Influence of Beta, Shape and Rotation on the H-mode Pedestal Height

by A.W. Leonard with

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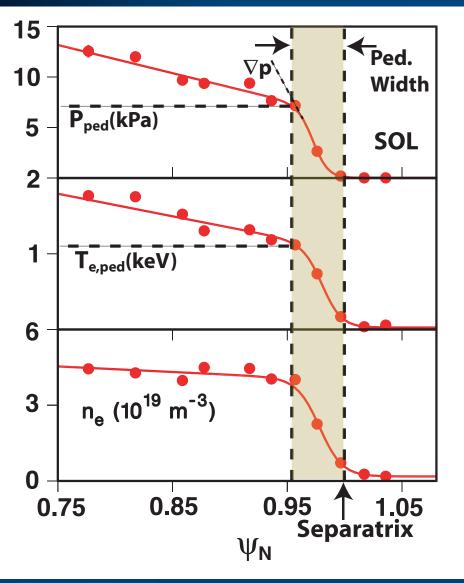
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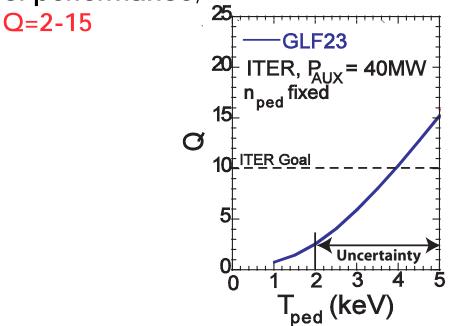




Pedestal Height is Greatest Uncertainty in Predicting Tokamak Performance



- Pedestal sets boundary condition for core transport
- For stiff transport, core profiles strongly dependent on pedestal
- Pedestal uncertainty for ITER corresponds to a wide range of performance;





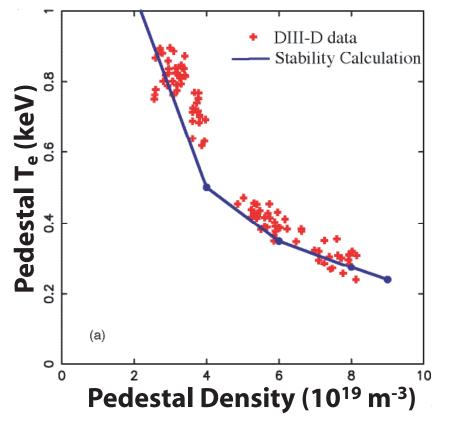
Pedestal Width is key to Pedestal Height Scaling

- Validated edge stability model can predict pedestal top pressure if width is known
- Pedestal pressure height increases with improved edge stability
 - Pedestal pressure increase with global $\boldsymbol{\beta}$ and stronger shaping
 - No change with toroidal rotation
- Stability model utilized to extract pedestal width
 - Greater accuracy than directly measured width
 - Pedestal width increases with higher pedestal pressure
 - Pedestal pressure rise double expected from stability with fixed width
- Pedestal models predict an ion gyro-radius, ρ^* , width scaling, yet
 - Width correlated with pressure ($\Delta \propto \beta_{ned}^{1/2}$)
 - No $T_i \left(\rho^{\star} \right)$ dependence



Validated MHD Stability Model a Tool for Extracting Pedestal Width from Pedestal Pressure

<u>DIII-D Stability Study:</u> Fixed parameters; I_p, B_t, Shape, pedestal width, etc.

