

Pedestals and Confinement

R.E. Waltz

Global confinement is highly dependent on the pedestal height

- If the core confinement is “stiff, global confinement is highly dependent on the H-mode pedestal temperature, T_{ped} . What does “stiff” mean?
- The core is “perfectly stiff”, if $T(0)$ is linear with T_{ped} and independent of power P_{ped} .
- The theoretical core transport models in standard use, GLF23 and Multi-Mode, are **not perfectly stiff**, but Multi-Mode has some stiffness $T(0) \propto T_{ped}^{0.3}$ and GLF23 is very stiff $T(0) \propto T_{ped}^{0.7}$
- While the core theoretical transport models can predict global confinement time to better than 10% given T_{ped} , empirical statistical scaling models for T_{ped} are typically 30%. Hence for very stiff models the combination likely has less predictability for confinement time than global τ_E scaling laws, typically 15%.
- For very stiff models Q can be uncertain by 50%, and predicting the H-mode pedestal heights is the focus of our uncertainty in predicting BPX performance.

Core Transport Models

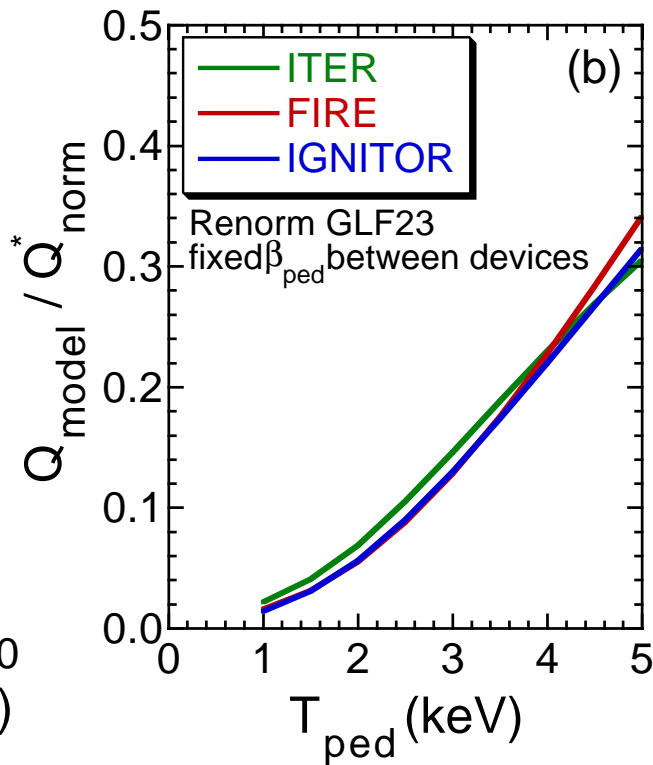
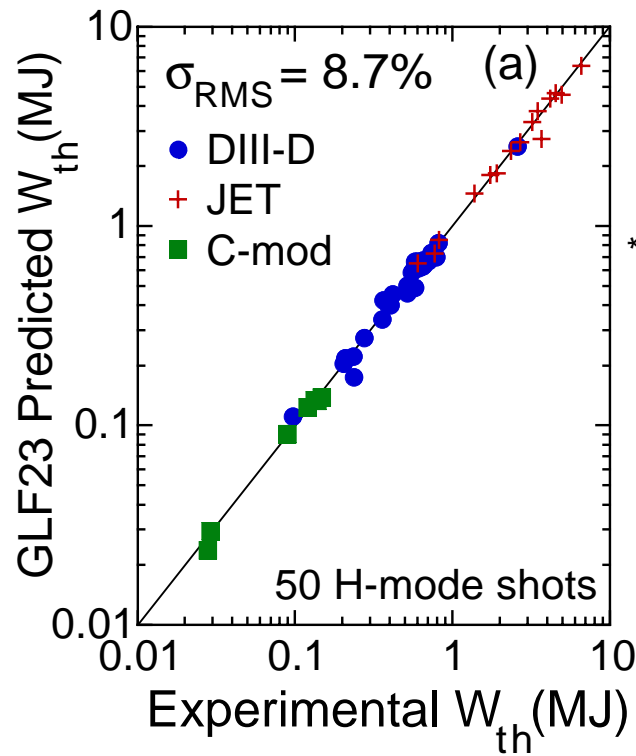
- The past decade has seen considerable progress in understanding of core transport and development of theoretical core transport models.
 - The focus has been on two comprehensive models: **GLF23renorm** and **MutiMode**
 - These theoretical drift wave based models with ExB shear stabilization have been very successful in matching the ITER profile data L- and H-mode database **given the pedestal temperature and density**, and in describing internal transport barriers.
 - **GLF23renorm** is fit to gyrokinetic linear stability and nonlinear simulations taking nothing from data, yet predicts core stored energy with RMS 8.7%.
 - **MultiMode** has similarly good fit statistics.

