

# Core Measurements of Magnetic Fluctuation-Induced Particle and Momentum Flux in MST

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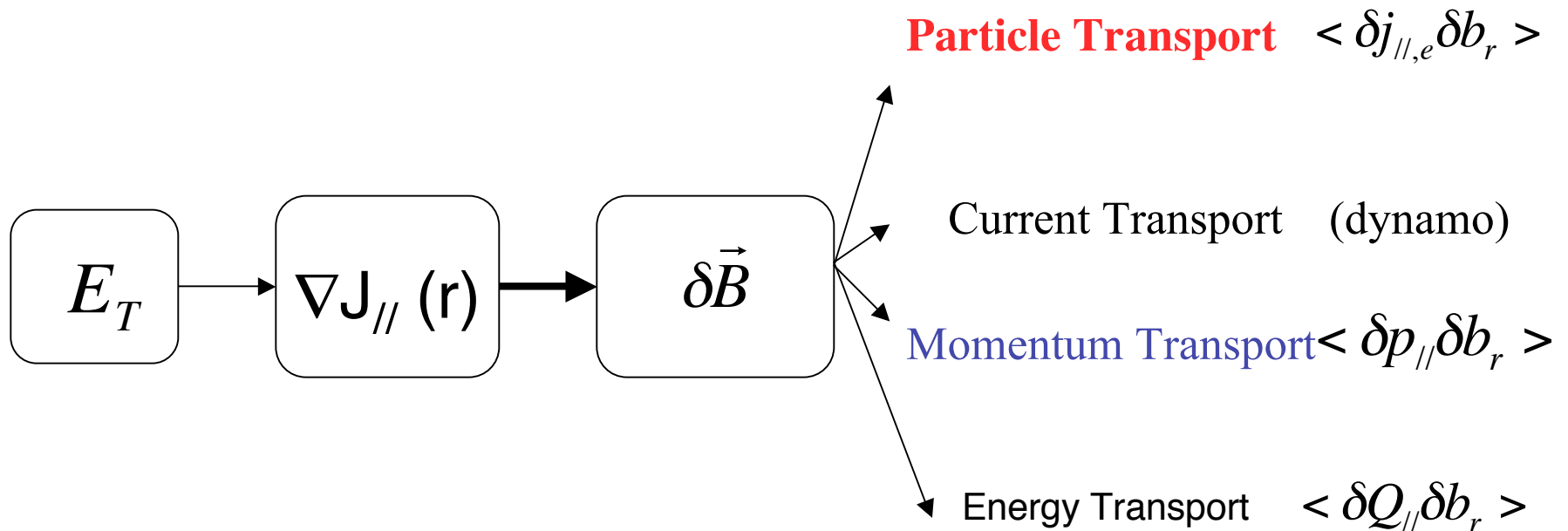
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12<sup>th</sup> TTF -2007 San Diego, CA Apr.19 ,2007

# Introduction

Magnetic fluctuations play an important role in particle and momentum transport in the laboratory plasmas

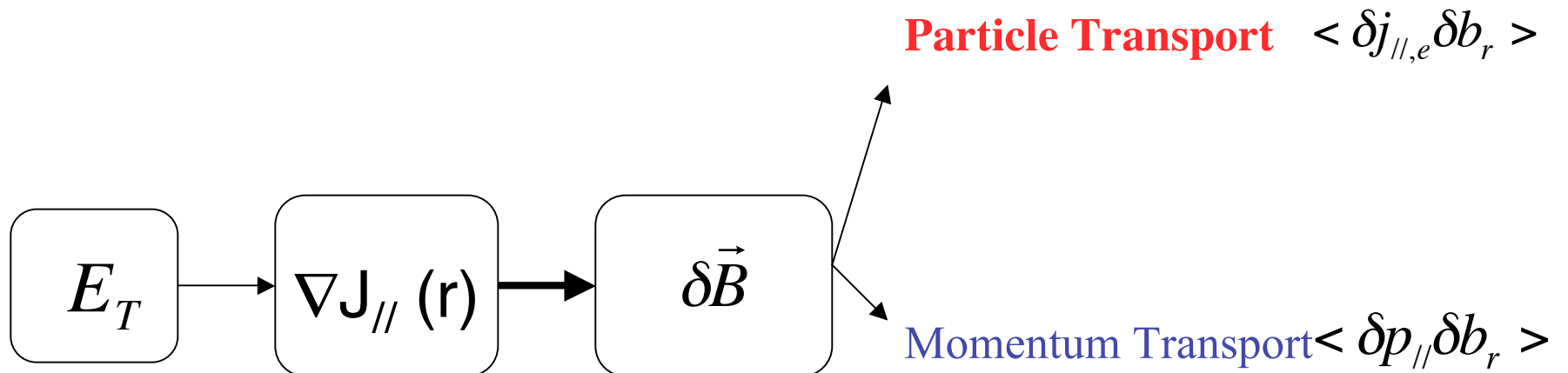


Transport also determines equilibrium dynamics

# Introduction

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Magnetic fluctuations play an important role in particle and momentum transport in the laboratory plasmas



Transport also determines equilibrium dynamics

# Outline

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(1) Measurement of density gradient fluctuation

