



# NEW ASPECTS OF THE IDENTIFICATION OF MAGNETIC ISLANDS FROM ECE SIGNALS AND CONTROL BY ECCD

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Field Effects in Control", University of Wisconsin,  
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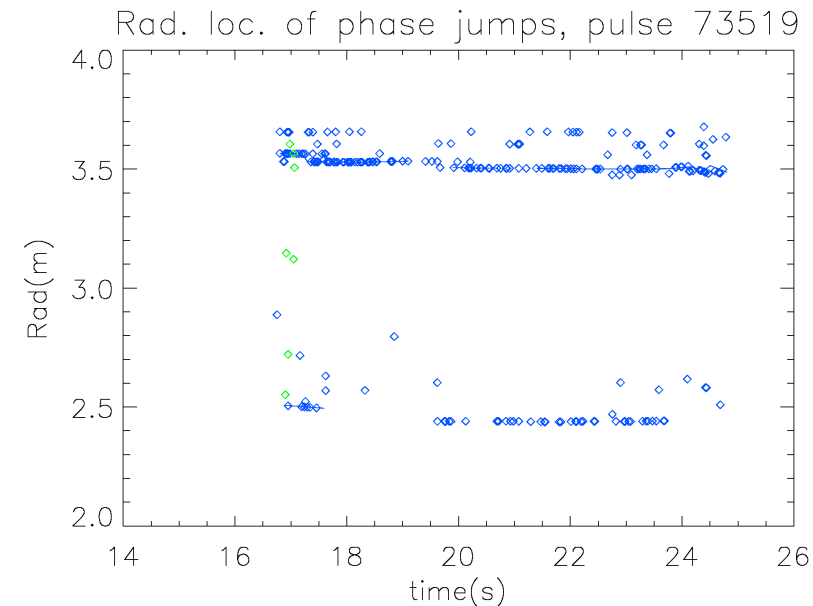
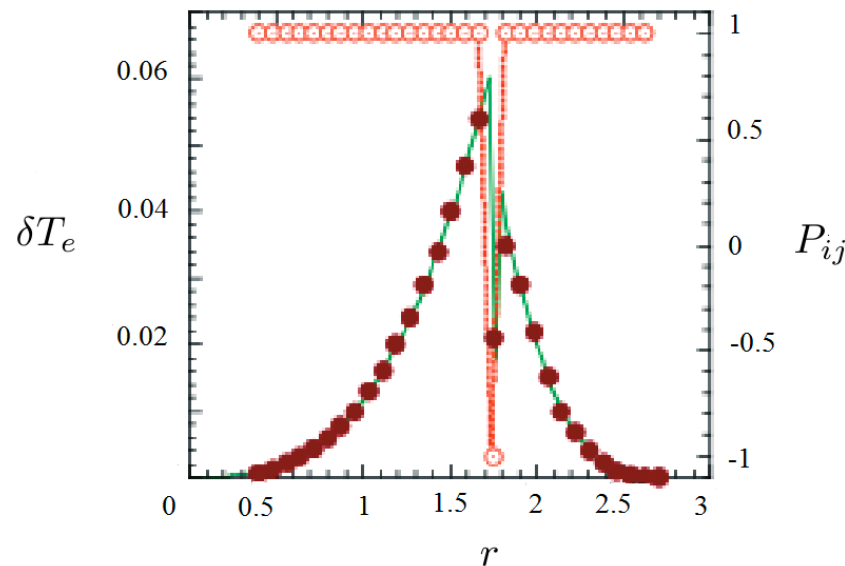


# Outline

- New method of reconstruction of the structure of the tearing modes from ECE signals for intershot analysis
- Response of tearing unstable plasma slab to an rf driven current in the frame of a neoclassical nonlinear slab model
- Appearance of current sheets and secondary island structure
- Open questions for control strategies



## ECE $\delta T_e(r,t)$ fluctuations and tearing mode islands



- Ideally, the Temperature fluctuations at the Island rotation frequency should invert their phase near to the island O-point [J. Berrino et al, Nucl. Fusion **45** 2350 (2005)].
- The normalized cross-correlation  $P_N(x) \approx \cos \delta\phi_{x,1}$  of thermal fluctuations sensed by two adjacent ECE channels has a concavity that is extremal at the rational surface  $x=0$  and can be monitored on a sequence of ECE channels