- (a) GLF23renorm comparison with H-mode data

- (b) model Q/Q_{norm} vs T_{ped}

$$Q_{\text{norm}} = \kappa R (I/a)^2 (n_{\text{ped}}/n_G)^2 (n_i/n_e)^2 (n_e/n_{\text{ped}})^{1.5} C_{\text{RLT}}/P_{\text{aux}}$$

$$\text{with } C_{\text{RLT}} = \exp[2(2.0 + .004P_{\text{net}})/(R/a) + 0.5(1 - n_i/n_e)]$$



(see Kinsey Sherwood talk)

Core Transport Models (cont'd)

- While both models have similar ITG and trapped electron physics and comparable RMSE fits to data, they not only have quantitatively, but qualitatively, different Q –projections.
- While GLF23renorm is **not as stiff** as IFS-PPPL and '96GLF23, it is **still very stiff** with Q having nearly inverse P_aux dependence. Approximatedly:

$$Q \propto \text{Volume } n_{\text{ped}}^2 T_{\text{ped}}^2 / P_{\text{aux}} \quad (\text{see Kinsey Sherwood talk})$$

- This means Q can be doubled by halving P_aux required to get into H-mode, and P_fus is insensitive to P_aux.

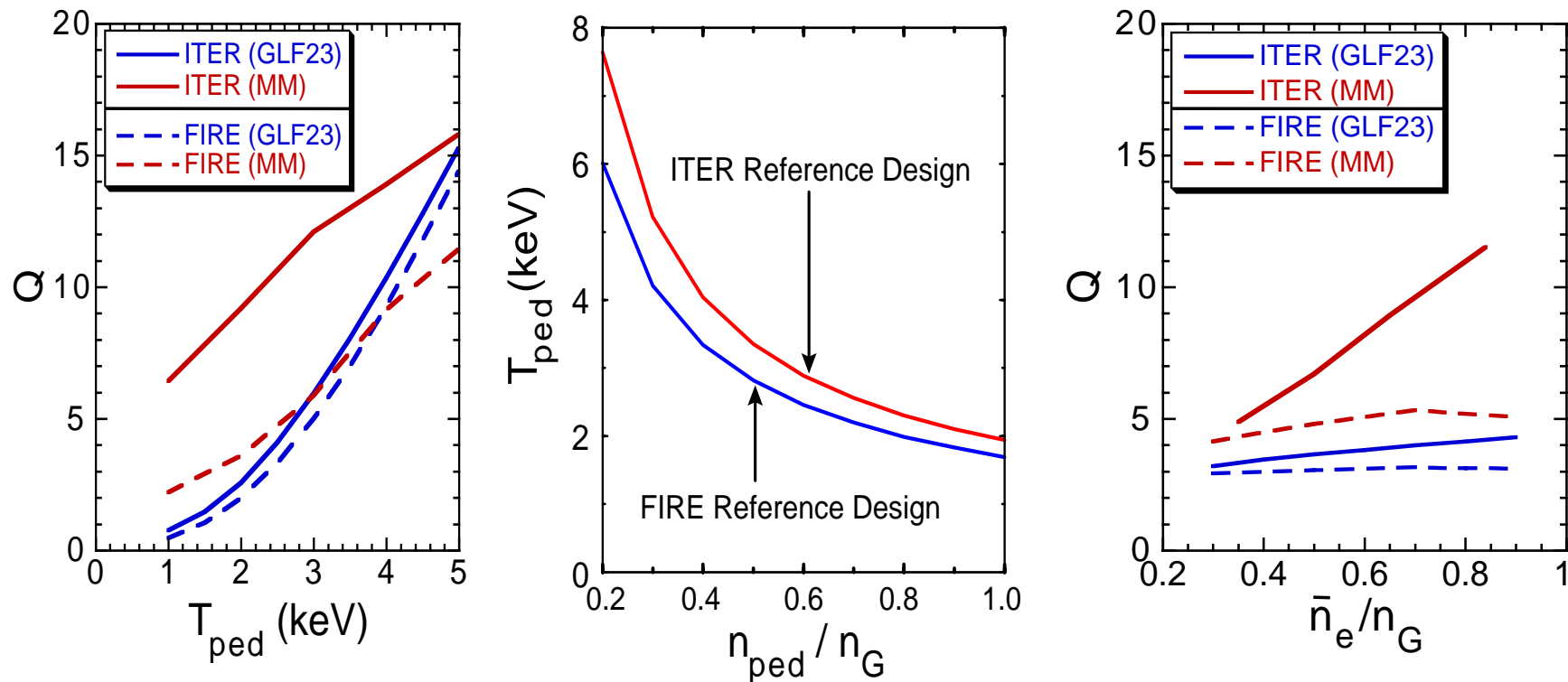
- Since (as we will discuss), the projected $T_{\text{ped}} \propto 1 / n_{\text{ped}}$, Q depends weakly on $n_{\text{ped}} / n_{\text{Greenwald}}$, and pedestal projections should focus on predicting maximum

