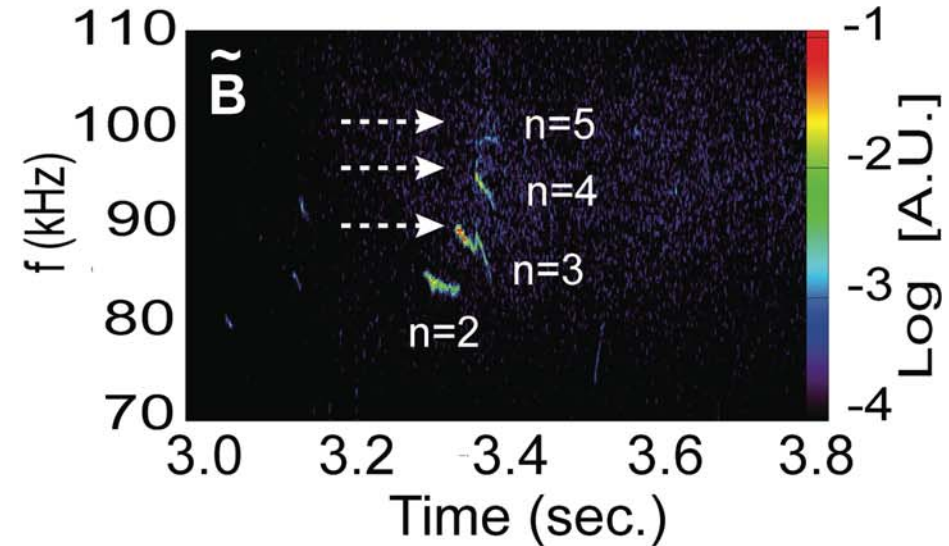
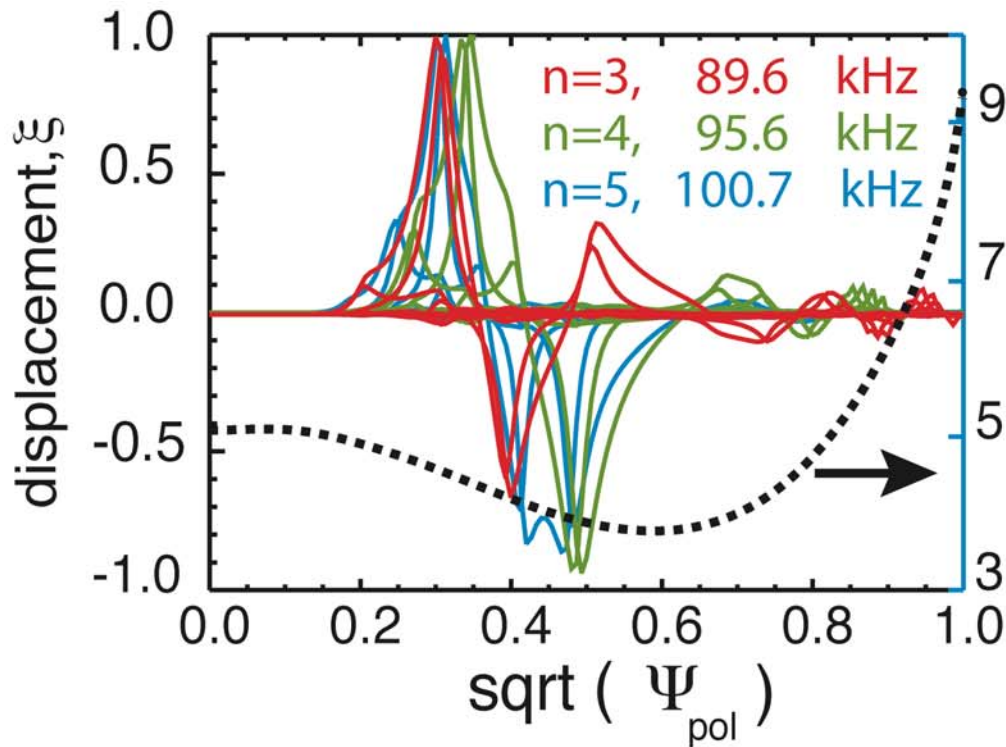
- Observation of Alfvén wave excitation below the fundamental resonance condition in DIII-D and JET
- **Ideal MHD analysis of radial mode structure, location**
- Stability analysis and coupling to high order resonances
- Implications