# ECE $\delta T_e(r,t)$ fluctuations and radial tearing modes structure

- **New method** of reconstruction of the structure of the tearing modes from *measurements* of ECE  $\delta T_e(r, \zeta)$  for intershot analysis

$$\delta T(r, \zeta) = T(r, \zeta) - T_0(r) = \frac{W^2}{16} T_0'(r) \frac{S_s}{r_s} \frac{q/q_s}{1 - q/q_s} \frac{\Psi(r)}{\Psi(r_s)} \cos \zeta$$

- **Minimisation of functional**

$$\Phi(\Psi) \equiv \frac{1}{2} \sum_i^N \left\| \delta T(\Psi(R_i), \mathbf{c}) - \delta T_{ECE}(R_i) \right\|^2$$

under the constraint

of fulfilling the tearing mode equation in curvilinear geometry (toroidicity & shape)

$$(m - nq) \left\{ \left( \frac{g_{\vartheta\vartheta}}{g} \right)_{0,0} \Psi''_{m,n} + \left( \frac{1}{\sqrt{g}} \left( \frac{g_{\vartheta\vartheta}}{\sqrt{g}} \right)' \right)_{0,0} \Psi'_{m,n} - \left( \frac{1}{\sqrt{g}} \left( \frac{g_{r\vartheta}}{\sqrt{g}} \right)' \right)_{0,0} \Psi'_{m,n} - \left( \frac{g_{rr}}{g} \right)_{0,0} m^2 \Psi_{m,n} \right\} - mq \left( \frac{J_0^{\varphi'}}{F_0'} \right)_{0,0} \Psi_{m,n}$$



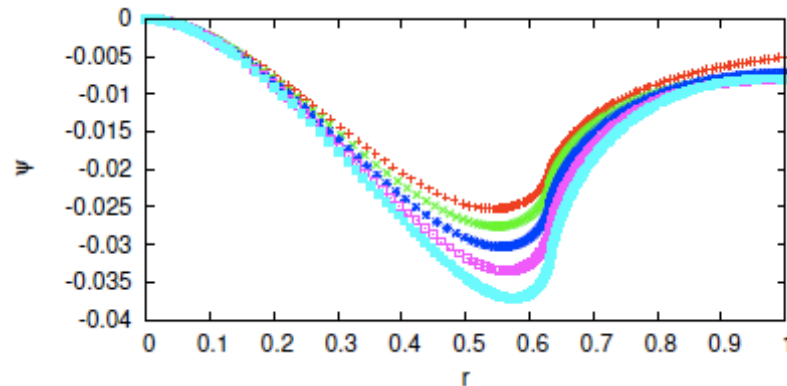
# Geometric effects on tearing eigenfunction

- Toroidal, shaped, equilibrium configuration described by:

$$R = R_0 + r \cos \vartheta + \Delta + r \lambda \sin \vartheta - E \cos \vartheta + O(\varepsilon^2)$$

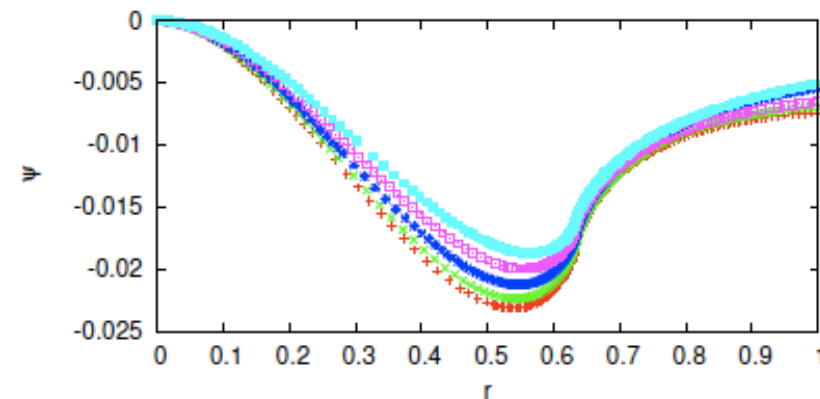
$$Z = r \sin \vartheta - r \lambda \cos \vartheta + E \sin \vartheta + O(\varepsilon^2)$$