$$p_{\text{ped}} \quad \text{or better} \quad \text{beta_norm_ped} = \text{beta_ped} / (I / aB)$$

- MultiMode as is **much less stiff** with $Q \propto \text{Volume } n_{\text{ped}}^2 T_{\text{ped}} / P_{\text{aux}}^{0.25}$

Core Transport Models (cont'd)

- Examples GLF23 / MM with Onjun-Bateman et al T_{ped} Model



* Kinsey, Onjun, Batman, et al

Core Transport Models (cont'd)

- Thus core transport model **stiffness** is a key issue, but we shouldn't need a BPX to resolve this difference.
- $W_{\text{tot}} / W_{\text{ped}} \propto P^s$ roughly: **GLF23renorm**: $s = 0.1$, **MultiMode**: $s = 0.2$
- Remarkably, ITER database statistical free fits over all data machine says

$W_{\text{tot}} \propto P^{0.31}$ and $W_{\text{ped}} \propto P^{0.31}$ suggesting **perfect stiffness**, i.e. $s=0$. m. 0.05
(recent *Thomsen, Cordey et al paper*)

- Precise controlled single machine P scaling data or new experiments should be able to distinguish between $s=0.1$ and $s=0.2$

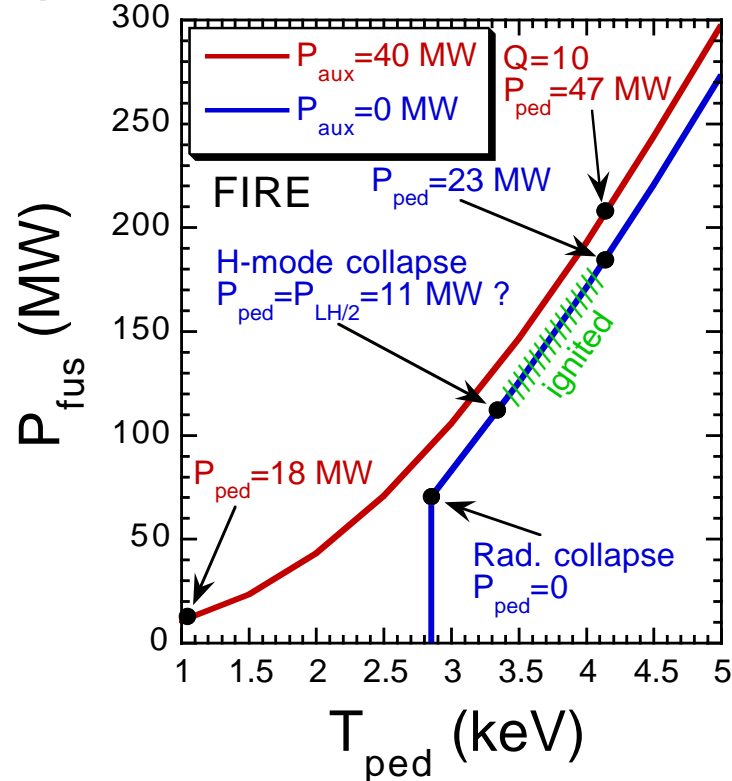
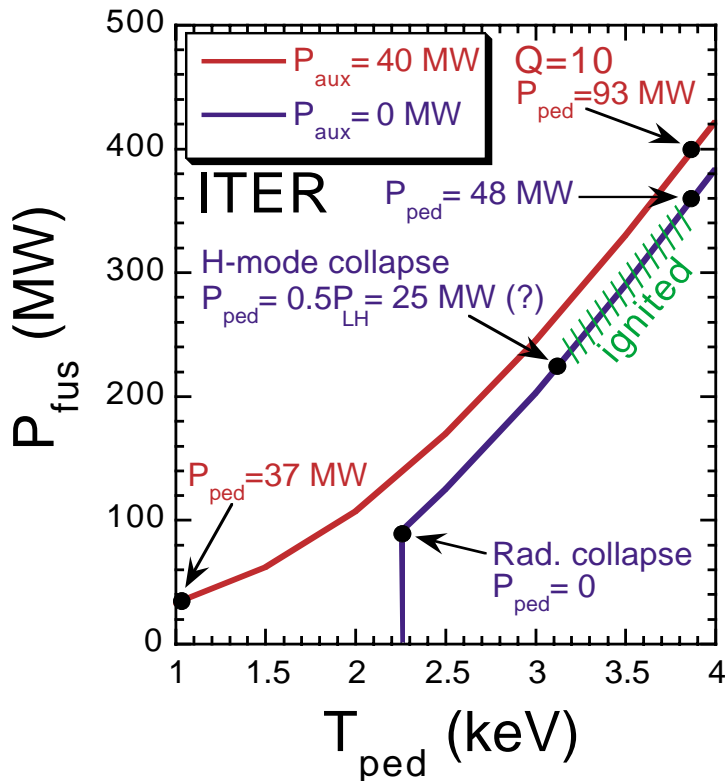
Core Transport Models (cont'd)

- Stiff cores are magical for getting high Q ...even ignition Q = infinity with $P_{aux} = 0$!!!!

If there is enough power flow P_{ped} to maintain the pedestal temperature T_{ped}