# Eigenmode Analysis Confirms Localization of EAEs to the Reverse Magnetic Shear Region of DIII-D



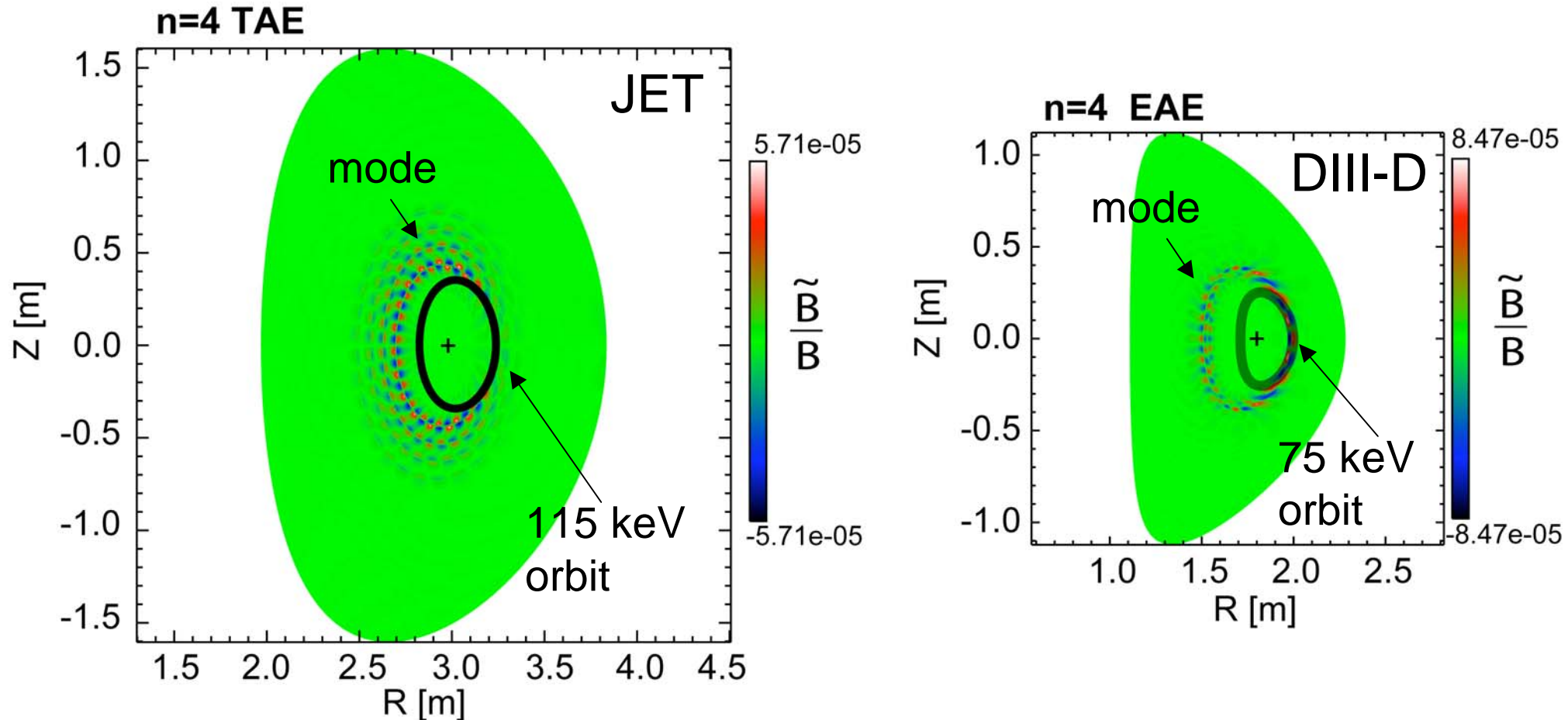
- Mode frequencies agree with experiment
- Core localization agrees with EC emission measurements