$$\nabla \tilde{n}_e$$

(2) Measurement of particle transport by magnetic fluctuations

$$\frac{\langle \delta j_{\parallel, e} \delta b_r \rangle}{eB}$$

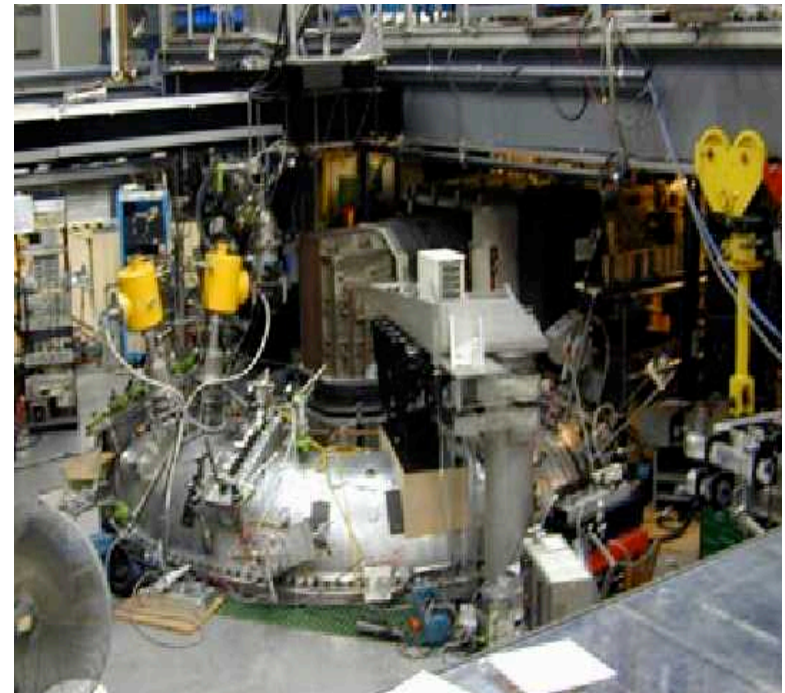
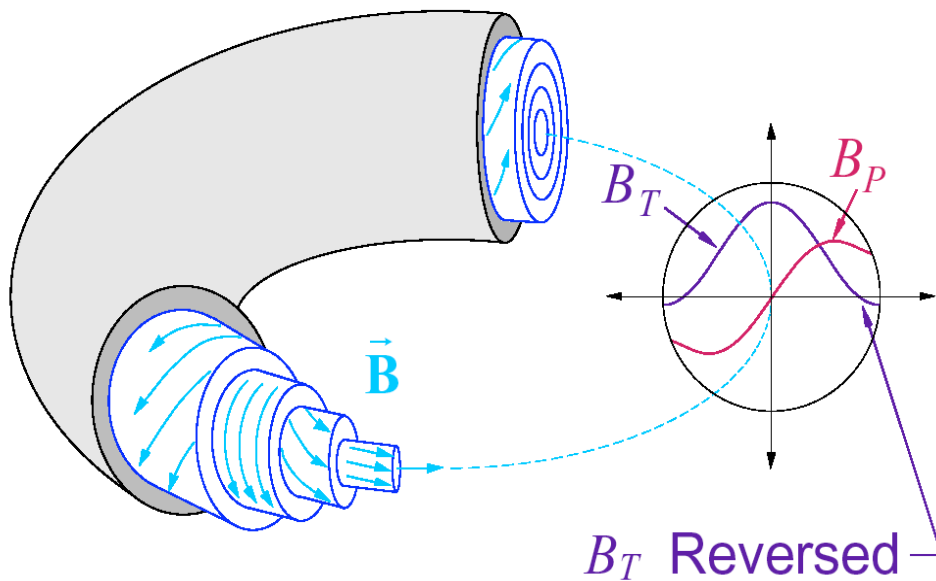
(3) Measurement of momentum transport (convective)

$$\frac{\langle \delta p_{\parallel, i} \delta b_r \rangle}{B}$$

*Identify the role of stochastic magnetic field in particle and momentum transport.*

# Madison Symmetric Torus

MST Reversed-Field Pinch (RFP) is toroidal configuration with relatively weak toroidal magnetic field  $B_T$  ( i.e.,  $B_T \sim B_p$  )



$$q(r) = \frac{r B_T}{R B_P} < 1$$

$R_0 = 1.5 \text{ m}$ ,  $a = 0.51 \text{ m}$ ,  $I_p < 600 \text{ kA}$ ,  $B_T \sim 3\text{-}4 \text{ kG}$ ,  
 $n_e \sim 10^{19} \text{ m}^{-3}$ ,  $T_{e0} < 1.3 \text{ keV}$ ,  $\beta = \langle p \rangle / B^2(a) = 15\%$

# Particle Balance Equation

$$\frac{\partial \langle n_e \rangle}{\partial t} + \nabla \cdot \Gamma_r = D_{\perp} \nabla^2 \langle n_e \rangle + \langle kn_0 n_e(r,t) \rangle$$

$$\Gamma_r = \Gamma_p^M + \Gamma_p^E + \Gamma^{Pinch} + \dots$$

Electrostatic fluctuations

Magnetic fluctuation induced particle flux

$$\nabla \cdot \Gamma_p^M = \nabla \cdot \left\langle \frac{\delta j_{\parallel,e} \delta b_r}{eB} \right\rangle = \underbrace{V_{\parallel,e} \nabla \cdot \left\langle \frac{\delta n \delta b_r}{B} \right\rangle}_{\text{convective particle flux}} + n \nabla \cdot \left\langle \frac{\delta V_{\parallel,e} \delta b_r}{B} \right\rangle_{\text{Conductive flux}}$$

$$j_{\parallel,e} = enV_{\parallel,e}$$

$B, \delta b_r$

*Faraday Rotation plus*

*Differential interferometer*

*Fizeau interferometer*

## Measurement of magnetic fluctuation and mean electron velocity by Faraday rotation

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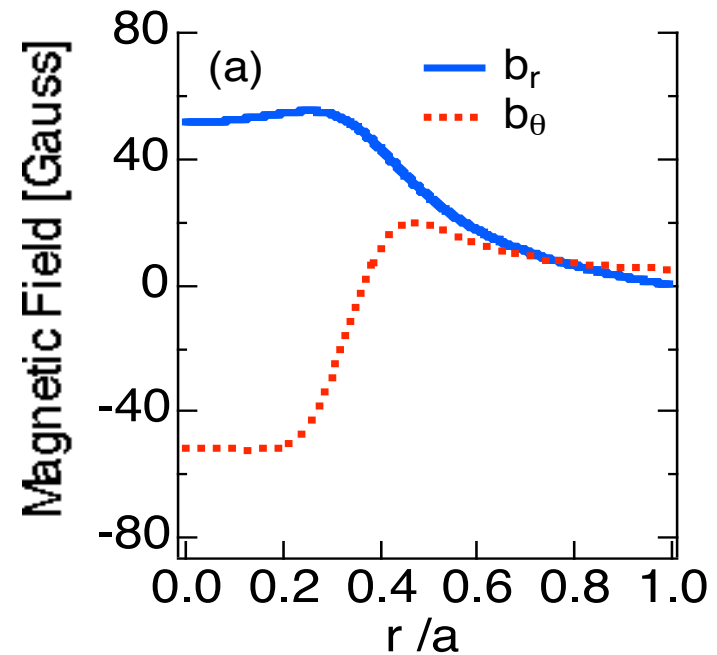
$$\nabla \cdot \Gamma_p^M = V_{\parallel,e} \nabla \frac{\langle \delta n \delta b_r \rangle}{B} = \frac{V_{\parallel,e}}{B} \langle (\nabla \delta n) \delta b_r \rangle + \frac{V_{\parallel,e}}{B} \langle (\delta n) \nabla \delta b_r \rangle$$