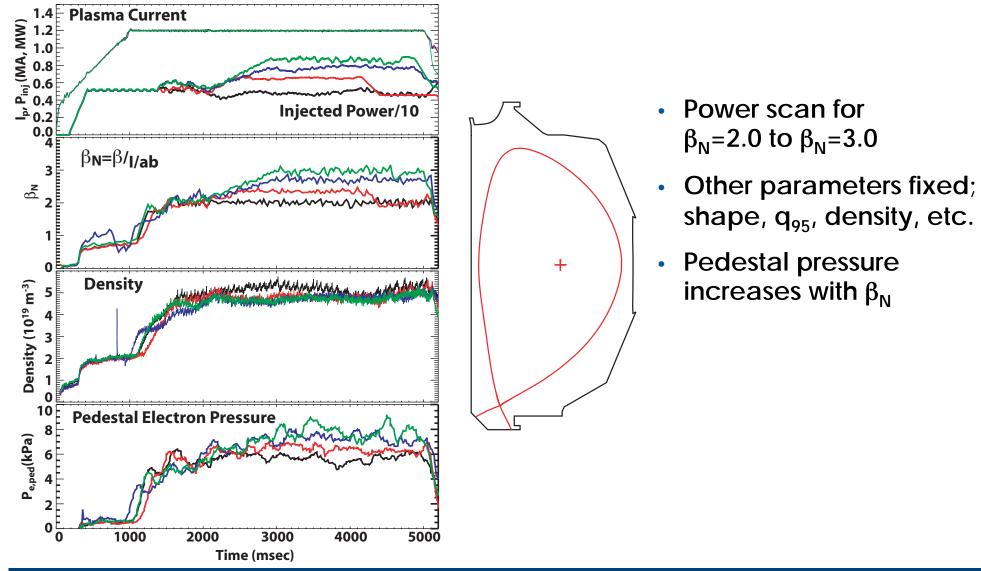


[P.B. Snyder, H.R. Wilson, et al., PPCF 46 (2004) A131]

- The peeling-ballooning model has been validated over a range of conditions
- Stability model predicts pedestal pressure for a given width
- Stability model can extract width from a measured pedestal pressure
 - Pedestal top more accurately measured than gradient and width

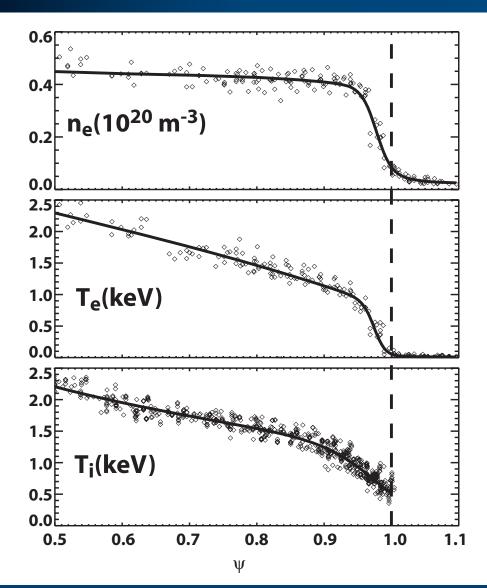


Pedestal Pressure Increases with Global Beta





Pedestal Profiles Fit Just Prior to an ELM



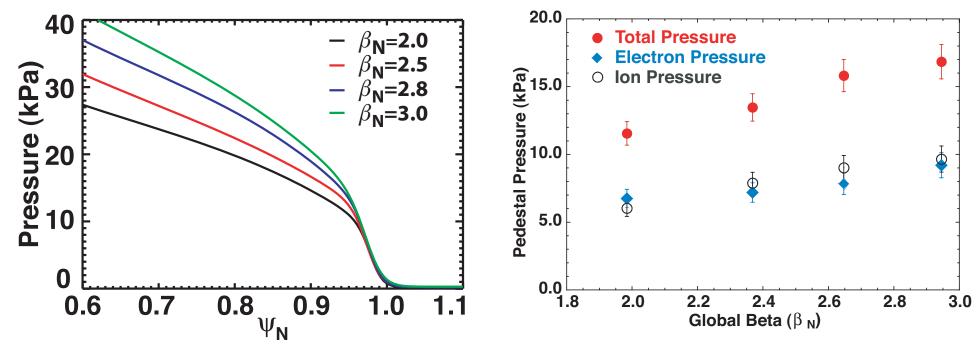
- Profiles fit to data combined from the last 20% of many ELM cycles
- Hyperbolic tangent fit to profiles
 - Pedestal height more certain, 5-10%
 - Width/gradient less certain, ~20%
- T_i pedestal is usually significantly wider than T_e or n_e
 - Ion pressure width set by density width
- Pedestal pressure characterizes pedestal height for comparison with stability analysis