- Sensitivity of tearing eigenfunction to  $\Delta_{shaf}$ ,  $E$



"Autof\_SHAF\_0.2\_ELON\_0.dat" u 1:2 +  
 "Autof\_SHAF\_0.4\_ELON\_0.dat" u 1:2 x  
 "Autof\_SHAF\_0.6\_ELON\_0.dat" u 1:2 \*  
 "Autof\_SHAF\_0.8\_ELON\_0.dat" u 1:2 □  
 "Autof\_SHAF\_1\_ELON\_0.dat" u 1:2 ■

*Sensitivity to  $\Delta_{shaf}$*



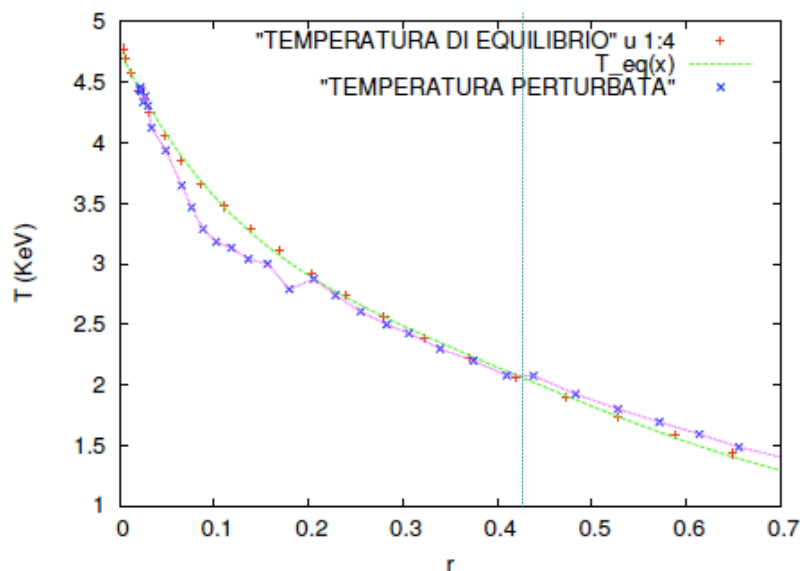
"Autof\_SHAF\_0\_ELON\_0.2.dat" u 1:2 +  
 "Autof\_SHAF\_0\_ELON\_0.4.dat" u 1:2 x  
 "Autof\_SHAF\_0\_ELON\_0.6.dat" u 1:2 \*  
 "Autof\_SHAF\_0\_ELON\_0.8.dat" u 1:2 □  
 "Autof\_SHAF\_0\_ELON\_1.dat" u 1:2 ■

*Sensitivity to  $E$*

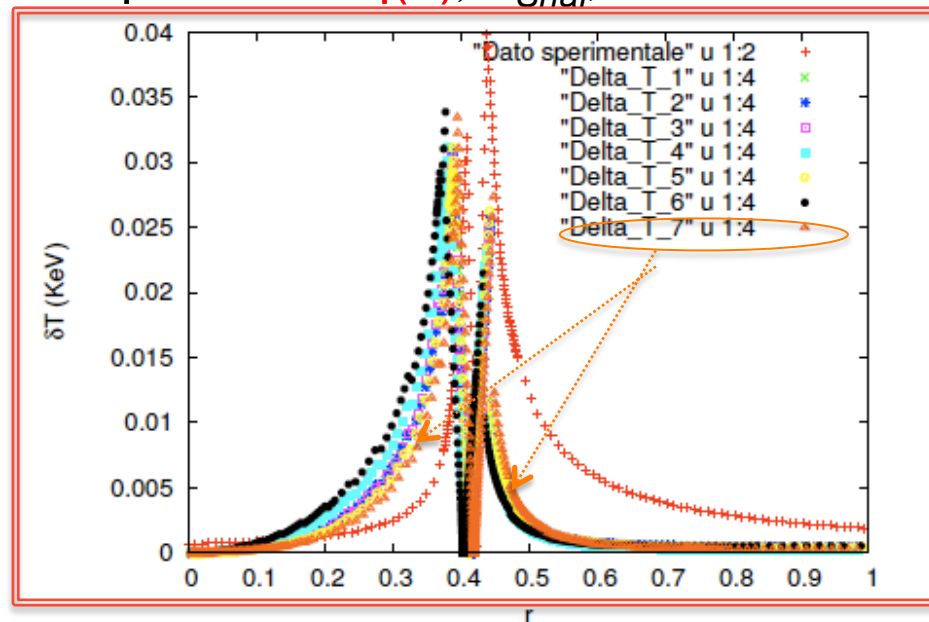


# Geometric effects on tearing eigenfunction

- Minimization of **mean square discrepancy  $\Phi(\Psi)$**  is to be performed in terms of control parameters of equilibrium:  $q(0)$ ,  $\Delta_{Shaf}$ ,  $E$



