

# MHD Analysis of the Tokamak Edge Pedestal in the Low Collisionality Regime

## Thoughts on the Physics of ELM-free QH and RMP Discharges

**P.B. Snyder<sup>1</sup>**

Contributions from: H.R. Wilson<sup>2</sup>, D.P. Brennan<sup>1</sup>,  
K.H. Burrell<sup>1</sup>, M.S. Chu<sup>1</sup>, T. Evans<sup>1</sup>, M. Fenstermacher<sup>3</sup>,  
A. Kirk<sup>2</sup>, A. Leonard<sup>1</sup>, W. Meyer<sup>3</sup>, T.H. Osborne<sup>1</sup>,  
E.J. Strait<sup>1</sup>, M. Umansky<sup>3</sup>, P. West<sup>1</sup>, X.Q. Xu<sup>3</sup>, DIII-D Team

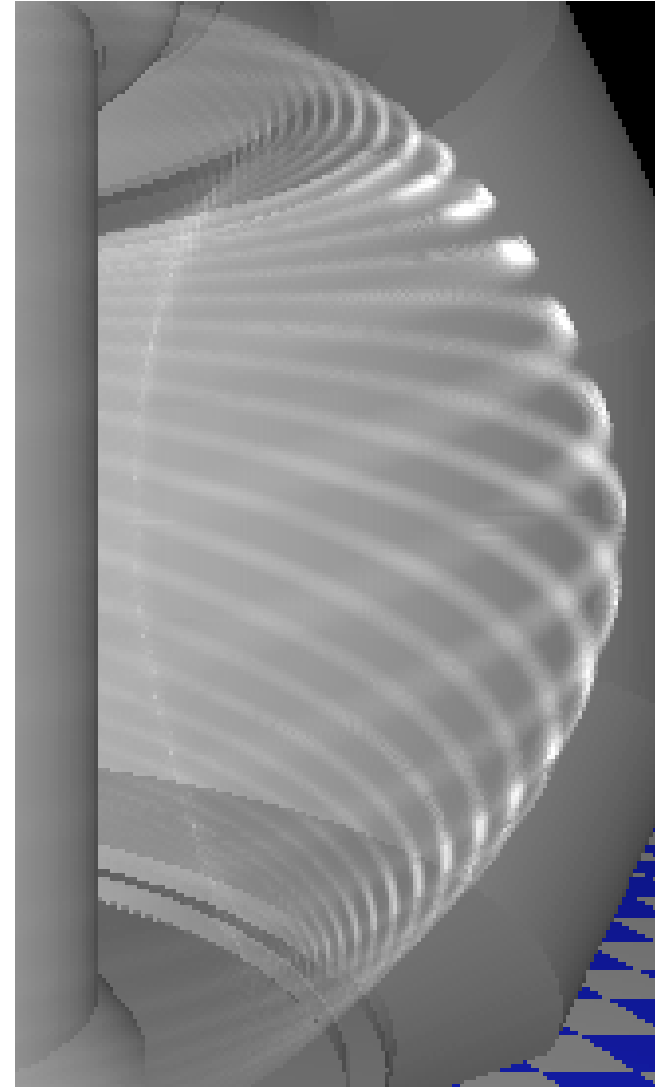
<sup>1</sup>General Atomics, San Diego, USA

<sup>2</sup>Culham Science Centre, Oxfordshire UK

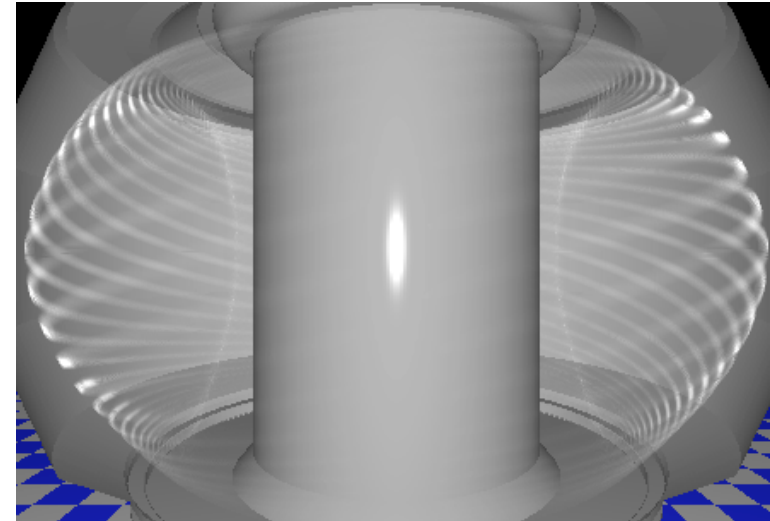
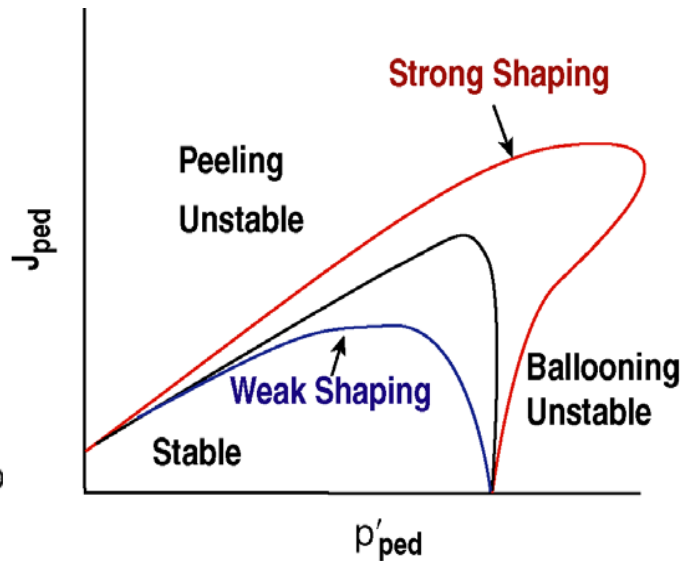
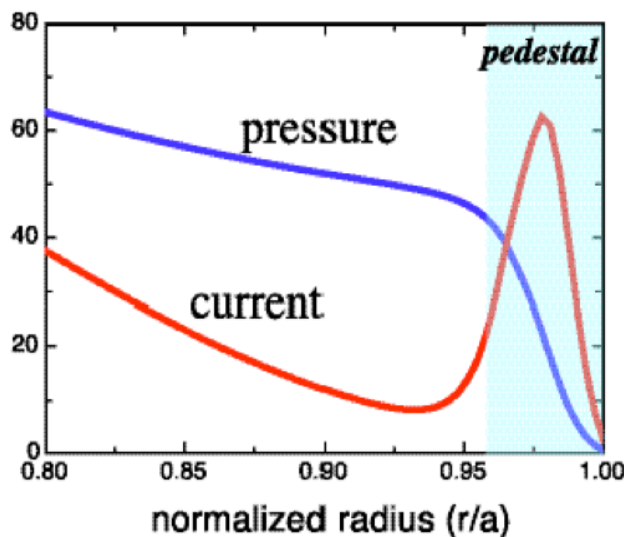
<sup>3</sup>LLNL, Livermore, CA USA