# Eigenmode Analysis Confirms Localization of TAEs to the Reverse Magnetic Shear Region of JET



- Calculations agree with magnetic measurements for mode frequency and toroidal mode number ( $n=3, 4, 5$ )
- Core localization confirmed from central interferometer measurements

# Short Poloidal Wavelength and Large Beam Ion Drift Orbits in JET and DIII-D Reverse Shear Plasmas



- $k_{\theta}\rho \approx 1$  in JET and  $\approx 2$  in DIII-D, expect high order resonances

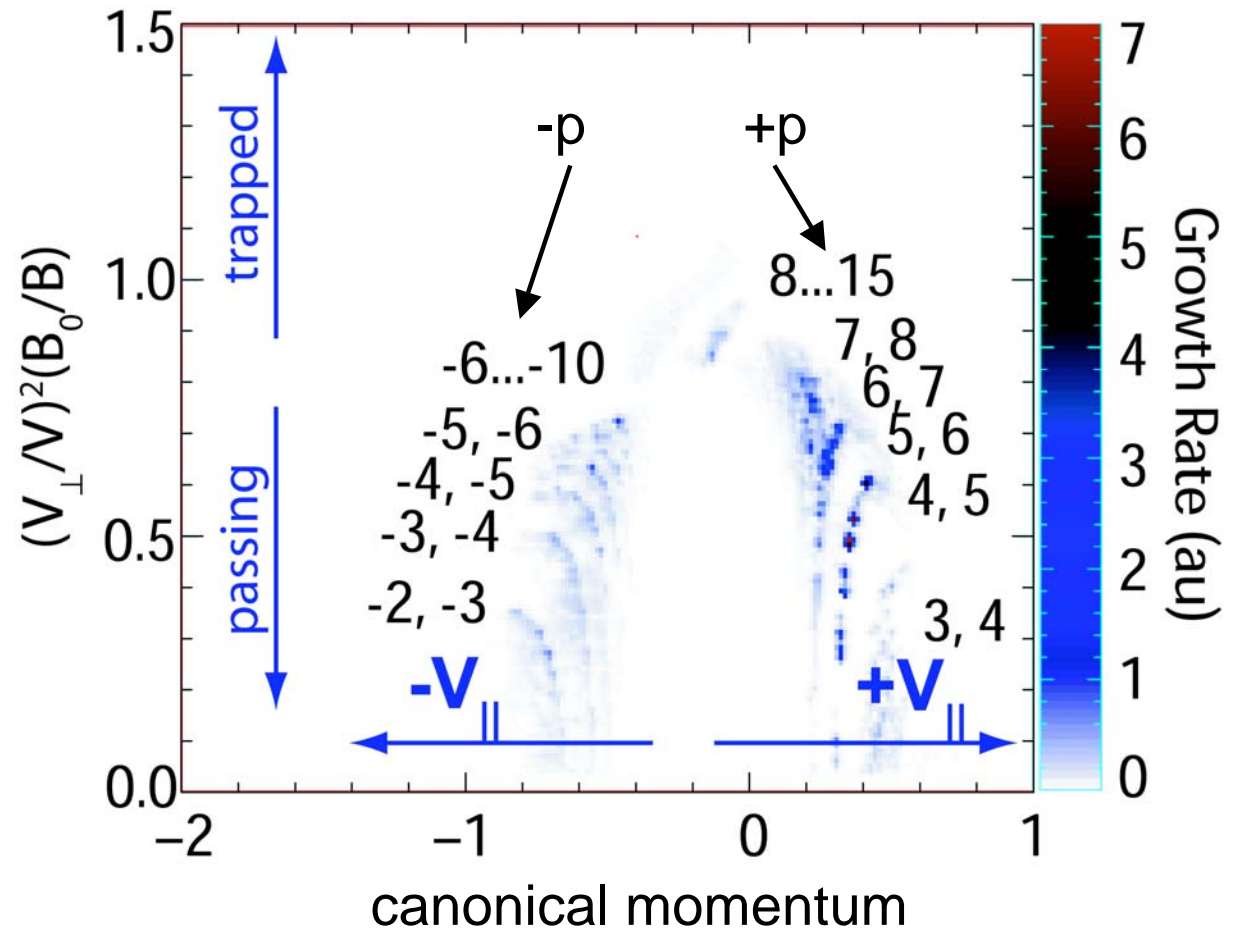