JET Te profile for #70677 with (3,2) NTM



(b) Il funzionale minimizzato è alla curva Delta\_T\_7 (triangoli)

Automatic optimization

E	$\Delta_s$	$q_0$	$\Phi$	$\Delta'$
1	1	1.0912	3.8454	-2.8175
1	1	1.09749	3.77903	-2.6243
1	1	1.04312	4.14636	-3.567
1	1	1.24197	5.3007	-0,7313
1	1	0.929192	3.75385	-4.741
1	1	1.35433	6.21886	2.0911
1	1	0.826206	2.81569	-5.84774

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## Remarks on models of NTM control by ECCD

- Much detailed work has been devoted to extension of the basic nonlinear Rutherford model to obtain *quantitative criteria* for the *power required to control a magnetic island* by rf driven current
- The generalized Rutherford Equation for the tearing mode island width  $W$  is obtained by *a nonlinear averaging of Faraday-Ohm law* over the *single scale length* defined by the width of the magnetic island separatrix
- 
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$$\frac{\tau_R}{r_s} \frac{dW}{dt} = r_s \Delta'_0 + \underbrace{\beta_p \left( \frac{\varepsilon^{1/2}}{s} \frac{r_s}{W_c} \frac{W/W_c}{1 + (W/W_c)^2} \right)}_{\text{Neoclassical bootstrap effect}} - r_s g \frac{\varpi(\varpi - \omega_{*i})}{\omega_{*e}^2} \left( \frac{L_s}{L_n} \right)^2 \frac{\rho_{i\theta}^2}{W^3} + \underbrace{\frac{8r_s \delta_{EC} q}{\pi W^2} \eta_h \left( \frac{W}{\delta_{EC}} \right) \left( \frac{J_{EC}(t)}{J_{boot}} \right)}_{\text{ECCD control term}}$$

Neoclassical bootstrap effect

ECCD control term

- If the (helical) ECCD current is driven within a depth  $\delta_{EC} < W$ , **important 2D nonlinear** effects are missed by the Rutherford models



## Study of 2D effects in a Neoclassical 4-Field Model\*

*Faraday-Ohm* 
$$\frac{\partial \psi}{\partial t} + \vec{v}_E \cdot \vec{\nabla} \psi = -\vec{v}_{pe} \cdot \vec{\nabla} \psi - \eta_{NC} (J_{\parallel} - J_{bs} - J_{EC})$$

*Shear-Alfvén* 
$$\frac{\partial U}{\partial t} + \vec{v}_E \cdot \vec{\nabla} U = \frac{1}{m_i n} B_0 \nabla_{\parallel} J_{\parallel} - \frac{\mu_0 (1 + \tau_T)}{m_i n B_0} (J_{\parallel} \nabla_{\parallel} p_{e\Delta} + p_{e\Delta} \nabla_{\parallel} J_{\parallel})$$

*Parallel ion velocity* 
$$\frac{\partial v_{i\parallel}}{\partial t} + \vec{v}_E \cdot \vec{\nabla} v_{i\parallel} = -\frac{(1 + \tau_T)}{m_i n} \left( \nabla_{\parallel} p_e + \frac{2}{3} \nabla_{\parallel} p_{e\Delta} \right)$$

*Electron pressure* 
$$\frac{\partial p_e}{\partial t} + \vec{v}_E \cdot \vec{\nabla} p_e = -\left( \frac{5}{3} p_e + \frac{4}{9} p_{e\Delta} \right) \nabla_{\parallel} \left( v_{i\parallel} - \frac{J_{\parallel}}{en} \right)$$

$$p_{e\Delta} = -\frac{m_e n q \mu^e}{\tau_{ee} \epsilon} \frac{\nabla_{\parallel} B}{\langle (\nabla_{\parallel} B)^2 \rangle} \left( \frac{\partial \phi}{\partial r} - \frac{1}{en} \frac{\partial p_e}{\partial r} + \frac{1}{3en} \frac{\partial p_{e\Delta}}{\partial r} \right)$$