Pedestal Pressure Increases with β_N

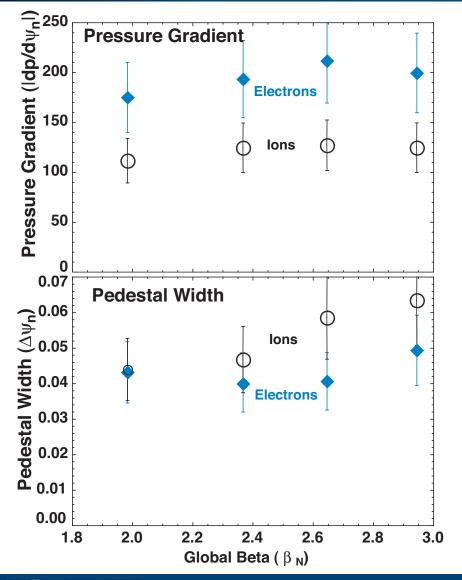
Total pedestal pressure increases ~50% as β_N increases from 2.0-3.0

Both electron and ion pedestal pressure increase





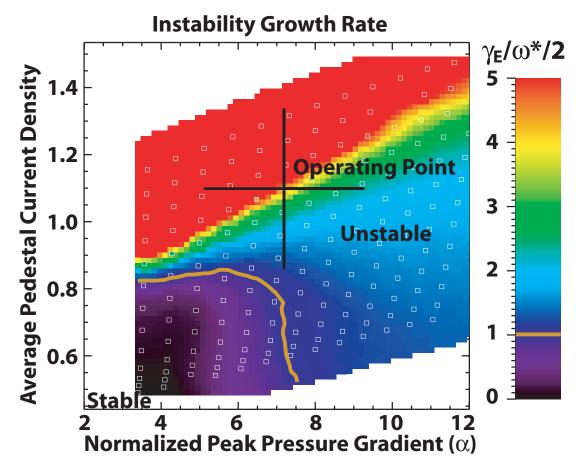
Both Pressure Gradient and Width Increase with β_N



- Both gradients and widths increase with β_{N}
- Larger uncertainty, ~20%, for gradient and width measurements
- Stability constraint applied to pressure can reduce uncertainty in pedestal width scaling



Stability Space is Mapped for Each Configuration

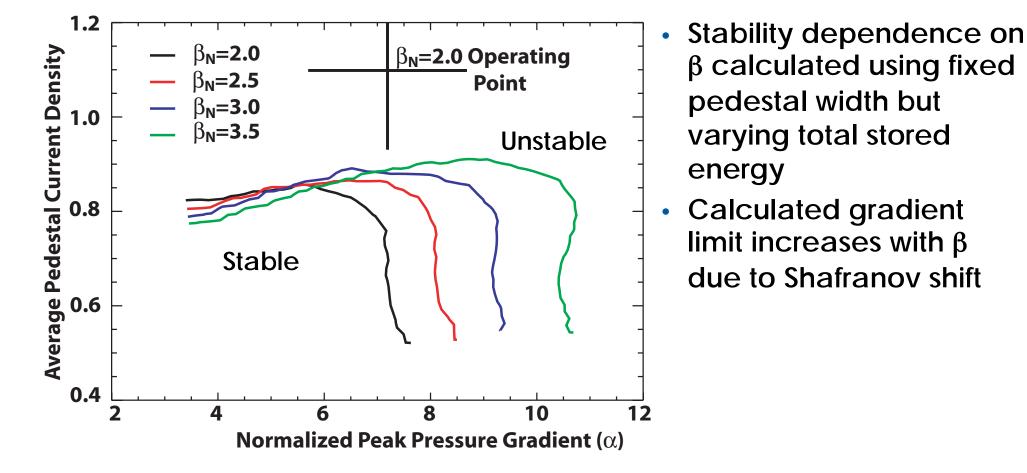


- MHD equilibria constructed by measured pressure profile and Sauter bootstrap model for edge current
- Create 2D array of equilibria with varying pedestal current and pressure
 - Fixed pedestal width
 - Fixed total stored energy
- Stability analysis of each equilibrium using ELITE, n=5-25
 - Stability threshold: $\gamma_E \leq \omega^*/2$
- Variation in stability threshold analyzed for varying global β, shape, etc.