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# The Peeling-Ballooning Model

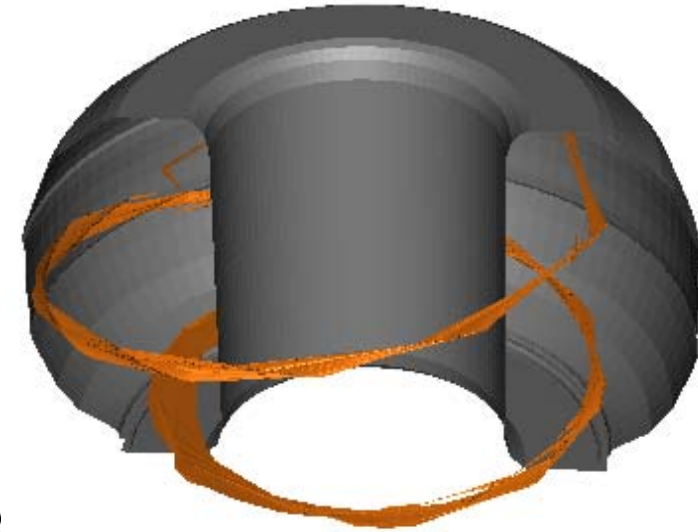
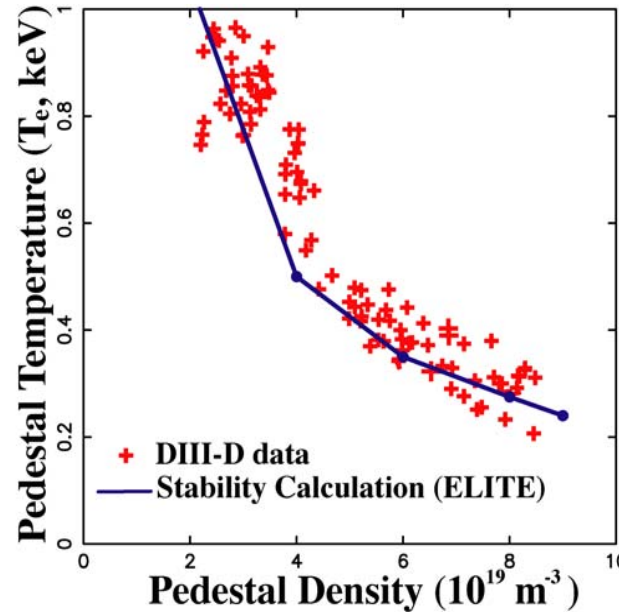
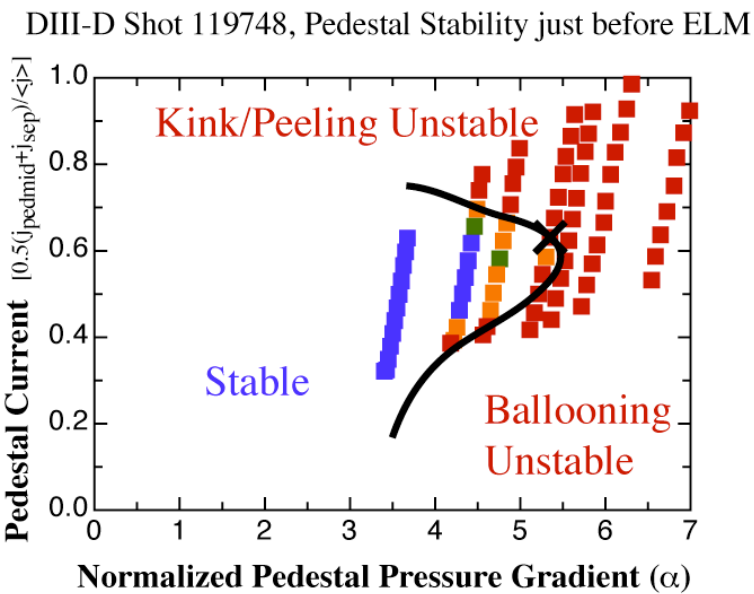


ELITE, n=18 mode structure

- **Pedestal Height and ELM heat impulses key issues for tokamaks/ITER**
  - Peeling-Ballooning model offers explanation for ELM onset and constraints on pedestal
- **ELMs caused by intermediate wavelength (n~3-30) MHD instabilities**
  - Both current and pressure gradient driven
  - Complex dependencies on  $v_*$ , shape etc. due to bootstrap current and “2nd stability”

[P.B. Snyder, H.R. Wilson, et al., *Phys. Plasmas* **9** (2002) 2037 & *Nucl. Fusion* **44** (2004) 320.]