*Closure relation  
for anisotropy*

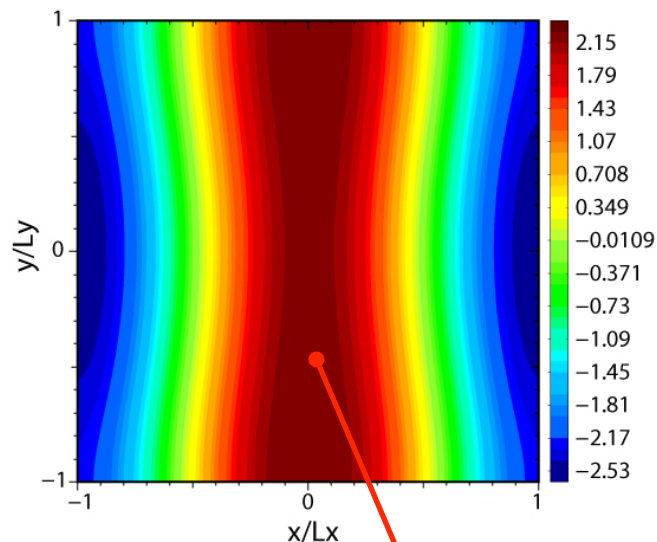
[\*] Lazzaro, Comisso, Valdettaro, Phys. Plasmas **17**, 052509 (2010)





## ECCD centered on the O-point

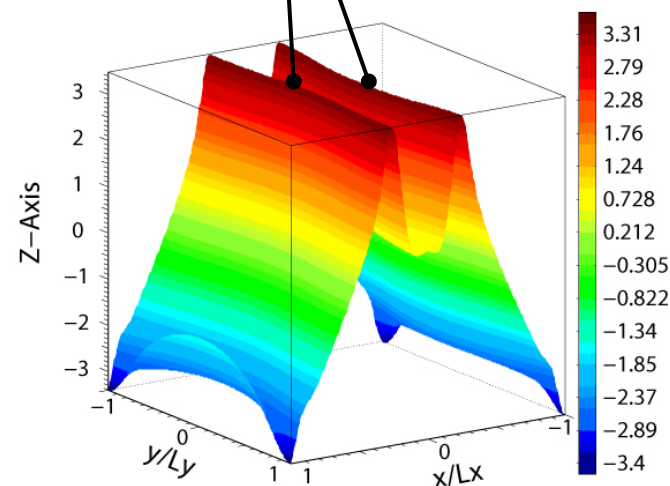
Perturbed Poloidal Magnetic Flux at time 1860.00



ECCD deposition has led (promptly) to a *new equilibrium state* without singular points!

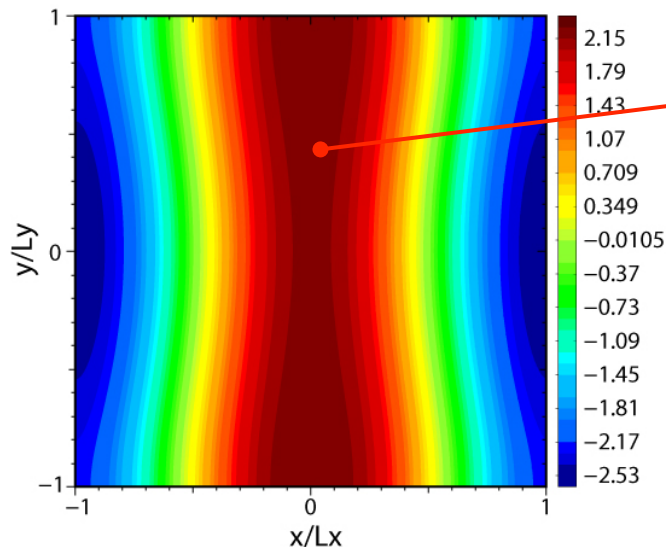
Current sheets appear on both sides of singular surface, as *alternative* to the equilibrium with magnetic islands