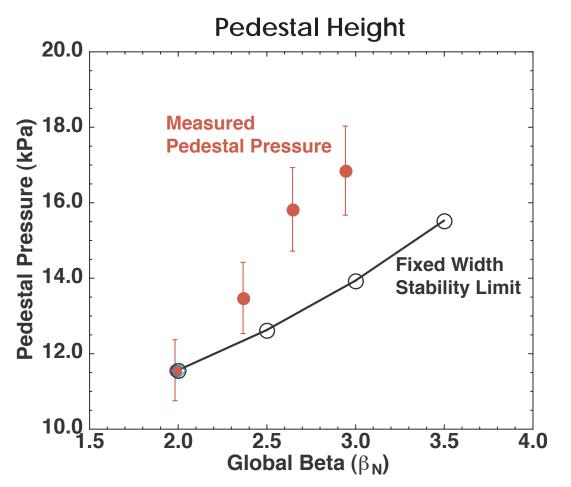
Pressure Gradient Limit for Fixed Width Increases with Global β

Stability Contours for β_N Variation with Fixed Width



NATIONAL FUSION FACILITY

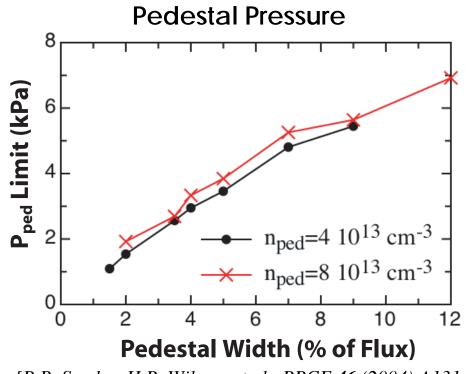
Improved Stability at Fixed Pedestal Width Can Account for Half of Pedestal Pressure Rise with β_N

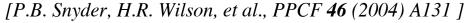


- Measured pedestal pressure proportional to global β_N
- Increase in stability limit at fixed pedestal width accounts for only half of observed increase in P_{ped} with β_{N}
- Width must increase with β to account for pedestal pressure increase



Pedestal Gradient Expected to be Weakly Reduced with Increasing Width





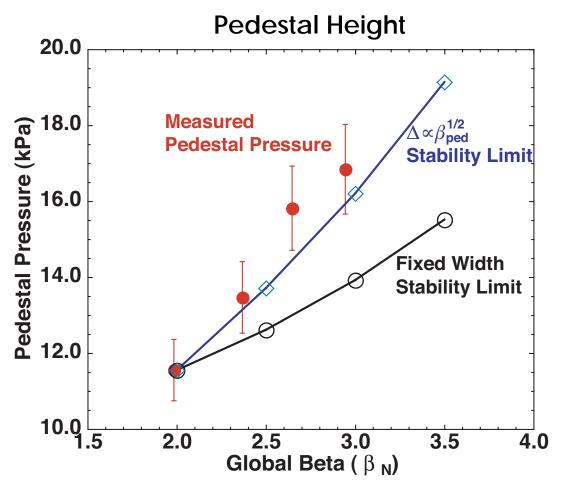
 Previous numerical studies indicate width (Δ) scaling of stability limit:

-
$$abla p_{crit} \propto \Delta^{-1/4}$$
 or $P_{ped} \propto \Delta^{3/4}$

- All other parameters fixed;
 Shape, β, etc.
- Width variation of ∇p due to radial extent of finite *n* modes



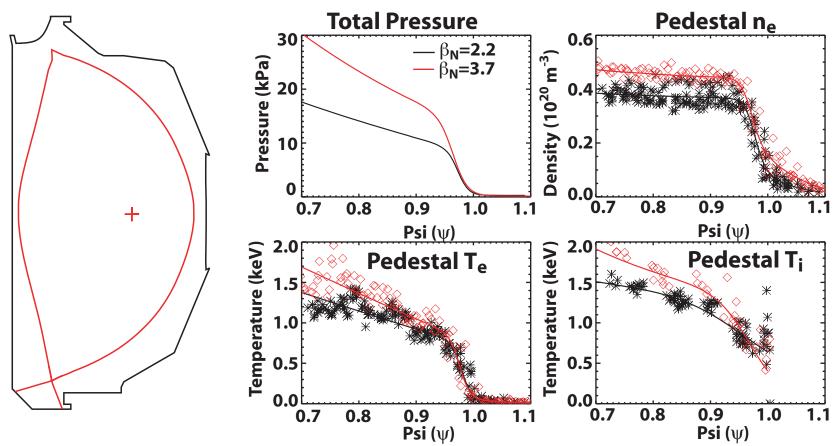
Stability Analysis Implies Pedestal Width Increase with $\boldsymbol{\beta}$