$\nabla b_r(0) \approx 0$  ,  $\delta n(0) = 0$

## Measurement of magnetic fluctuation and mean electron velocity by Faraday rotation

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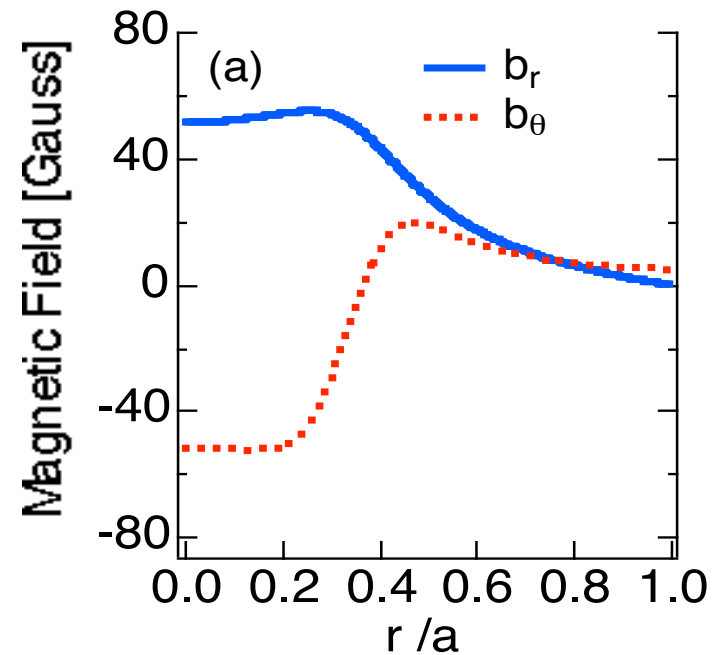
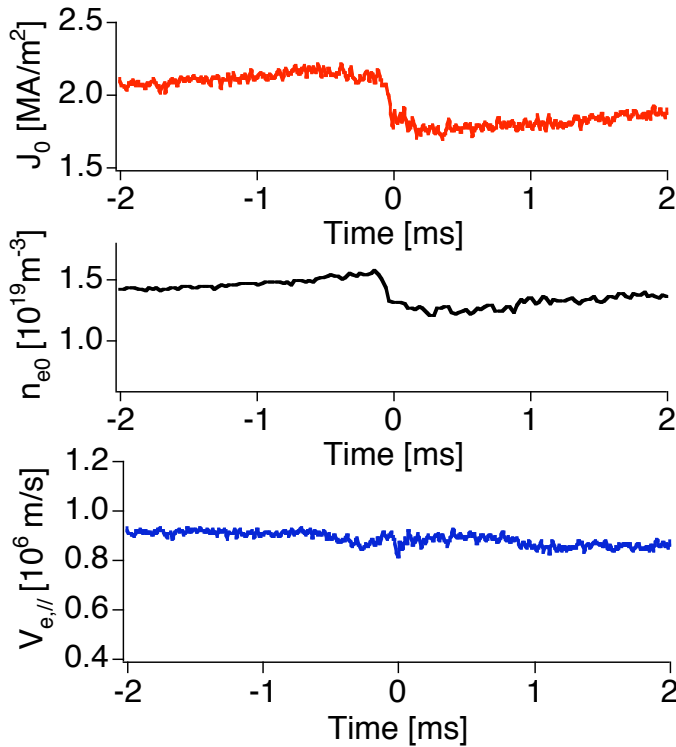


# Measurement of magnetic fluctuation and mean electron velocity by Faraday rotation

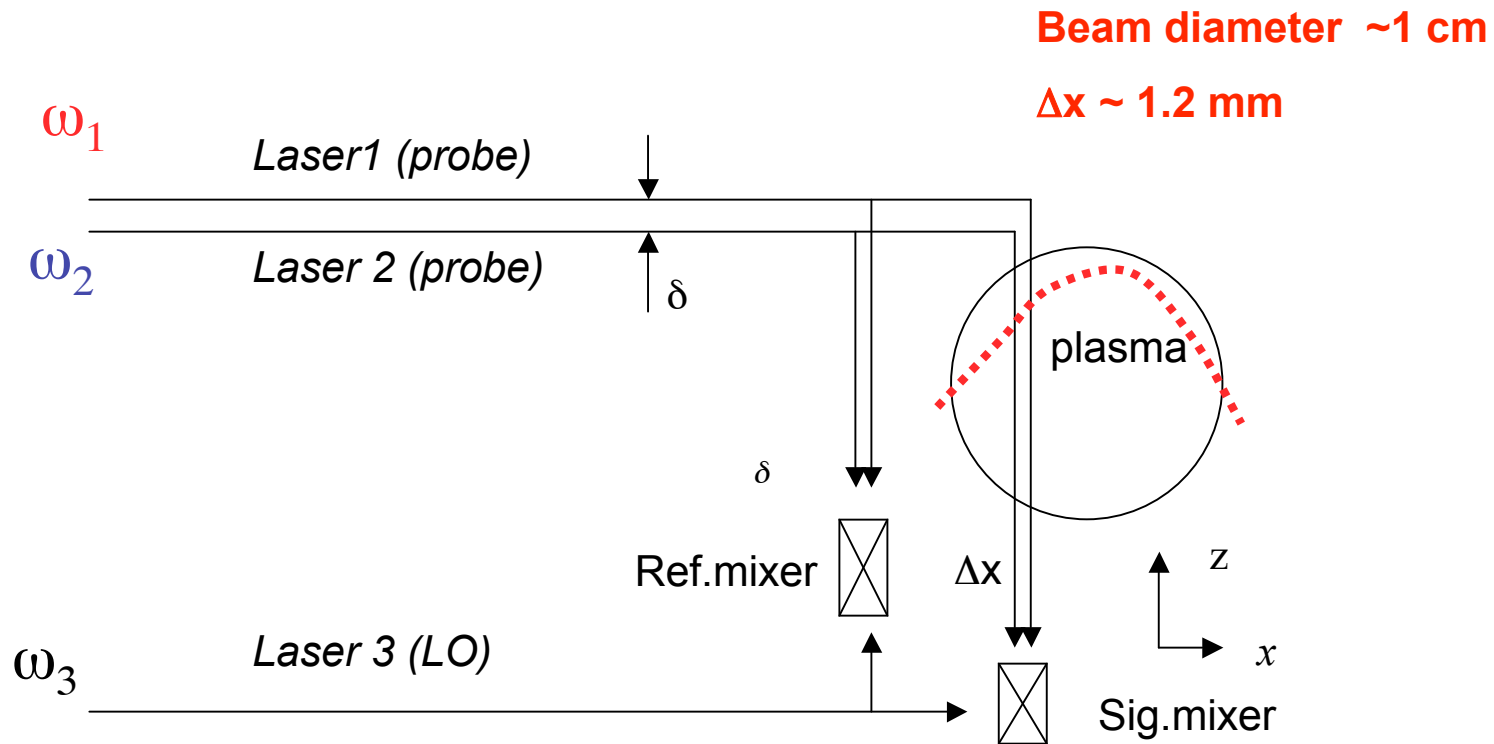
$$\nabla \cdot \Gamma_p^M = V_{\parallel,e} \nabla \frac{\langle \delta n \delta b_r \rangle}{B} = \frac{V_{\parallel,e}}{B} \langle (\nabla \delta n) \delta b_r \rangle + \frac{V_{\parallel,e}}{B} \langle (\delta n) \nabla \delta b_r \rangle$$