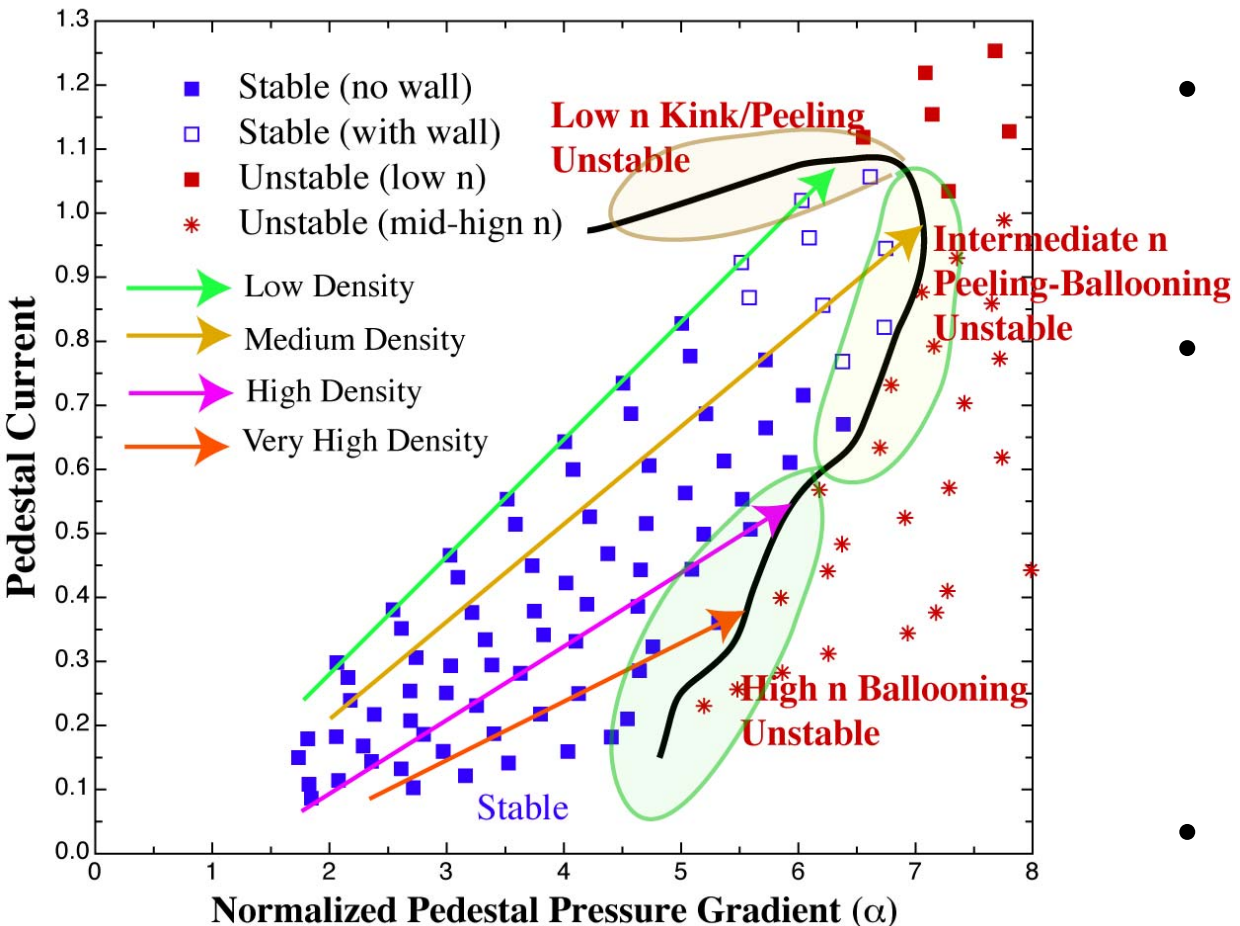
# The Peeling-Ballooning Model: Validation and Nonlinear Dynamics



- **Successful comparisons to expt both directly and in database studies**  
*[P.B. Snyder, H.R. Wilson, et al., Phys. Plasmas 9 (2002) 2037; D. Mossessian, P.B. Snyder et al., Phys. Plasmas 10 (2003) 1720; P.B. Snyder, H.R. Wilson, et al., Nucl. Fusion 44 (2004) 320.]*
- **Nonlinear: Expected P-B linear growth and structure in early phase, followed by explosive burst of one or many filaments into the SOL**
  - Leads to two-prong model of ELM losses (conduits and barrier collapse)  
*[P.B. Snyder, Phys Plasmas 2005, H.R. Wilson, PRL 2004] [See also DP Brennan oral]*
- **Picture developing to explain ELM onset and dynamics in the usual moderate to high density ELMing regime - initial comparisons of structure, radial velocity**
- **Much less focus on exciting new regimes, QH and RMP, which occur at low density and can be ELM-free**

# QH Modes Exist at Low Density, High Rotation

- QH mode operation generally requires *strong counter rotation* in the pedestal region and *low density*

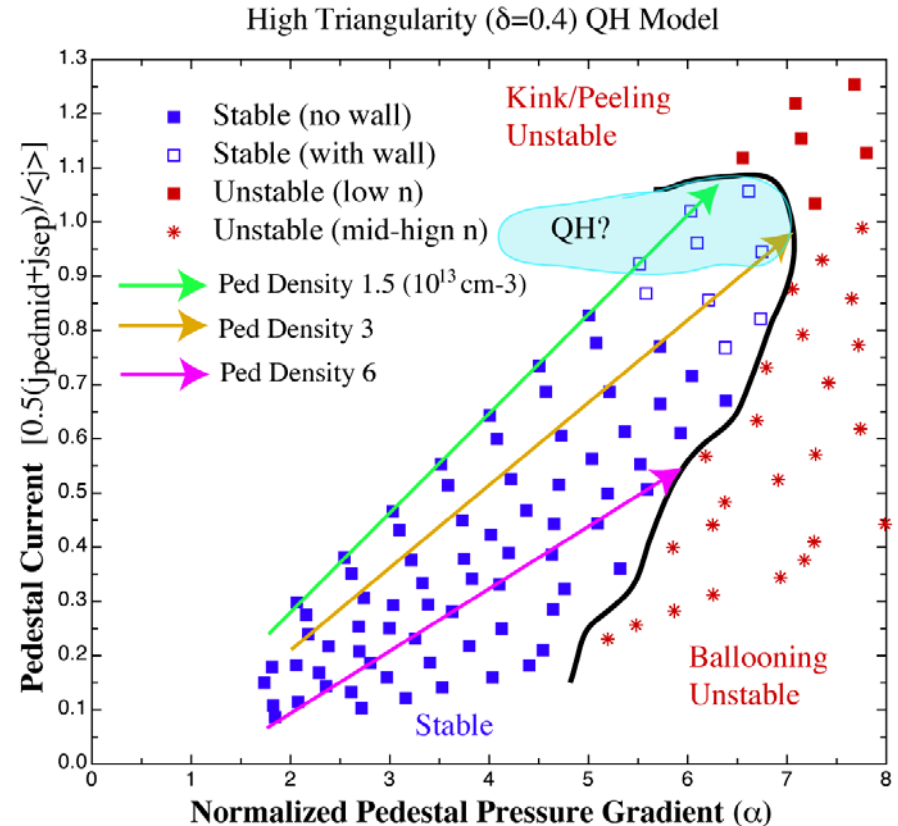
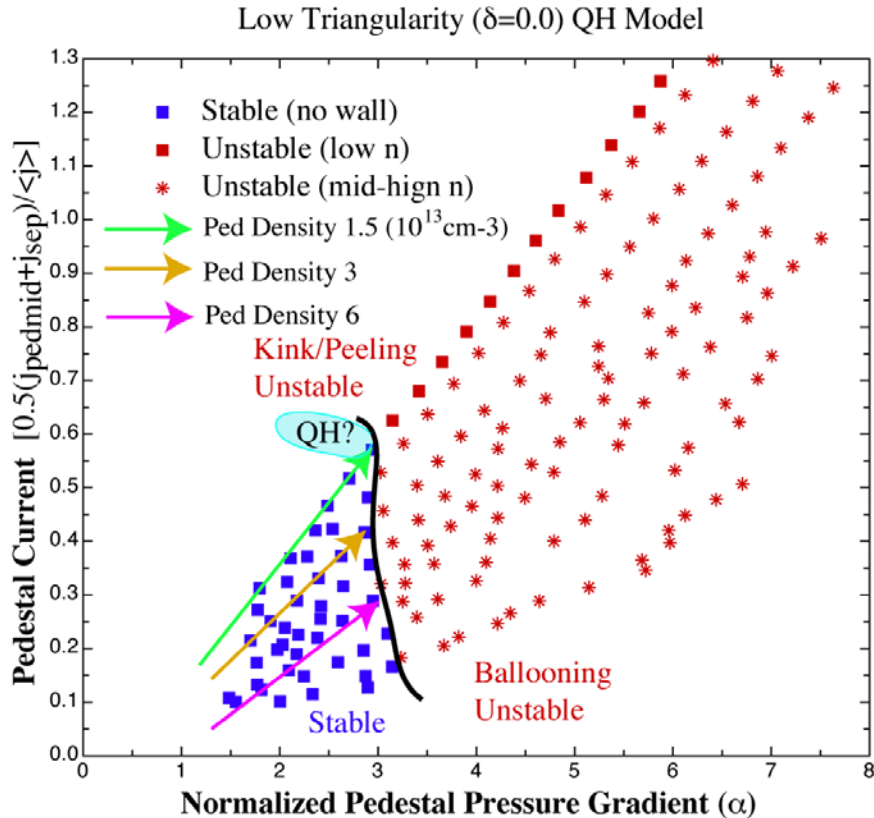