- Pedestal pressure proportional to global β_N
- Width must increase with β to account for measured pressure increase
- Width scaling consistent with previous statistical study
 - $\Delta \propto \beta_{ped}^{1/2}$
 - T.H. Osborne, et. al., Jour. Nucl. Mater., 266-269, 131 (1999)



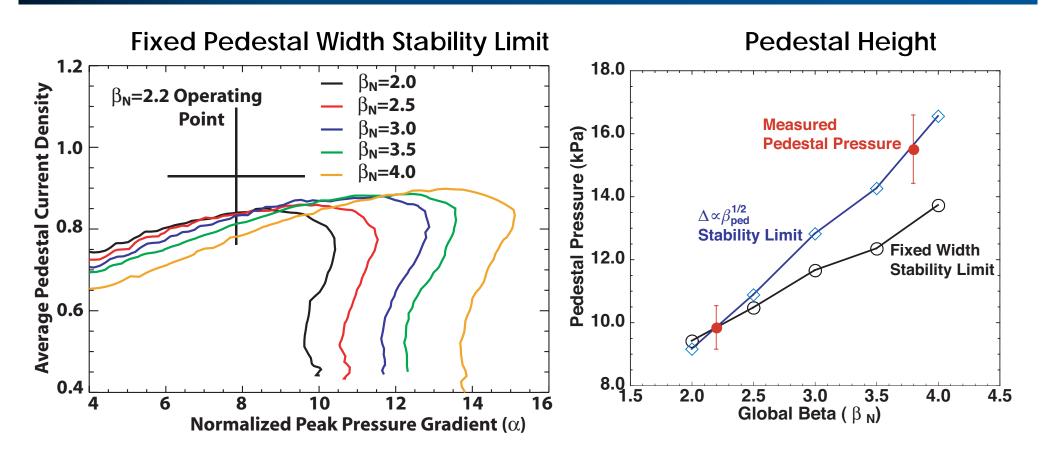
Similar Dependence of P_{ped} on global β_N Observed in High β Advanced Tokamak Regime



- High β scenario with early heating
- Increase in β_N from 2.2 to 3.7, ~68%
- Pedestal pressure rises from 9.8 kPa to 15.5 kPa, ~58%



Pedestal Width Scales with β in Advanced Regimes



- Pedestal stability continues to improve over wide range of β
- Pedestal width scaling, $\Delta \propto eta_{ped}^{1/2}$, consistent with pressure increase

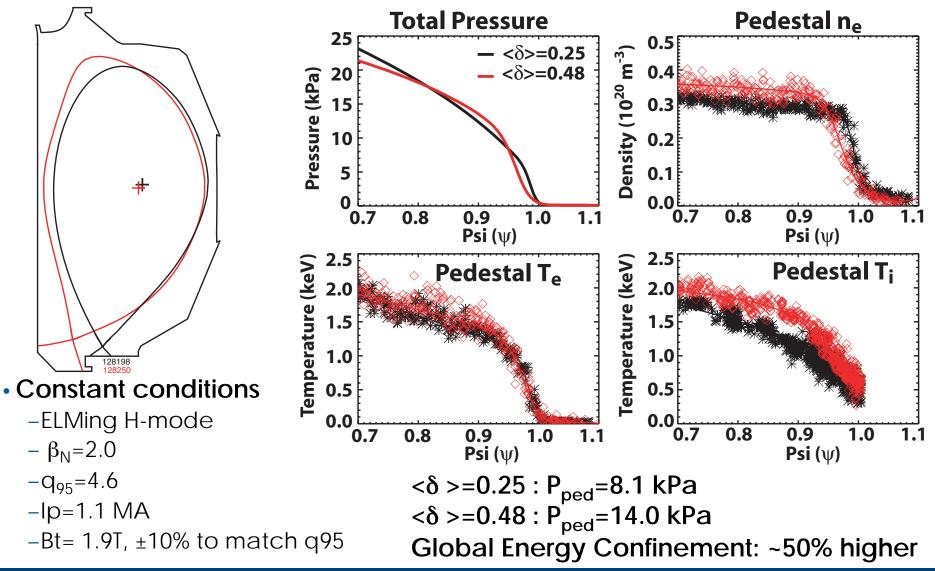


Shape an Important Factor for Pedestal Height

- Shape dependence for pedestal and core confinement long observed
- Stronger shaping improves edge stability
 - Elongation, triangularity, squareness, second separatrix, etc.
- Contribution of stability to increased pedestal for stronger shaping not generally quantified
- Stronger shaping leads to higher stability limit and wider pedestal