$\nabla b_r(0) \approx 0, \delta n(0) = 0$

$$V_{\parallel,e} = \frac{J_0}{en_{e0}}$$



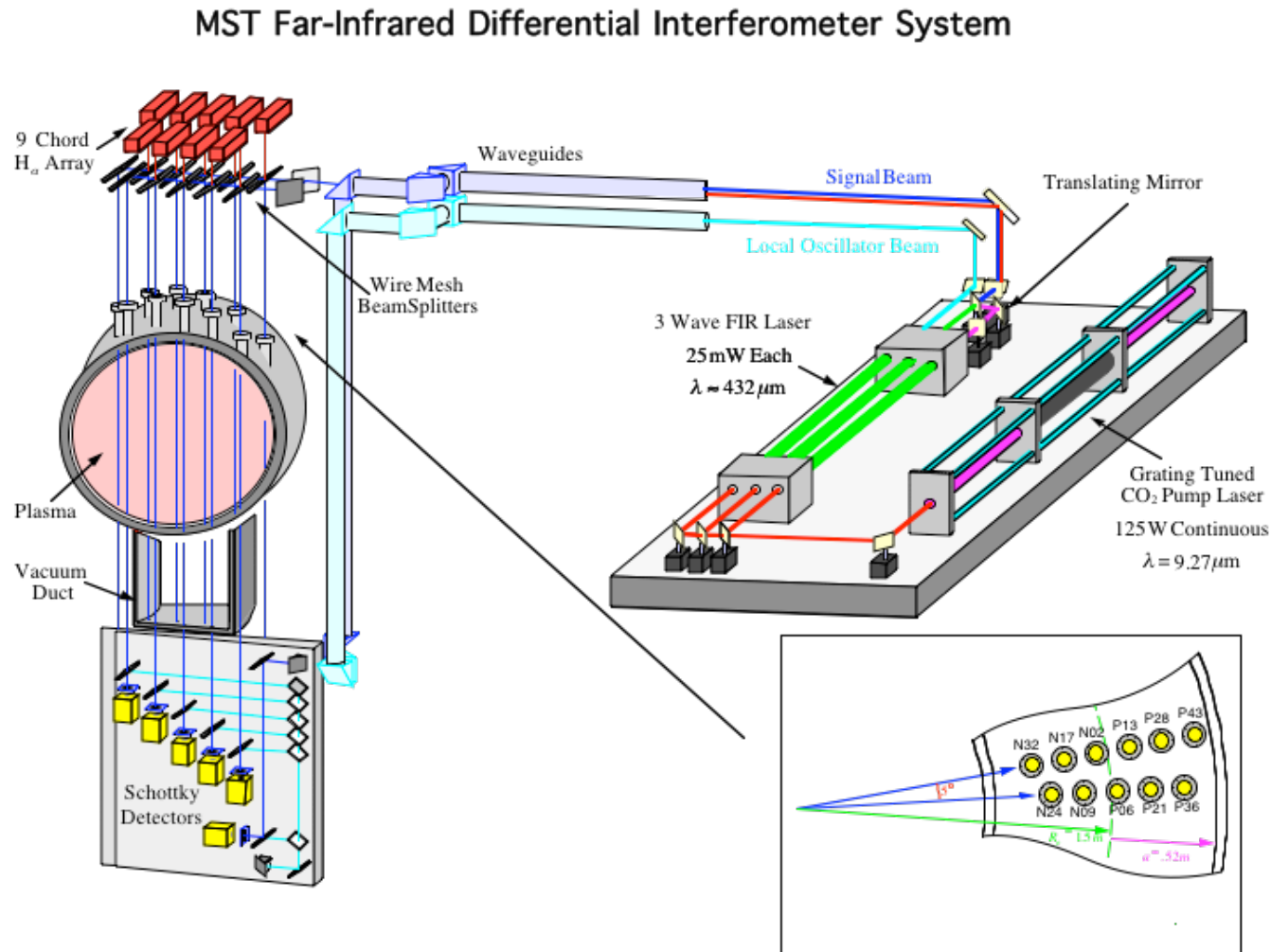
# $\nabla \delta n$ measurement by a new differential interferometer



$$\omega_1 - \omega_2 \rightarrow \Delta\phi(x) = \int_{x_1} n dl - \int_{x_2} n dl$$

*Differential Interferometer measures phase between closely-spaced laser beams*

# FIR Differential Interferometer System



11 chords differential  
interferometer

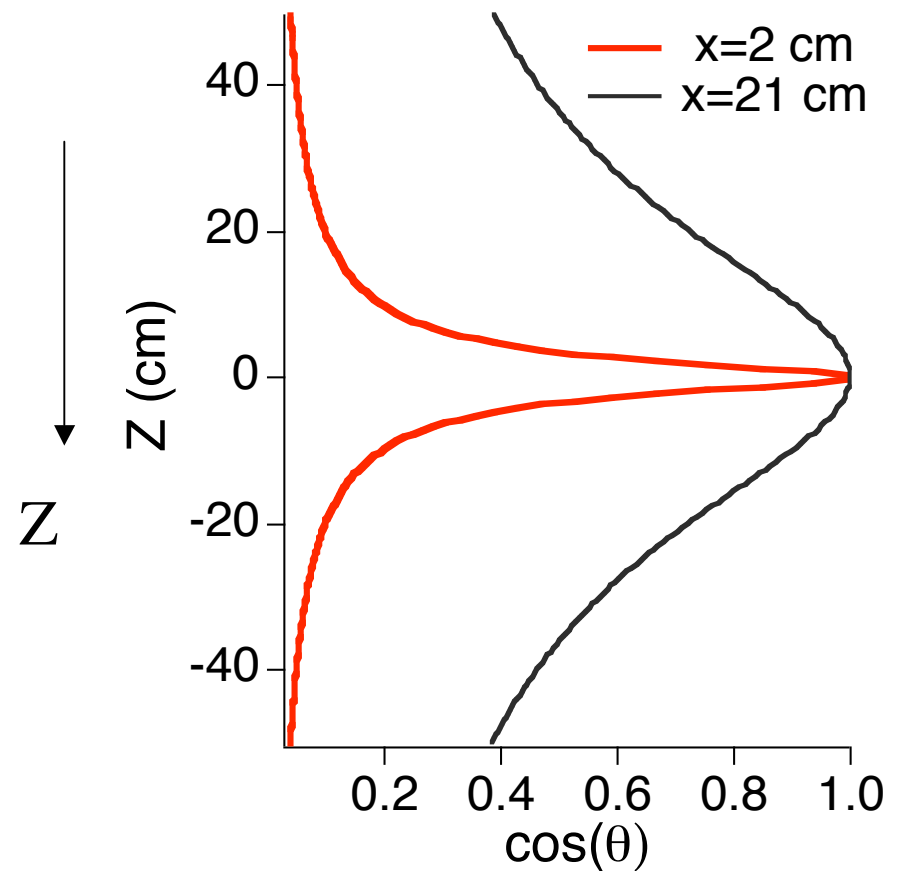
# Localization of Density Gradient Fluctuations