# Outline

- Observation of Alfvén wave excitation below the fundamental resonance condition in DIII-D and JET
- Ideal MHD analysis of radial mode structure, location
- Stability analysis and growth rate from high order resonances
- Implications

# NOVA-K Analysis Reveals Many High Order Resonances Contribute to Mode Drive for EAEs in DIII-D

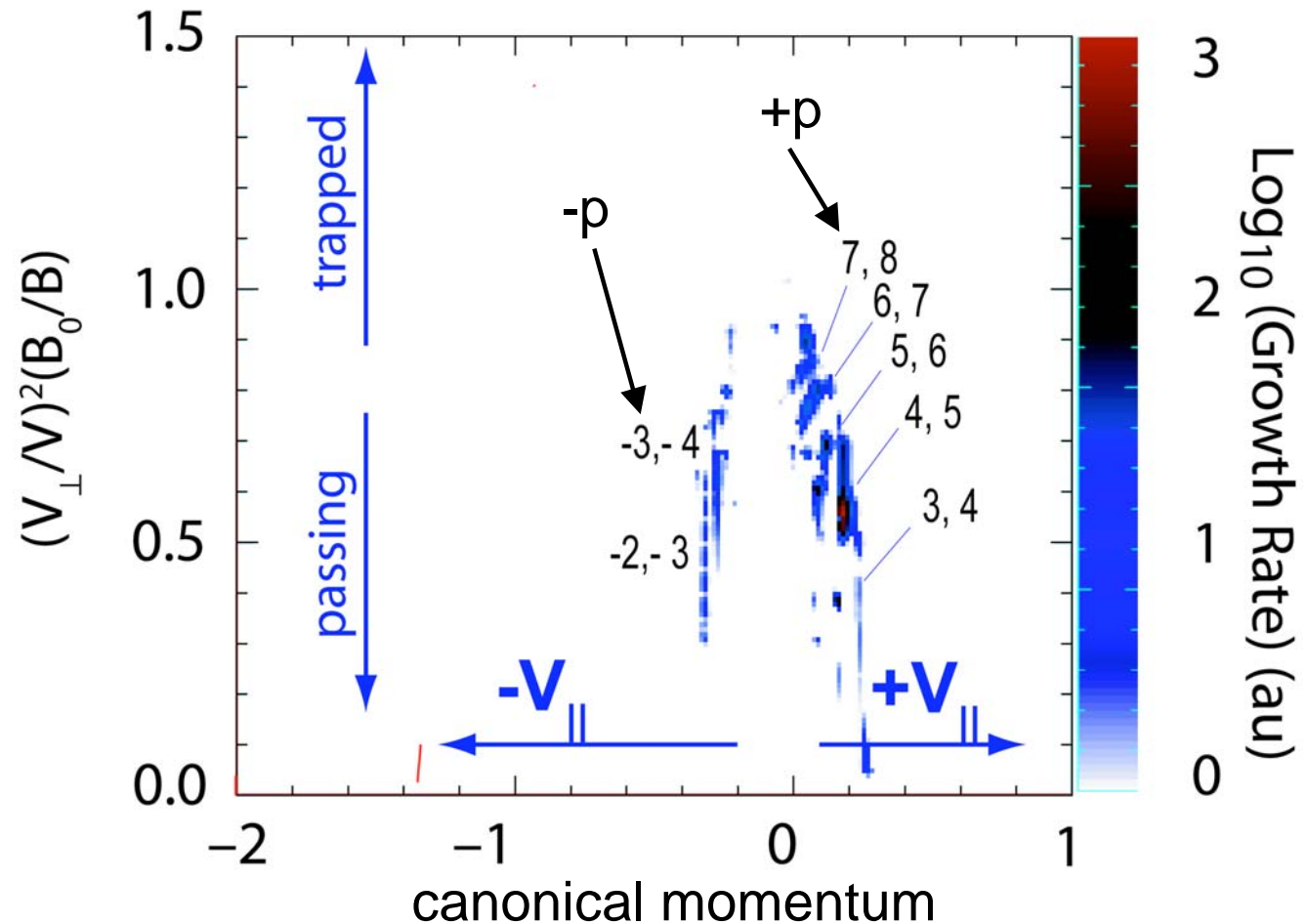
- $V_{\parallel} \propto \omega/p$  at high  $p$
- $p = \text{const.} \rightarrow V_{\parallel} \approx \text{const.}$
- 75 keV ions injected into region of strong high order resonances