Perturbed Parallel Current Density at time 1860.00



# ECCD with angular offset

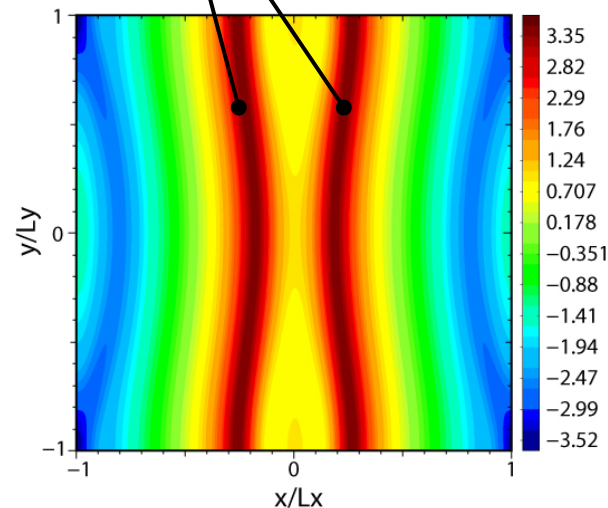
Perturbed Poloidal Magnetic Flux at time 1860.00



Notwithstanding the phase offset, reconnection is frozen!

Current sheets

Perturbed Parallel Current Density at time 1860.00

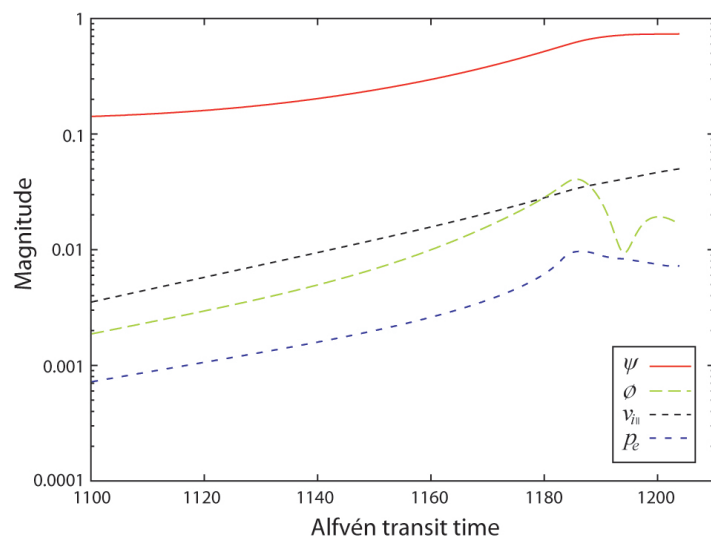


A (moderate) angular offset of ECCD produces a **behavior very much like that of an exact deposition on the O-point**

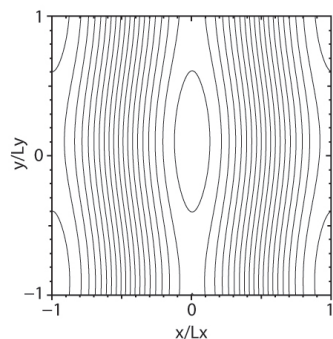


# Response to a train of *narrow* ECCD pulses

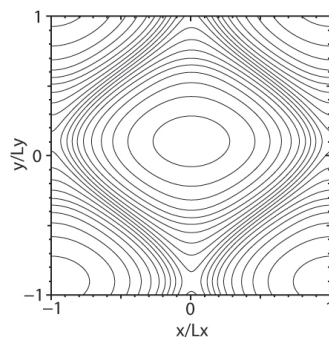
Free system evolution



(a)

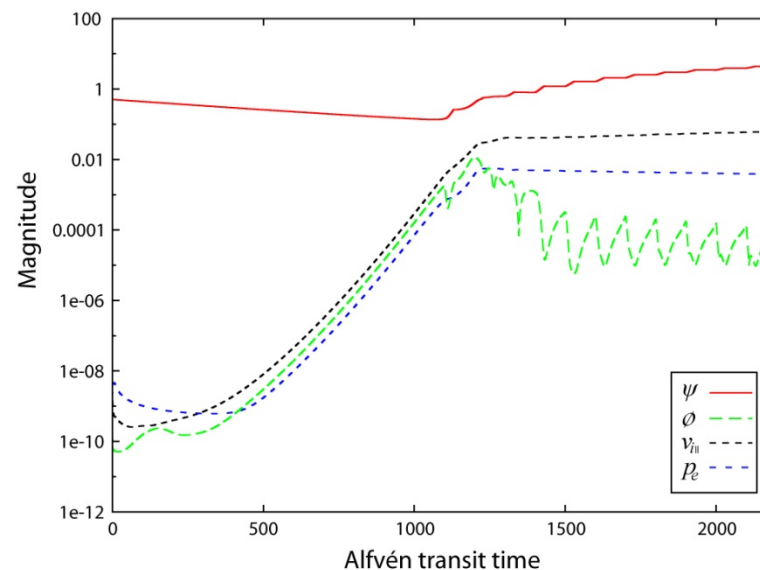
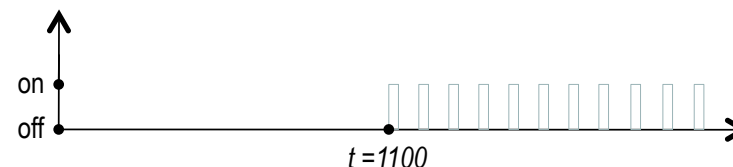