For dominate  $m=1$  mode

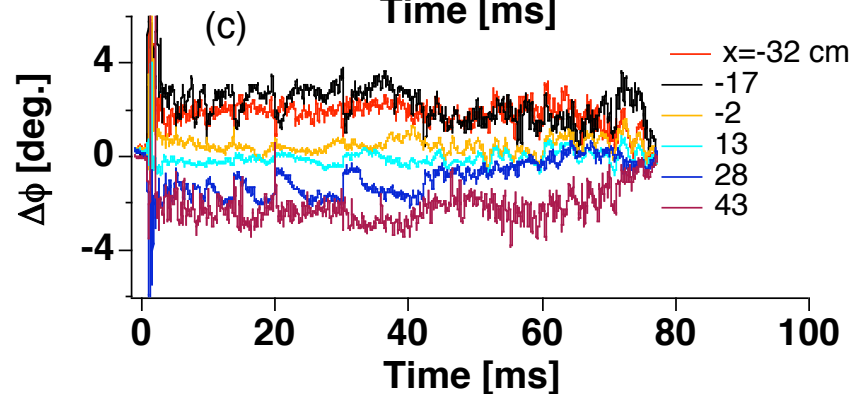
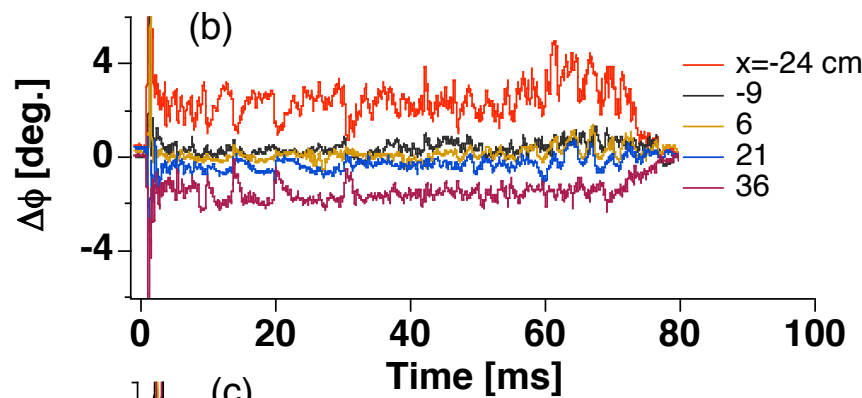
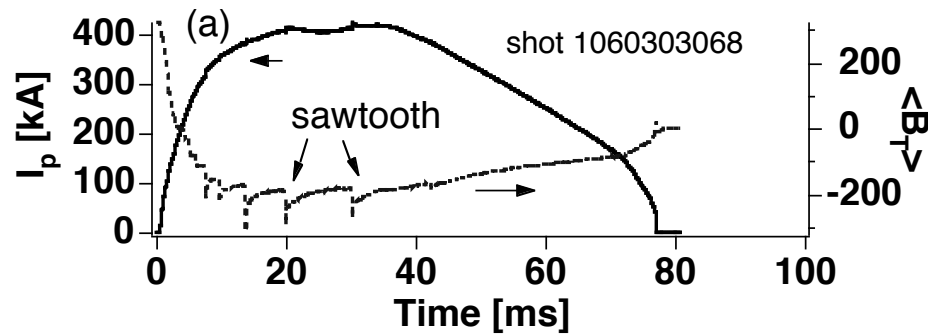
$$\tilde{\phi} = \int \delta n(r) \cos \theta dz$$

$$\left. \frac{\partial \tilde{n}(r)}{\partial r} \right|_{r=0} = \frac{\partial}{\partial x} \tilde{\phi}(x) = \frac{\Delta \tilde{\phi}(x)}{\Delta x}$$

See poster , P48(ding)



# Time History of Differential Interferometer

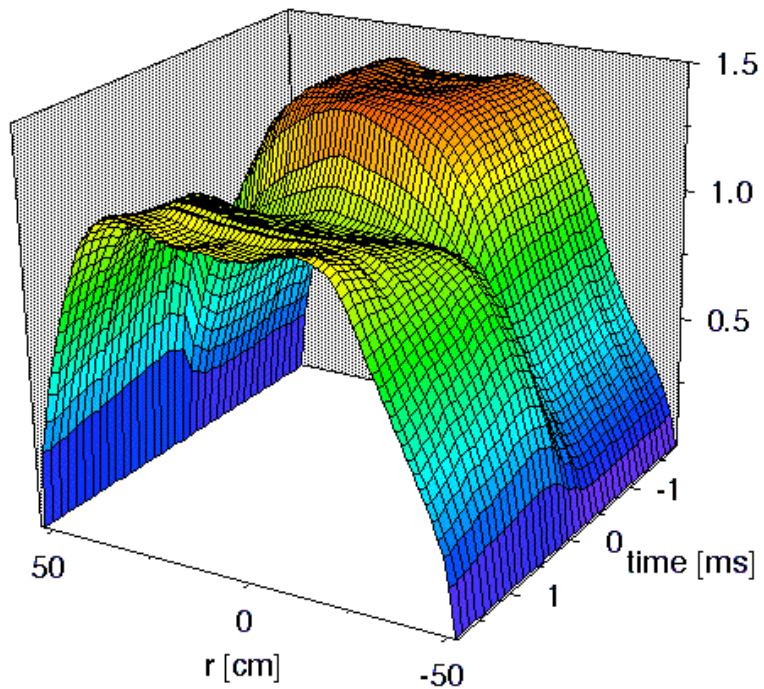


*Ensemble average  $\langle \frac{\Delta\tilde{\phi}}{\Delta x} \delta b_r \rangle$   
over multiple sawtooth  
events*