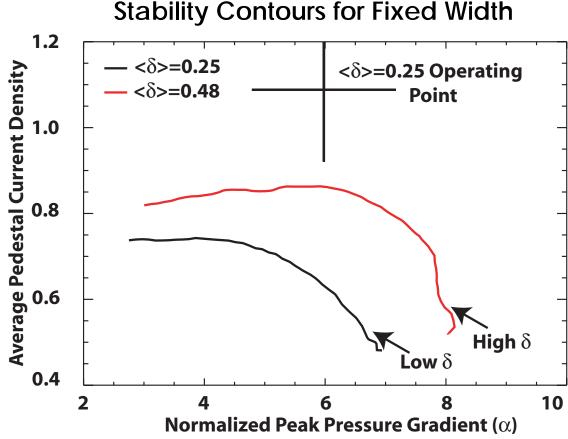


Shaping Can Produce Wide Range of Pedestal Heights





Pedestal Width Increases with Stronger Shaping



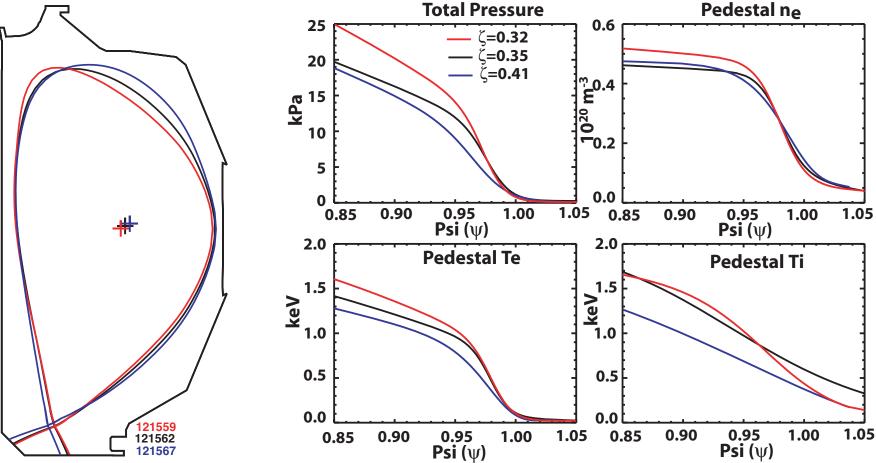
- Stronger shaping raises pedestal pressure 72%
 - Stability limit increases ~33% assuming fixed width
 - Width increase of 31% for $\Delta \propto \beta_{\rm ped}^{1/2}$ scaling yields
 - Expected increase in P_{ped} of 75%, in agreement with experiment



Moderate Changes to ITER Shape Can Significantly Affect Pedestal



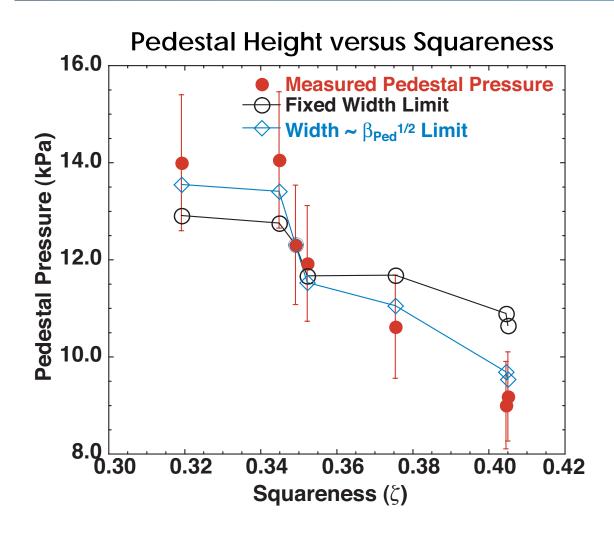
Measured Pedestal Profiles in ELMing H-mode