- $P_{fus} = 5 P_{\alpha}$; $Q = P_{fus}/P_{aux}$;

$$P_{ped} = P_{\alpha} - P_{brem} + P_{aux} > 1/2 P_{LH}$$



- We need to know power dependence (σ) for $T_{ped} = T_{ped_LH} (P_{ped} / P_{LH})^{\sigma}$

H-mode Pedestal Height

- Although we have some understanding of how T_{ped} is determined, we don't have theoretical models. Projected T_{ped} is largely based on statistical empirical fits.

- The "best" fits to all machine data are characterized by an RMS of 27%.

- If core transport model projections are perfect, and $Q \propto T_{ped}^2$, then

$$Q = 5 \quad \text{is really} \quad 2.65 < Q < 8.10$$

$$Q = 10 \quad \quad \quad 5.3 < Q < 16.2$$

- Approaches to finding the pedestal height:

- Free statistical fit: $W_{ped} = 3 p_{ped} \text{Volume}$ (e.g. *Thomsen, Cordey et al paper* *)

$$W_{ped} = e^{-3.74} I^{1.71} R^{1.16} p^{0.31} M^{0.30} q_{sh}^{1.20} \quad \text{RMS} = 25.4\% \quad *$$

- Stat. fit of $width_{ped}$ with approx. high-n MHD stability gradient constraint p^0

$$p_{ped} = width_{ped} [dp/dr]_{crit} \quad \text{e.g.} \quad width_{ped} \propto \rho_{pol}^{0.23} R^{0.77}$$

$$W_{ped} = e^{-4.61} I^2 R [M/nR]^{0.13} q_{sh}^{1.20} [a/R]^{-1.68} \quad \text{RMS} = 27.3\% \quad *$$

or $width_{ped} \propto \beta_{pol}^{0.5} R^{1.0}$ is a popular choice suggested by DIII-D data.