# Density Change and Convective Particle Flux

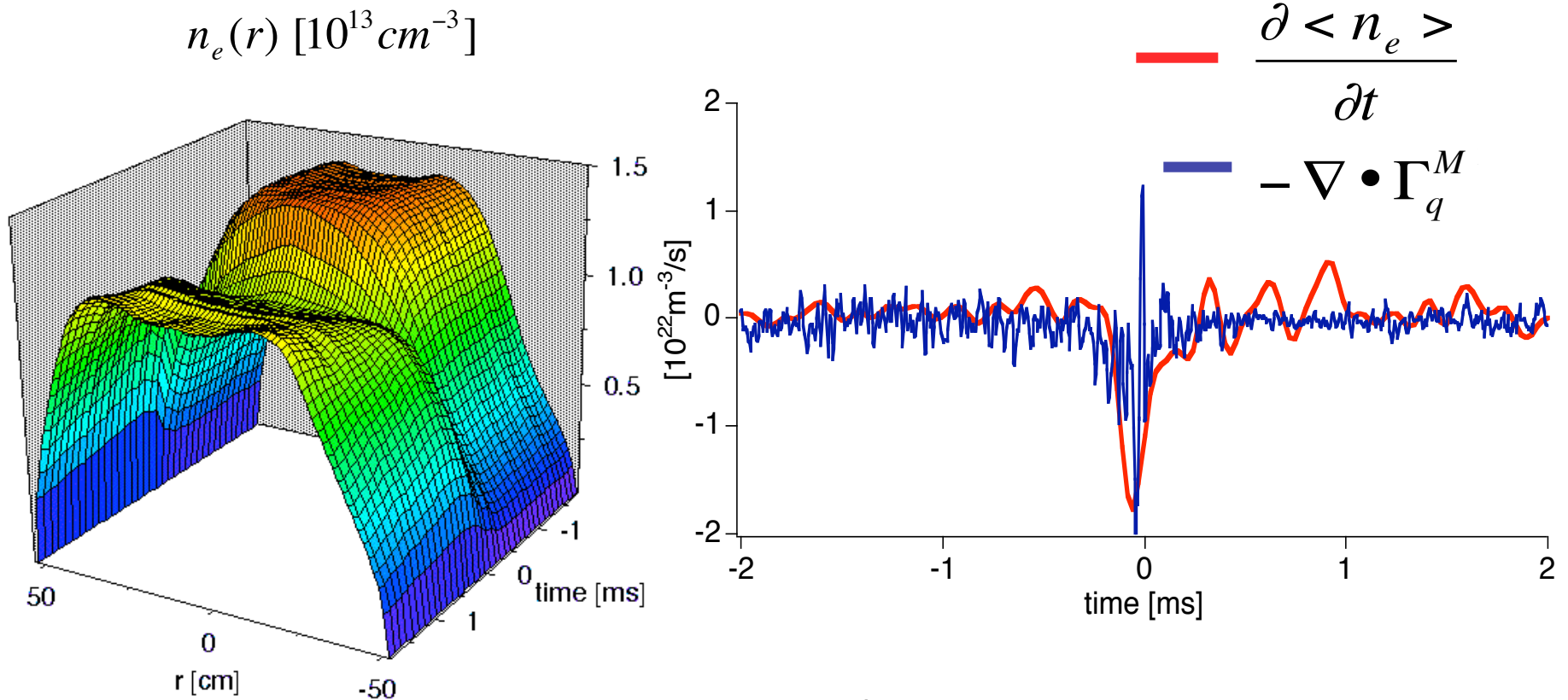
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$$n_e(r) [10^{13} \text{ cm}^{-3}]$$



*Density redistributes  
within  $300 \mu\text{s}$*

# Density Change and Convective Particle Flux



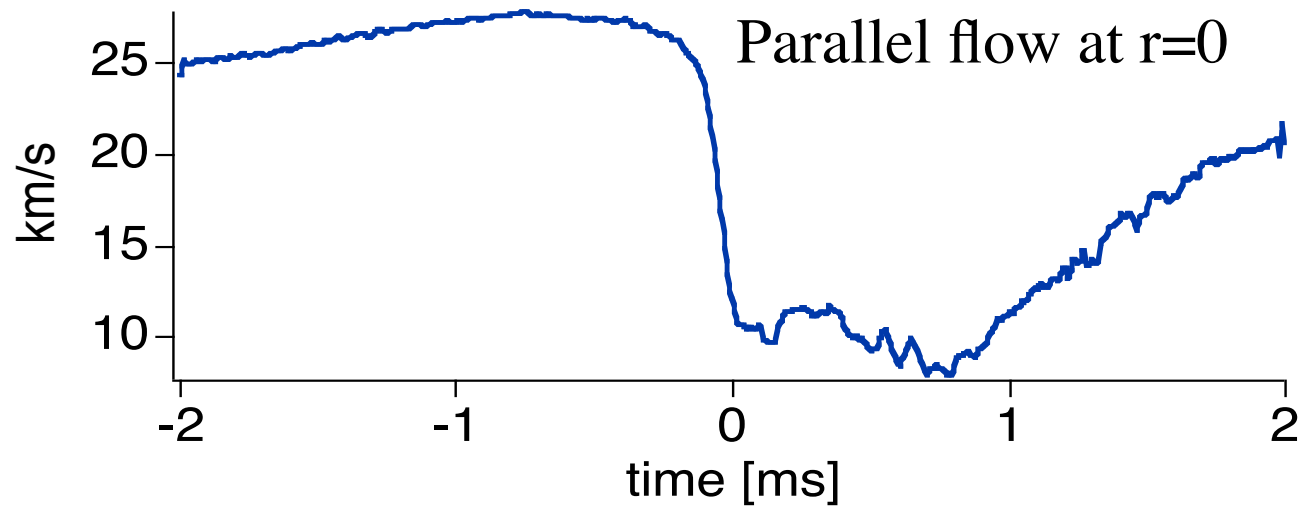
*Density redistributes  
within 300  $\mu\text{s}$*

$$\frac{\partial \langle n_e \rangle}{\partial t} + \nabla \cdot \Gamma_q^M \approx 0$$

*Density change is balanced by the convective particle transport*

# Momentum dynamics

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*Parallel momentum changes much faster than classical dissipation*