## Effect of Low Density

- The pedestal current is dominated by bootstrap current**
  - Roughly proportional to  $p'$
  - Decreases with collisionality
- Lower density means more current at a given  $p'$** 
  - ( $v_* \sim n_e^3$  at given  $p$ )
  - Moderate to high density discharges limited by P-B or ballooning modes
  - Very low density discharges may hit kink/peeling boundary
- Stability Analysis more complex at low density: uncertainty in current profile, resonant conditions**

# Theory: QH Mode Exists in Low-n Kink/Peeling Limited Regime

- Detailed Study Using Model Equilibria to Explore Stability Bounds in QH-like discharges



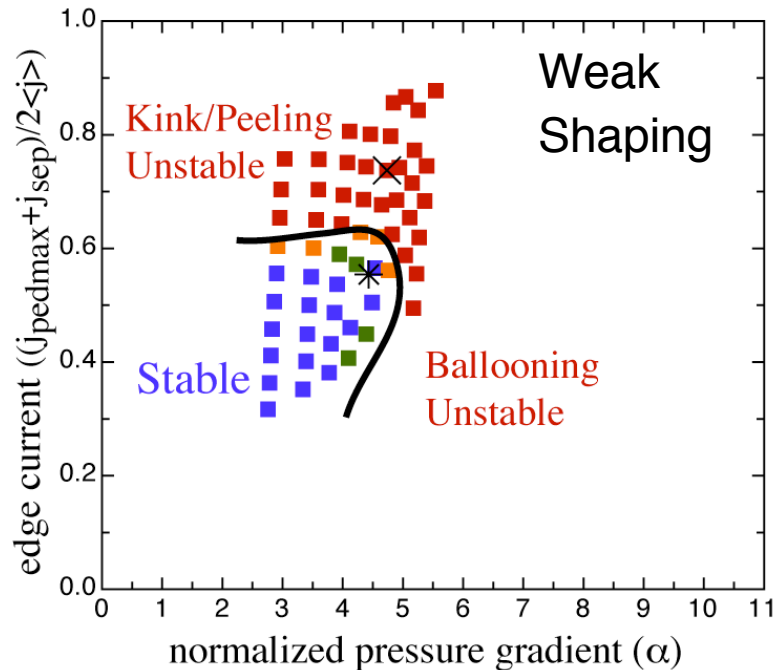
- Weak Shaping (left): QH Regime accessible only at very low density ( $n_{ped} < \sim 1.5 \cdot 10^{13} \text{ cm}^{-3}$ )
- Stronger Shaping (right): QH regime can be accessed at higher density (here up to  $n_{ped} < \sim 3 \cdot 10^{13} \text{ cm}^{-3}$ ), more robust
- Low-n modes experience some wall stabilization, despite localization



# Experiment: QH Discharges Exist Near Kink/Peeling Boundary

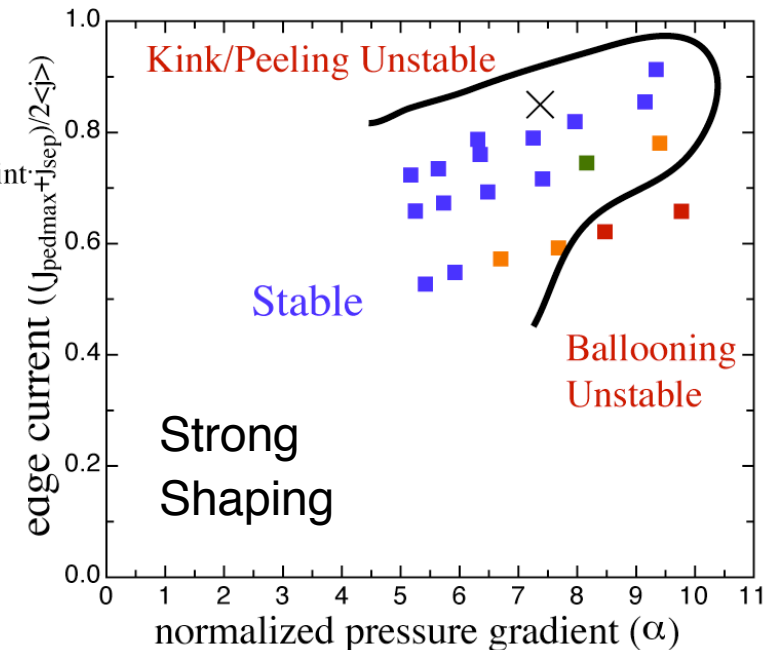
- Stability Studies Perturbing around reconstructed QH Discharges on DIII-D