H-mode Pedestal Height (cont'd)

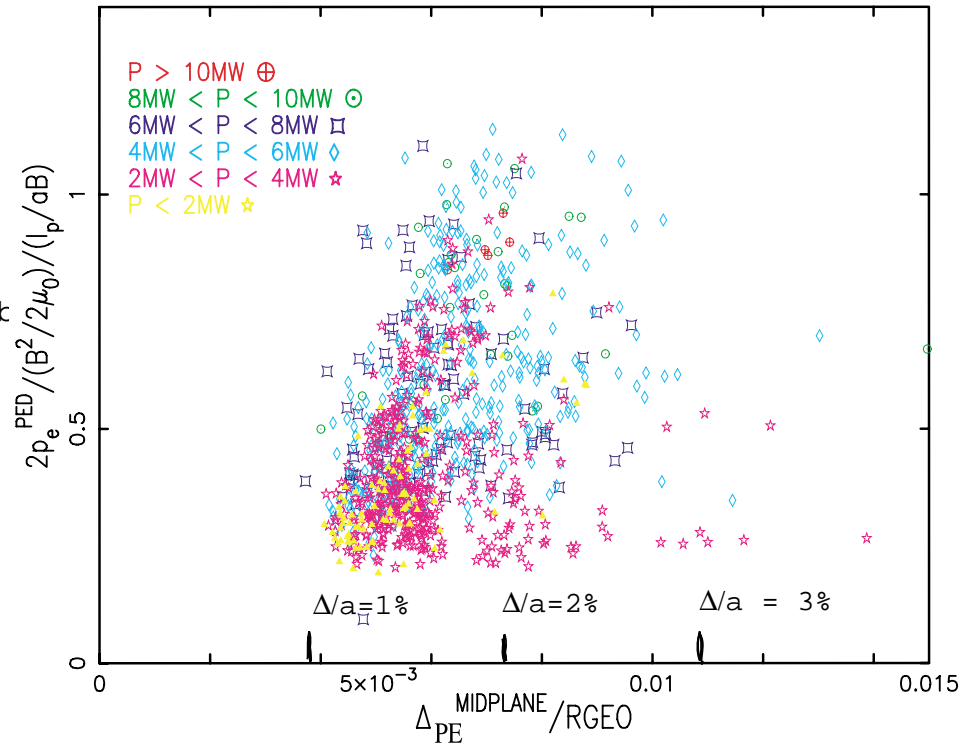
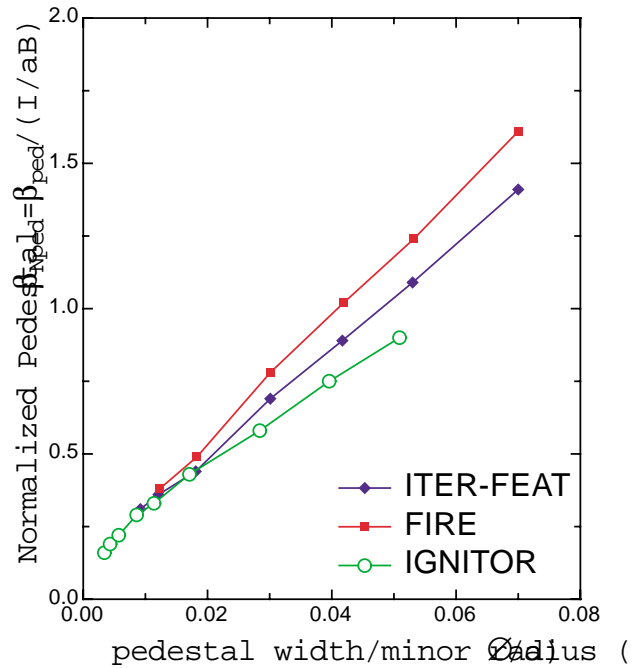
- Problems with statistical approaches:
 - Existing fits lump all data, when likely there is a low power P- dependent regime, and the stiff P-independent MHD fits likely apply only to a high power saturated regime.
 - Detailed peeling - ballooning mode edge stability with real equilibria varying width_ped, finds that $[dp/dr]_{crit}$ depends on width_ped, e. g. $p_{ped} \propto width_{ped}^{0.7}$ and furthermore edge stability (and ELM's) depend sensitively on edge shaping and edge bootstrap current (breaking density independence). (*Snyder recent APS talk*)
- Better not to focus on width_ped, or T_ped but instead on maximum attainable

$$\beta_{N_ped} : \quad \beta_{norm_ped} = \beta_{ped} / (I/aB)$$

H-mode Pedestal Height (cont'd)