# Parallel Momentum Balance

$$\frac{\partial}{\partial t} \langle \rho V_{\parallel} \rangle + \nabla \cdot \Gamma_p = v_{\parallel} \nabla^2 \langle \rho V_{\parallel} \rangle + M(r,t) \text{ (other momentum sources)}$$

See Poster P54 (Kuritsyn)

Fluctuation induced momentum flux

$$\Gamma_q = \Gamma_q^M + \Gamma_q^E \leftarrow \text{Electrostatics fluctuations}$$



Magnetic fluctuations

$$\nabla \cdot \Gamma_q^M = \nabla \cdot \left\langle \frac{\delta p_{\parallel} \delta b_r}{B} \right\rangle = T_{\parallel} \nabla \cdot \left\langle \frac{\delta n \delta b_r}{B} \right\rangle + n \nabla \cdot \left\langle \frac{\delta T_{\parallel} \delta b_r}{B} \right\rangle$$

convective momentum flux

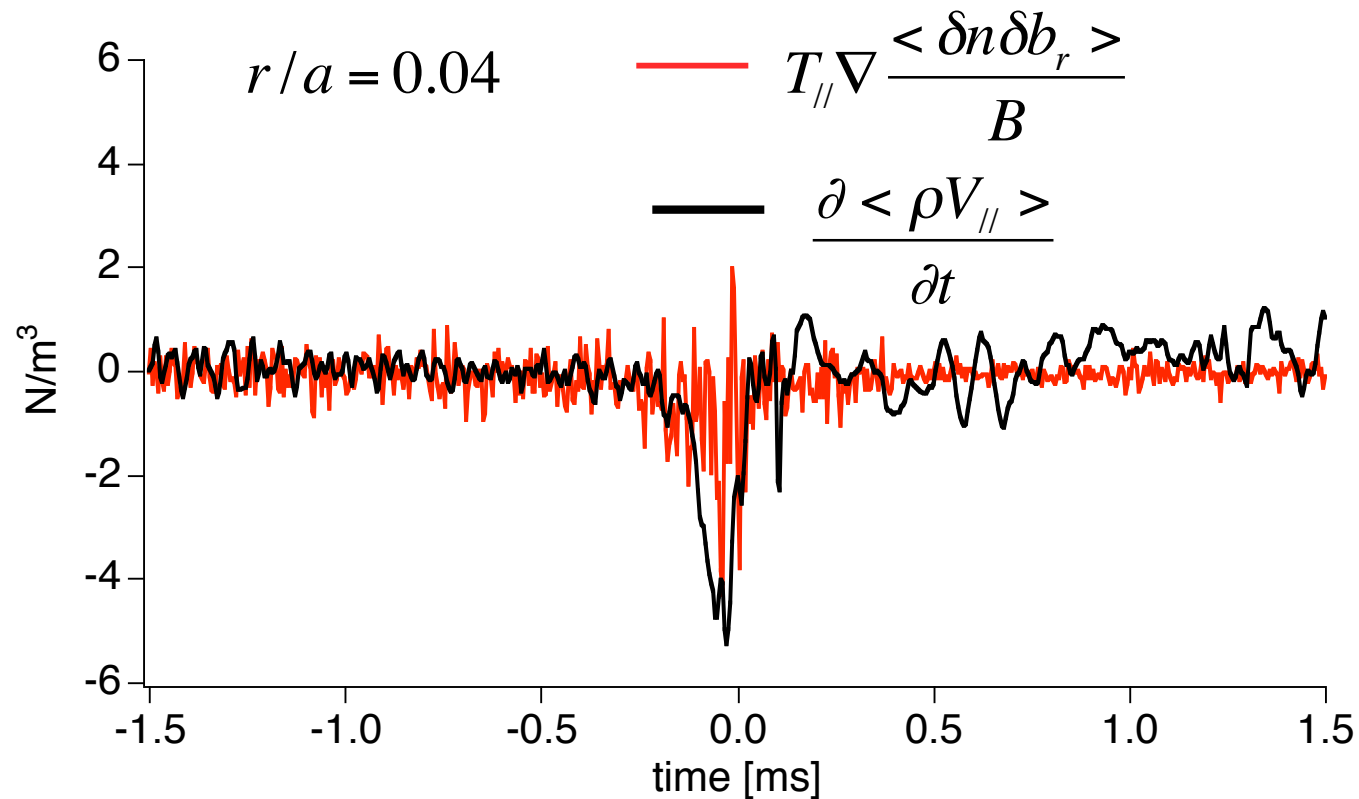
Conductive momentum flux

$$\frac{T_{\parallel}}{V_{\parallel,e}} \nabla \cdot \Gamma_p^M$$

Particle flux

# Magnetic momentum flux and parallel momentum change

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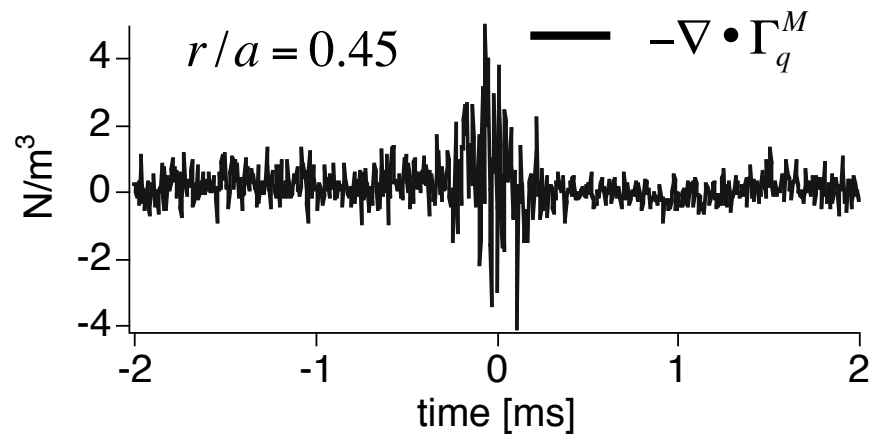
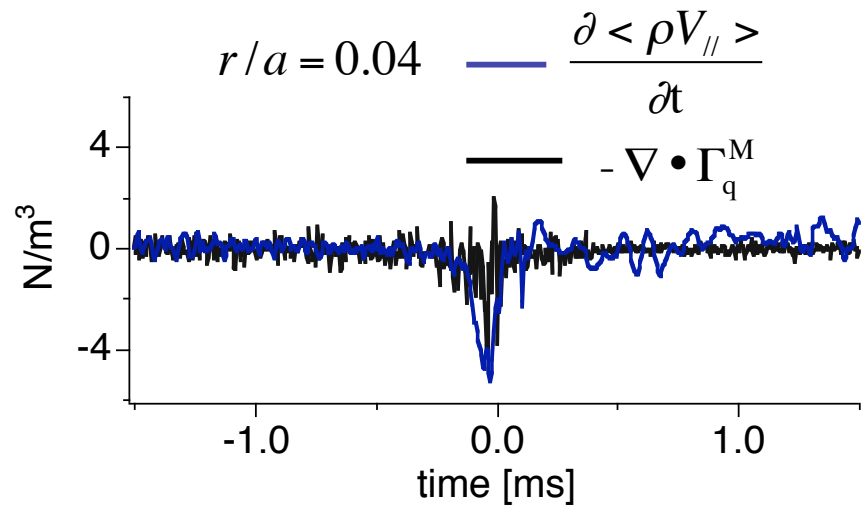