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- stable ( $\gamma < 0.001$ )
- marginal ( $.001 < \gamma < .01$ )
- weakly unstable ( $.01 < \gamma < .075$ )
- unstable ( $.075 < \gamma < .125$ )
- × full bootstrap current operating point
- \* efit operating point

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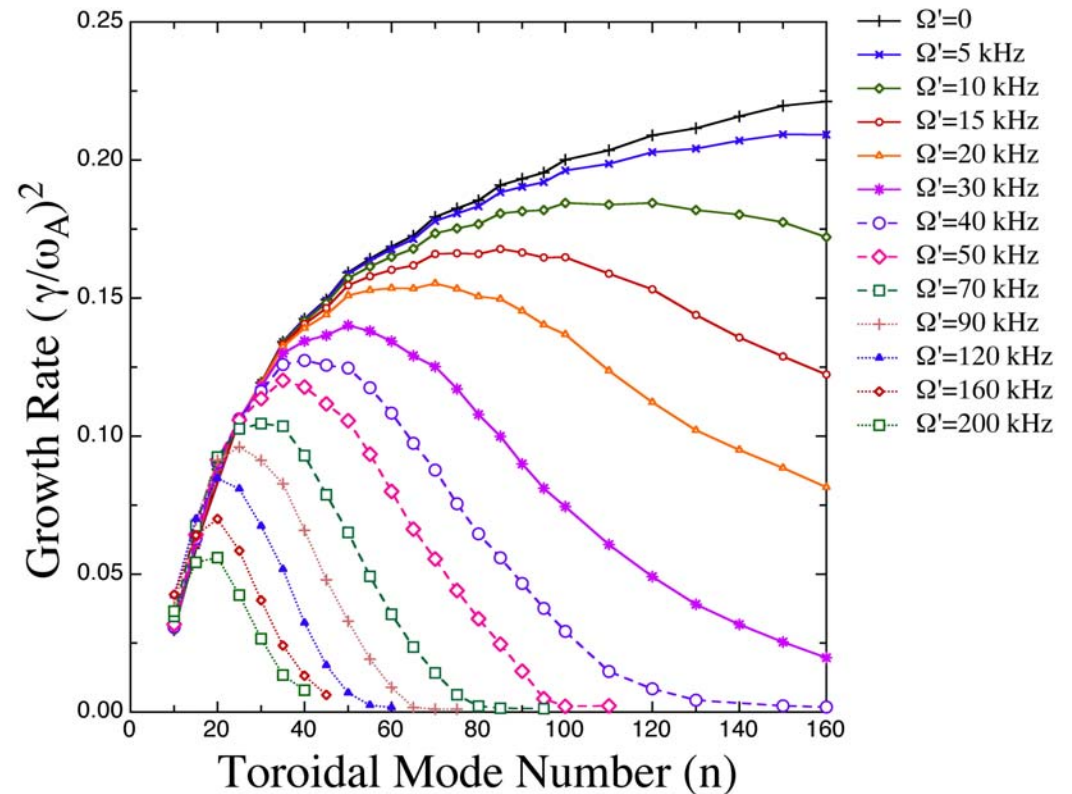
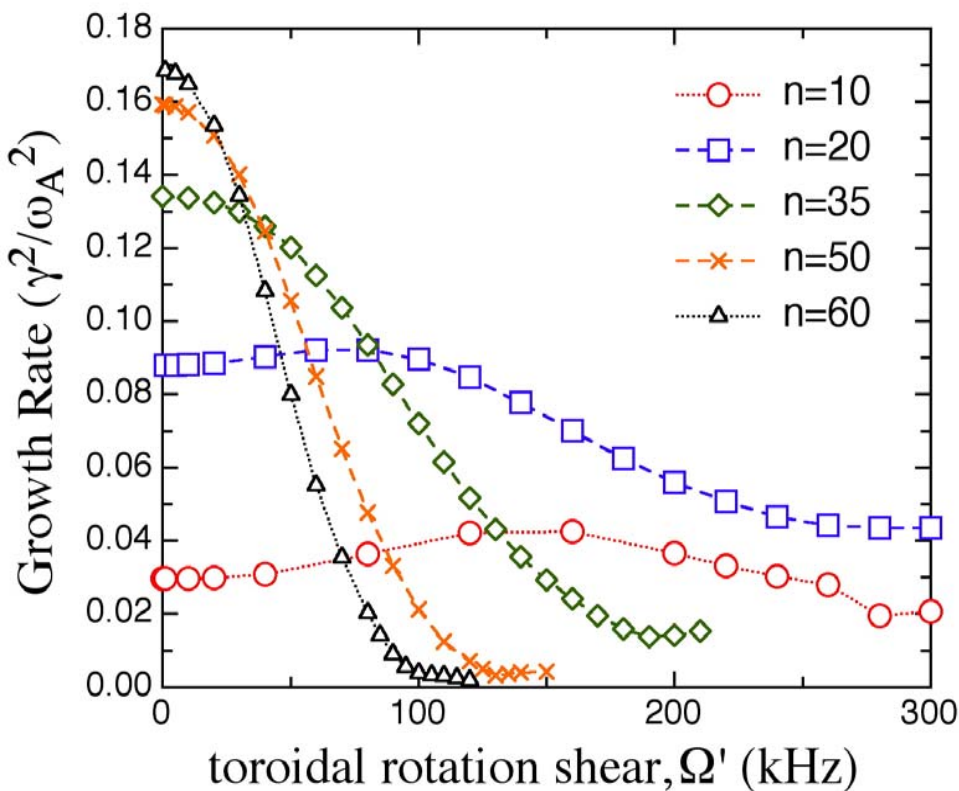


*[See WP West poster this afternoon for further details]*

- Moderate Shaping (left): QH operating point near kink/peeling bound, low density  $n_{ped} \sim 1.5 \cdot 10^{13} \text{ cm}^{-3}$
- Strong Shaping (right): QH operating point near kink/peeling bound, higher density QH operation possible,  $n_{ped} \sim 3 \cdot 10^{13} \text{ cm}^{-3}$
- Observed EHO during QH mode has poloidal magnetic signal qualitatively consistent with low- $n$  kink/peeling mode