(b)  $t = 1100$



(c)  $t = 1180$

Pulsed (ECCD centered on the O-point) system evolution

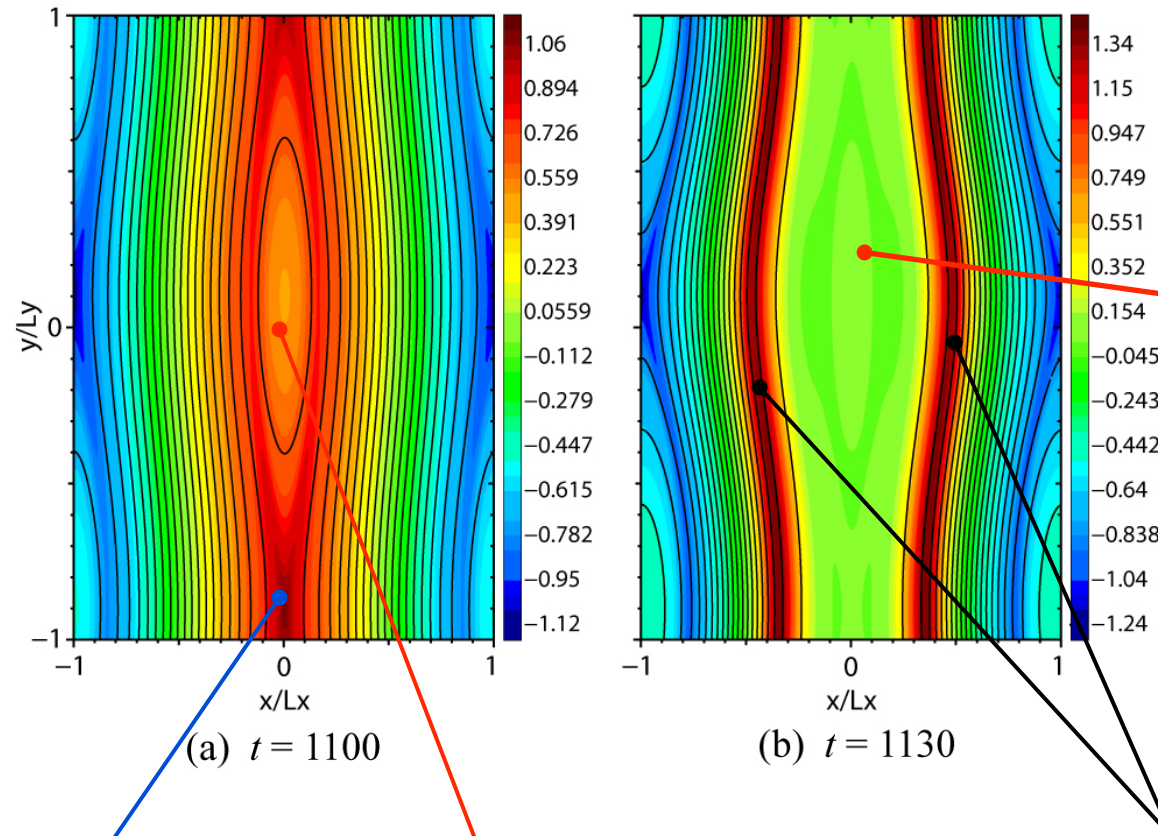


[Comisso and Lazzaro, to appear on Nucl. Fusion]



# Effect of the *first* narrow ECCD pulse

Poloidal magnetic flux (black lines) and out-of-plane current density (color)