- Scattering of co-injected 75 keV ions into counter going orbits calculated using the TRANSP code

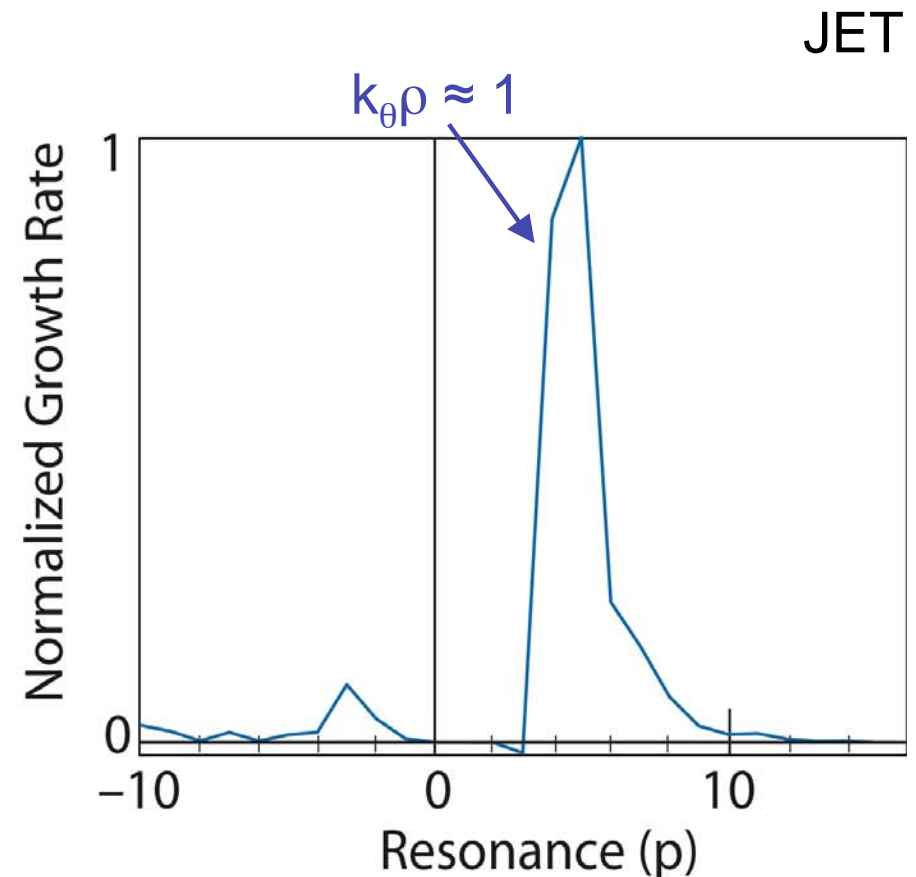
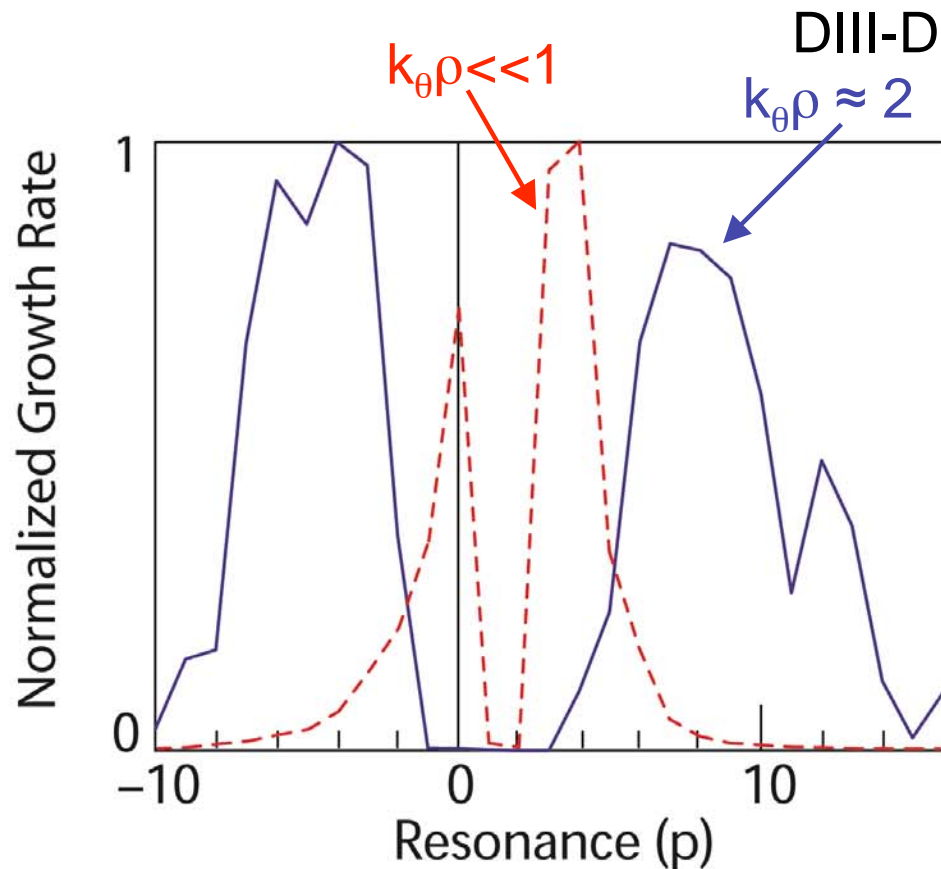
# NOVA-K Analysis Reveals Dominant High Order Resonances Contribute to Mode Drive for TAEs in JET