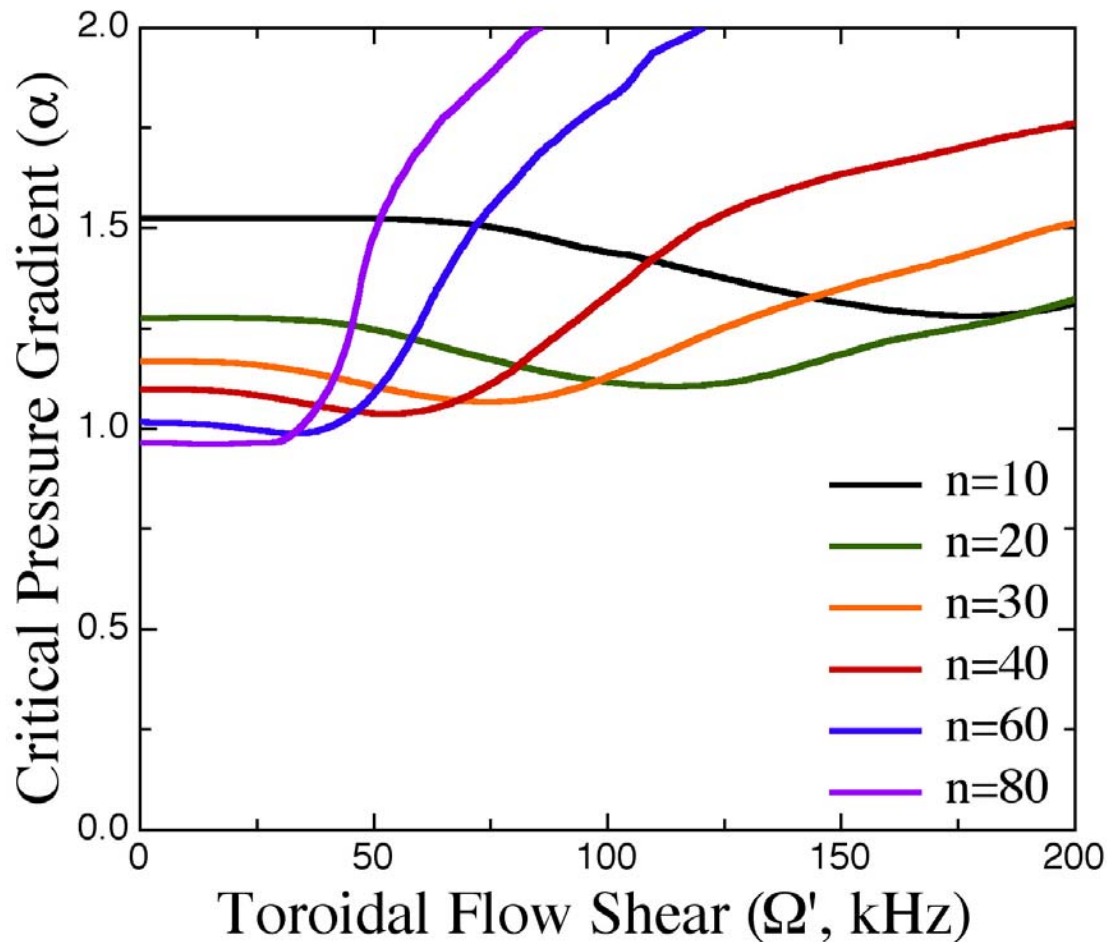
# Effect of Strong Toroidal Flow Shear in the Edge Region

- Eigenvalue formulation with rotation and compression derived and included in ELITE
  - Sheared rotation strongly damps high  $n$
  - weaker impact intermediate  $n$ , **can be destabilizing at low  $n$**
  - radial narrowing of mode structure
- Sheared flow stabilizes “ELRWM”
  - Allows plasma to reach ~ideal boundary, trigger rotating low- $n$  mode



# Effect of Strong Toroidal Flow Shear in the Edge Region

- Flow Shear Does Not Dramatically Impact Critical Gradient



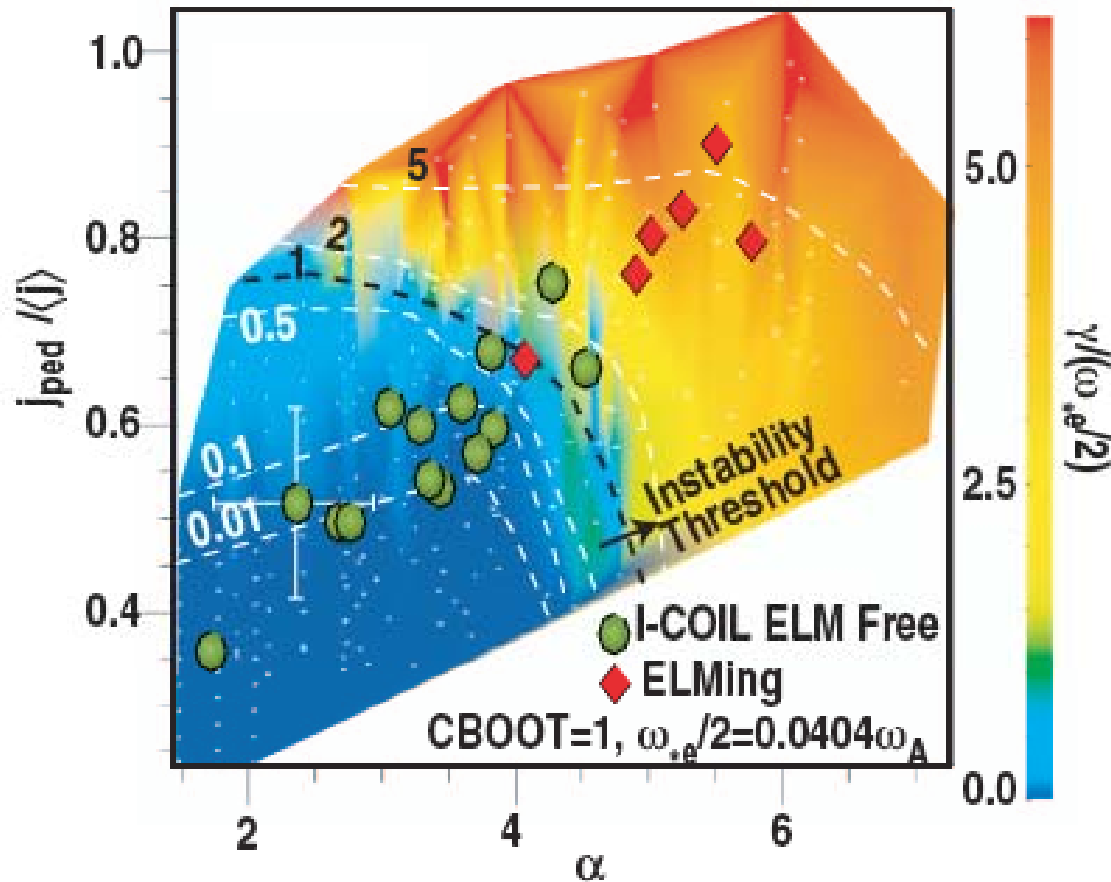
- Most unstable- $n$  decreases with flow shear (QH~50-120kHz)
- *Rotationally de-stabilized low- $n$  modes are limiting in QH regime*