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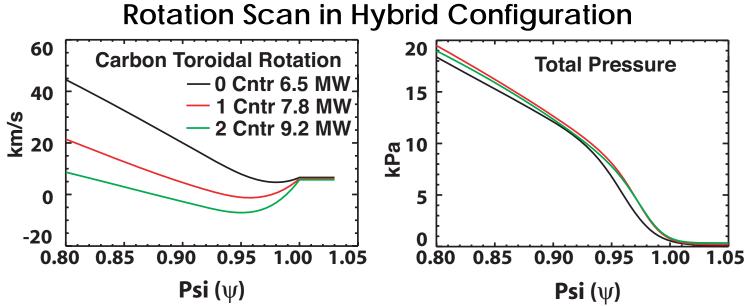
Pedestal Width Decreases with Squareness



- Pedestal pressure increases ~50% from highest to lowest squareness
- Improved stability for fixed width can account for half of pedestal pressure increase
- Pedestal width $\Delta \propto \beta_{ped}^{1/2}$ consistent with pressure variation



Toroidal Rotation does not Significantly Affect Pedestal Height



- Ratio of co to counter NBI to control rotation
- While central confinement degraded with counter injection pedestal pressure not significantly affected
- Previous stability studies in this parameter regime indicate edge stability limit not modified by toroidal rotation

[P.B. Snyder, et al., Nucl. Fusion 47 (2007) 961]



Implications for Pedestal Width Scaling

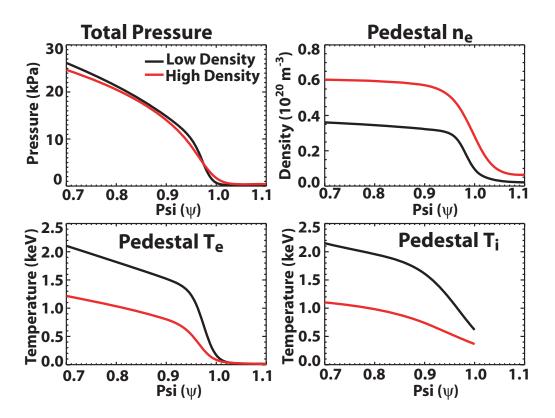
 Significant gyro-radius dependence expected if width set where ExB velocity shearing exceeds driftwave growth rate

$$- \Delta \propto \rho^{0.5-2.0} \left[f(S,\alpha,q) g(Z_{eff}) h(v^*) \right]$$

- Complicated dependence on other dimensionless parameters
- Possible $\Delta \propto \beta_{ped}^{1/2}$ pedestal width scaling mechanisms:
 - β_{ped} correlation with ρ^* : Improved stability leads to higher T_i
 - β_{ped} correlation with other parameters: S, α , etc.



Gyro-Radius Scaling Not Yet Observed



- ρ* reduced, but pedestal not narrower
- Other dimensionless parameters change; collisionality, shear, etc.

- The ρ* pedestal width scaling is critical
 - If $\Delta \propto \rho^*$, ITER likely not to achieve its mission
 - Current experiments cannot match ITER ρ^{\star}
 - Experiments in DIII-D, JT-60U
 and C-Mod have not found
 significant ρ* scaling
- A $\Delta \propto \beta_{ped}^{1/2}$ pedestal scaling consistent with single parameter scans in DIII-D and JT-60U

T.H. Osborne, et. al., Jour. Nucl. Mater., 266-269, 131 (1999)



Summary

- Pedestal pressure increases with improved edge stability
 - Increase twice that expected for fixed pedestal width
 - Pedestal width increase, $\Delta \propto \beta_{\it ped'}^{\rm 1/2}$ consistent with stability analysis and observed pressure variation
- Pedestal height and width not dependent on toroidal rotation
 - Consistent with stability analysis
- Future work to isolate underlying physics of width scaling
 - Universality of $\beta_{ped}^{1/2}$ scaling for pedestal width
 - Ion gyro-radius, ρ^{\star}
 - Other dimensionless parameters; S, α , q, etc.