- Some example edge stability studies for β_{N_ped} vs pedestal width (Snyder)

Comparison of Normalized Pedestal Stack



DIID

The physics mystery behind the pedestal

- $\beta_{ped} = (\text{width}_{ped} / a) (q/R) s / q^2$ approx. high-n MHD stability limit

Keeping shapes (s, q, a/R) the same :

- Is the layer width determined by the MHD stability **allowed** ?

$$(\text{width}_{ped} / a) \propto (\beta_{pol_ped})^{0.5} \propto (n_{ped} T_{ped})^{0.5} / B_{pol}$$

- **or**, by the **cause** of the good confinement layer ?

....turbulence growth rates compared to diamagnetic ExB shear rates

$$(\text{width}_{ped} / a) \propto \rho_{star_pol_ped} \propto (T_{ped})^{0.5} / (a B_{pol})$$

- Hard to distinguish scaling difference between $\rho_{star_pol_ped}$ and $(\beta_{pol_ped})^{0.5}$, but $\rho_{star_pol_ped} / (\beta_{pol_ped})^{0.5} \propto 1 / [a n_{ped}^{0.5}] \propto 1 / [a B (n_{ped}/n_G)]^{0.5}$

[a B] is going to get larger [ITER, FIRE, Ig] 10, 6, 6 [JET] 4.3 but not a lot, maybe offset with smaller (n_{ped}/n_G)

- Examples from a very stiff model:

fit to many GLF23renorm transport code runs for ITER, FIRE, IGNITOR at $q_{95} = 3$, $\kappa = 1.8$

$$P_{fus} = \text{volume } (\text{beta}_{ped_N})^2 [B^2 (I/a/B)]^2$$

$$\times 5.83 \times 10^{-5} (n_i/n_e)^2 (n_{line} / n_{ped})^{1.5}$$

$$\times \exp [2.(2.15+(1.-(n_i/n_e))+0.75(1.+0.5/v^{0.25})) / (R/a)]$$

$$\times \exp [2.(0.00275 P_{ped} (R/a)^{1.5} / T_{ped}^{1.5})^2]$$

where $v = 0.1 n_{line_19} R / T_{ped}^2$ and $\text{volume} = \kappa (\pi a^2) (2\pi R)$

[meters, Tesla, MA, keV, MW, n_{19} , etc]

$$\text{beta}_{ped_N} = \text{beta}_{ped} / (I/a/B)$$

$$P_{ped} = P_{fus} / 5. - P_{brem} + P_{aux} + P_{oh} \quad Q = P_{fus} / P_{aux}$$

(see Kinsey Sherwood talk)

GLF23renorm fit core + Thomsen-Cordey MHD-pedestal rule compared to y2 and gB_perkins H global τ_E scaling

$n_{line}/n_{ped} = 1.4$, $T(0)/T_{ped} = 5.0$, $T(0)/\langle T \rangle = 2.6$, $\langle \beta \rangle_N / \beta_{ped_N} = 3.32$

ITER-FEAT

P_aux	n_line / n_G	core-ped model			y2			gB_perkins		
MW		Q	β_{ped_N}	T_ped	Q	β_{ped_N}	T_ped	Q	β_{ped_N}	T_ped
40	0.86	4.9	0.42	2.9	11.	0.50	3.5	31	0.86	6.0
20		9.4	0.42	2.9	15.	0.43	3.0	49.	0.79	5.3

FIRE

P_aux	n_line / n_G	core-ped model			y2			gB_perkins		
MW		Q	β_{ped_N}	T_ped	Q	β_{ped_N}	T_ped	Q	β_{ped_N}	T_ped
20	0.70	4.1	0.58	2.8	4.4	0.43	2.0	8.	0.54	2.6
		4.8*	0.61*	2.9	8.5 #	0.55	2.6	19. #	0.82	3.9
10		8.2	0.58	2.8	2.9	0.30	1.4	2.8	0.30	1.4
		5.3*	0.47*	2.3	9.7 #	0.44	2.0	24. #	0.68	3.1

* Thomsen-Cordey free-fit power scaled pedestal rule

hh=1.15