# Hypothesis for QH Mode Mechanism

- **QH Mode exists in regime where low-n kink/peeling is limiting, due to low density, high bootstrap current**
- **Strong flow shear stabilizes “ELRWM” branch, leaves rotationally destabilized low-n “ideal” (with kinetic and diamagnetic corrections) rotating kink/peeling mode most unstable**
  - *This rotating mode is postulated to be the EHO*
- **As EHO grows to significant amplitude it couples to wall, damping rotation and damping its own drive**
  - Presence of the mode breaks axisymmetry, spreads strike point and stochasticizes surface -> more particle transport and more efficient pumping, allowing steady state density profile
  - $T_e$  profile is able to reach a transport steady state in low  $n_e$  regime
- **EHO saturates at finite amplitude, resulting in near steady-state in all key transport channels in the pedestal region**

# RMP ELM-free Discharges in Similar Regime



- **n=3 Resonant Magnetic Perturbations used to suppress ELMs in low density discharges**
- **ELM-suppressed shots in stable region, nearest kink/peeling boundary**
  - Increasing density causes ELMs to return
- **Propose that RMP plays the role of the EHO here**
  - Particle,  $T_e$ , rotation steady state
- **While EHO grows only to amplitude needed for steady state, RMP amplitude can be controlled**
  - Able to operate a factor of 2 below stability boundaries

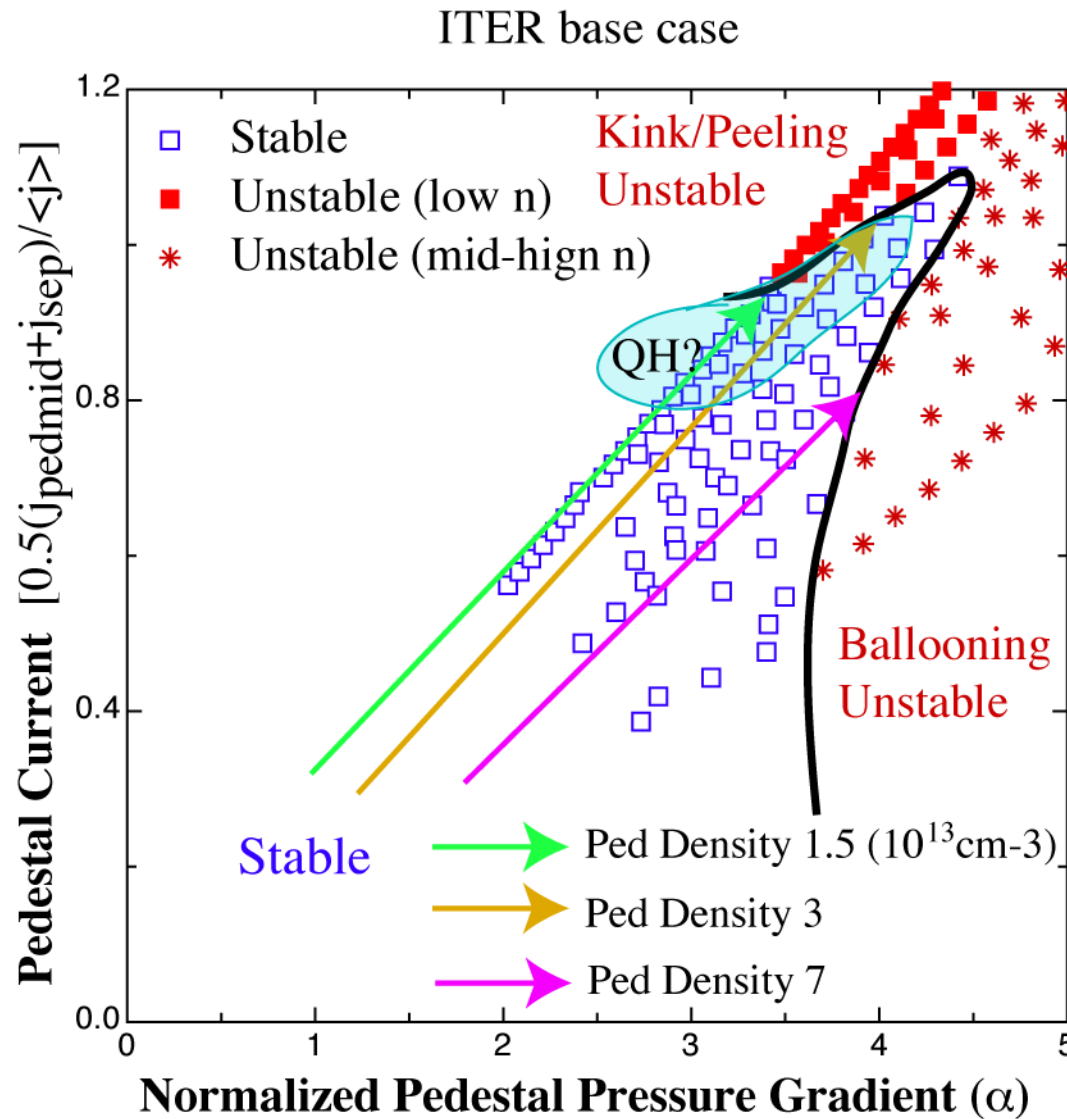
See T. Evans invited talk this afternoon

# Summary

- **Peeling-ballooning model has achieved a degree of success in explaining pedestal constraints, ELM onset and a number of ELM characteristics**
  - Nonlinear explosive growth of one or many filaments, similar to observations
  - Two prong model (conduits and barrier collapse) for ELM losses
- **Use same approach to study low density, ELM free, regimes**
- **Propose: QH exists in low-n kink/peeling limited regime**
  - Very low density required with moderate shaping, higher density and pressure possible with strong shaping
    - Agreement with observed QH density range
    - ITER study suggests QH regime for  $n_{\text{eped}} < \sim 4 \cdot 10^{19} \text{ cm}^{-3}$
- **Flow shear stabilizes ELRWM (and higher n), leaves low-n rotationally destabilized kink/peeling mode most unstable**
  - With kinetic corrections, this is the EHO
  - Saturates by damping rotation and providing particle transport
    - Essentially steady state operation in the key edge transport channels
- **Low density RMP ELM free discharges in similar regime**
  - Propose that RMP is playing the role of the EHO -> Controllable, can exist near or well below stability bound