- 115 keV ions injected into region of strong  $p=4,5$  resonances
- All resonances are for passing ions



- Scattering of co-injected 115 keV ions into counter going orbits calculated using the TRANSP code

# Contribution to Mode Drive from co-going Beam Ions Comes Mostly From $p=6-10$ in DIII-D and $p=4-5$ in JET



- Forcing  $k_{\theta}\rho \ll 1$  in DIII-D shifts the spectrum down to the lowest accessible resonance; dramatically weakens drive

# Simple Estimate of High Order Resonance Condition Consistent with NOVA-K Stability Analysis

	High order resonance	JET $V_{\parallel} \approx 0.16 V_A$	DIII-D $V_{\parallel} \approx 0.23 V_A$
RSAE	$V_{\text{RES}} \geq V_A/4p$	$p \geq 2$	$p \geq 1$
TAE	$V_{\text{RES}} \geq V_A/2p$	$p \geq 3$	$p \geq 2$
EAE	$V_{\text{RES}} \geq V_A/p$	$p \geq 6$	$p \geq 4$

- No clear velocity threshold for mode excitation, consistent with experiment
- EAE not seen in JET plasma, consistent with higher threshold

# High Order Resonance Excitation of Alfvén Waves Confirmed in High-q Regimes on JET and DIII-D

- Large drift orbits and high  $k_{\theta}$  at high-q are key to excitation
- Implications
  - No sharp velocity threshold
  - Resonance can extend over a large region of phase space
  - Fast ion transport induced by these multiple resonances needs to be assessed
- In ITER, growth rate peaks For  $k_{\theta}\rho_{\alpha} \approx 1$  (n=8-20)
  - High order resonances will contribute to mode drive in steady state regimes
- Future work: Identify losses associated with these resonances