$$\frac{\partial \langle \rho V_{||} \rangle}{\partial t} + T_{||} \nabla \frac{\langle \delta n \delta b_r \rangle}{B} \approx 0$$

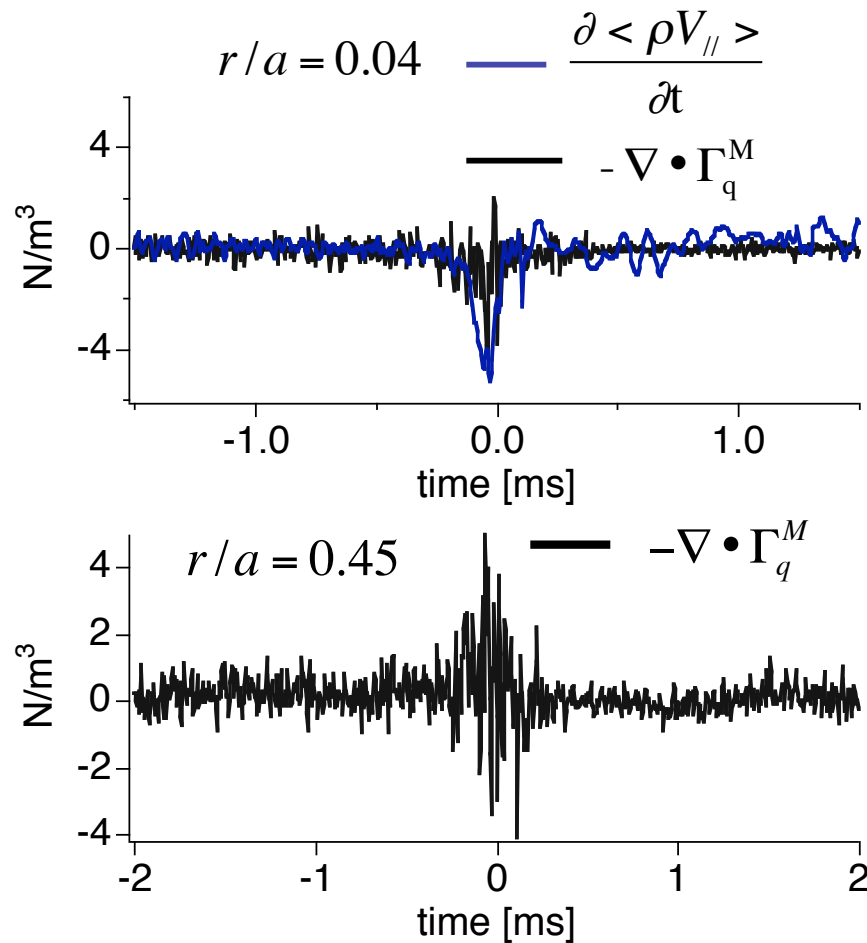
*Momentum flux significantly contributes to parallel momentum change*

# Momentum flux changes direction away from magnetic axis

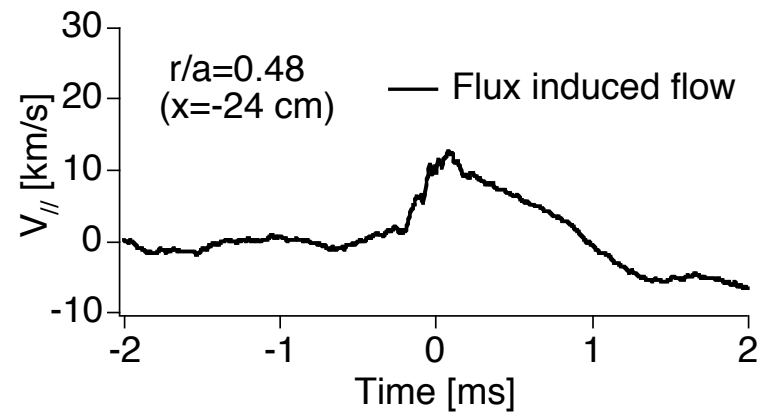
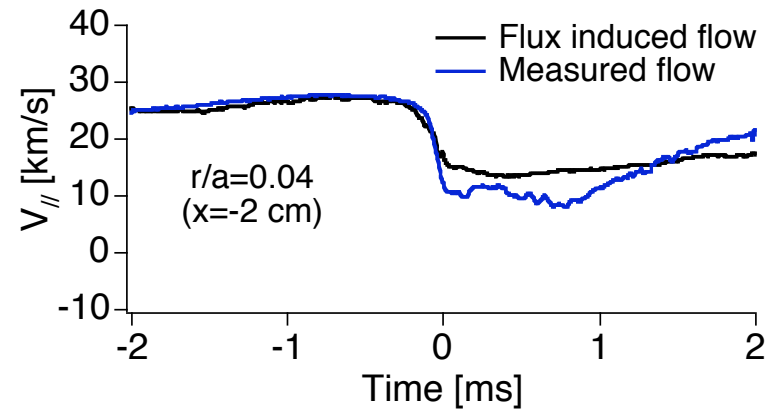
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# Momentum flux changes direction away from magnetic axis



$$V_{\parallel} = \int (\nabla \cdot \Gamma_q^M) dt + V_0(t = -2ms)$$



*The change of direction is consistent with momentum transport instead of total momentum loss*

# Summary

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- (1) Convective particle transport due to stochastic magnetic field has been measured by differential interferometer and Faraday rotation
- (2) Magnetic particle flux can account for the change of density on magnetic axis
- (3) Magnetic momentum flux significantly contributes to the change of parallel momentum in the core

*Relevant poster: P48(ding), P100 (Brower), P54(Kuritsyn), P52(Ebrahimi)*