# Extra Slides

# ITER Model Shows QH Regime May be Accessible at Low Density



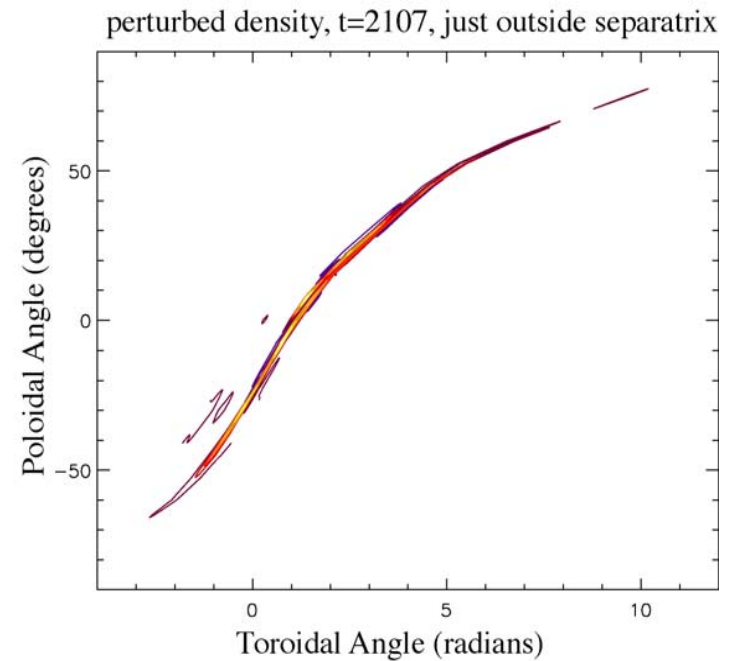
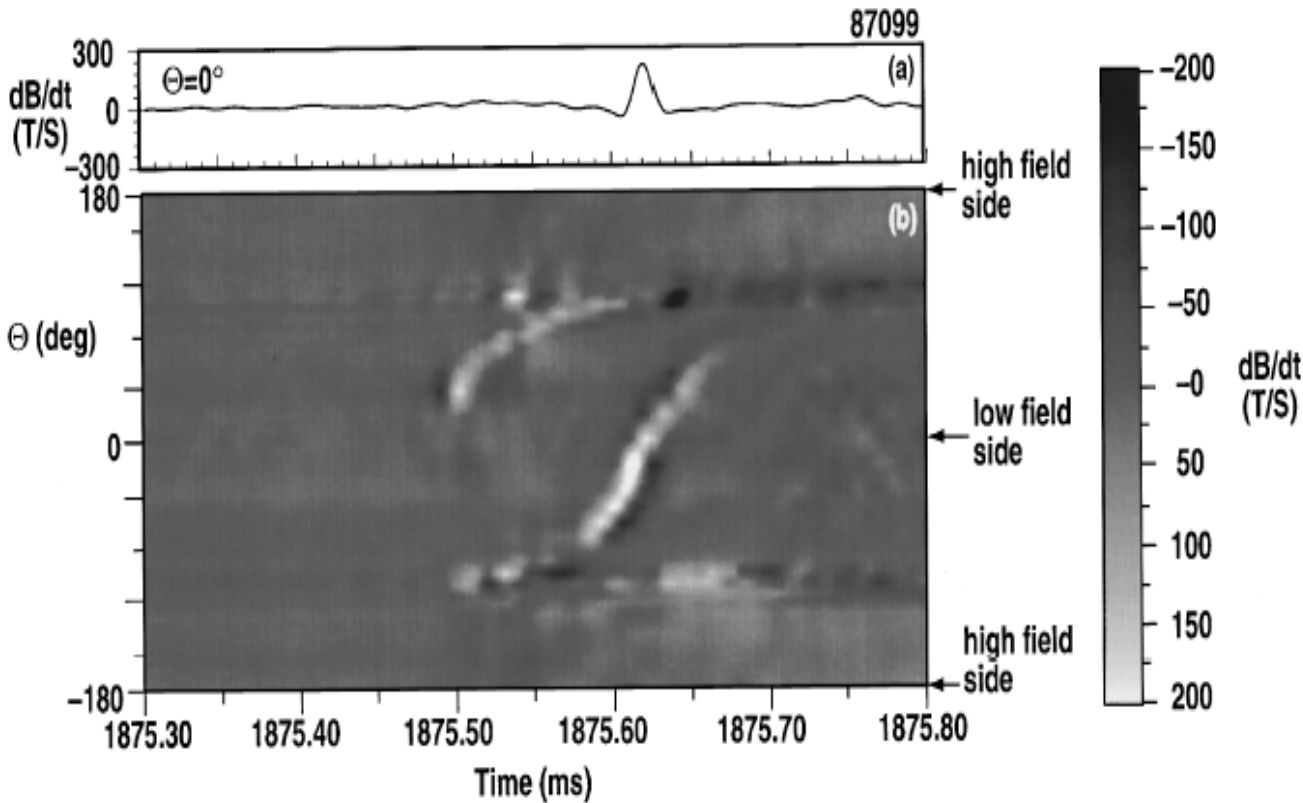
- ITER base case,  $R=6.2\text{m}$ ,  $a=2\text{m}$ ,  $B_t=5.3\text{T}$ ,  $I_p=15\text{MA}$
- Reference density  $\langle n_e \rangle = 10.1 \cdot 10^{19}\text{cm}^{-3}$ ,  $n_{\text{eped}} \sim 7 \cdot 10^{19}\text{cm}^{-3}$ 
  - High  $n$  ballooning limited at Ref density
- QH region for  $n_{\text{eped}} < \sim 4 \cdot 10^{19}\text{cm}^{-3}$ 
  - Worth exploring low density operation



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# Filaments Observed During ELMs



DIII-D Observation [E Strait, Phys Plas 1997]

3D Simulation

- Filament observed in fast magnetics during ELM (left)
- Finger-like structure from simulation (right) is extended along the magnetic field
- Qualitatively similar (rotation rate consistent with toroidal extent)