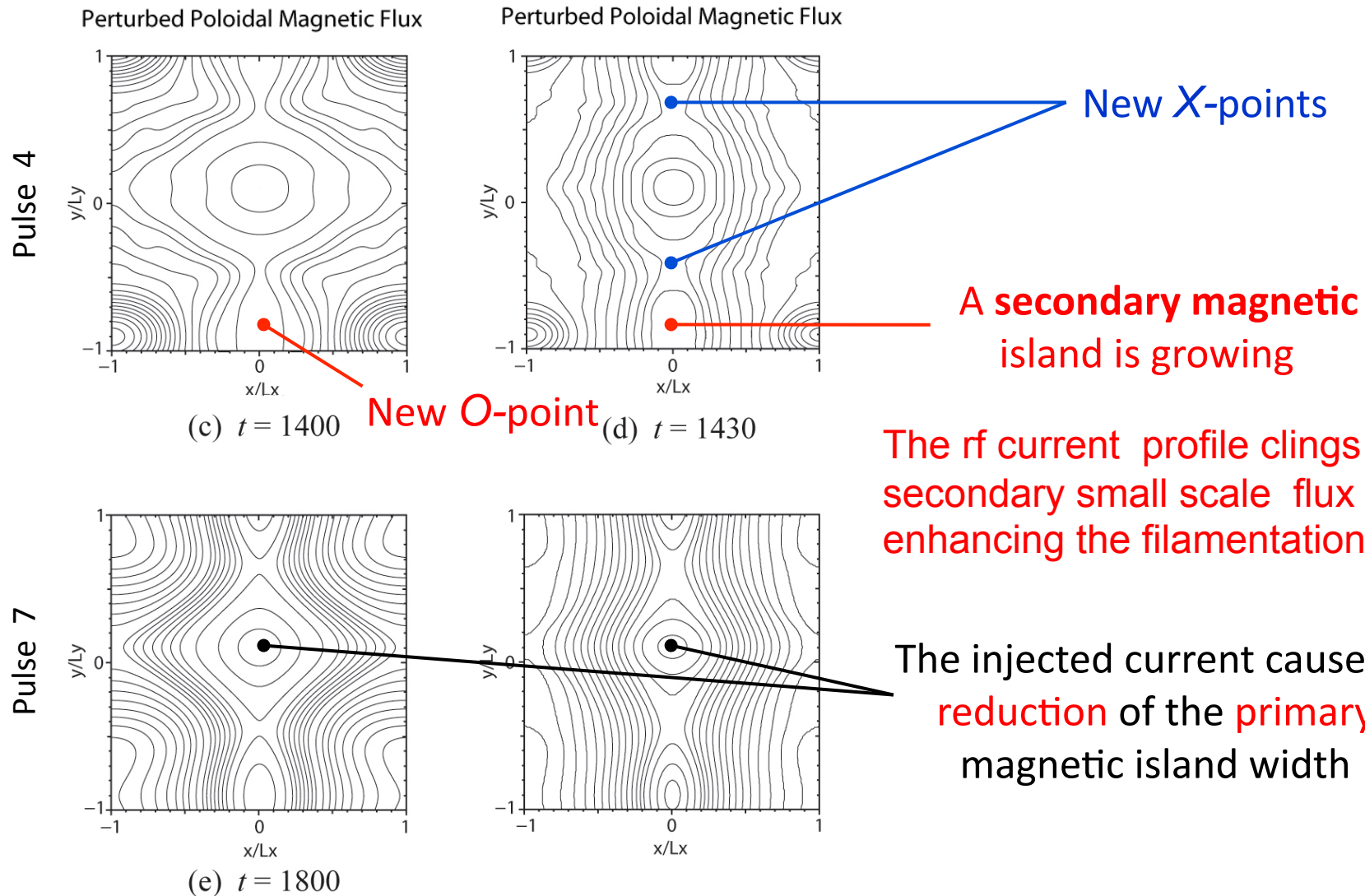
Immediate freezing of the reconnection process and a new nonlinear equilibrium state is reached with no singular points

X-point

Magnetic island

Current sheets

# Magnetic Island behavior under ECCD pulses





# Conclusions

- An automatic method developed for identification of the structure of tearing modes, capable of estimating the linear  $D'$  appears promising
- The study of two dimensional time dependent response of a tearing mode magnetic island to an RF driven current shows the possibility of strong nonlinear effects.
- Application of Extended Magnetohydrodynamics (ExMHD)\* model shows:
  - **first** the prompt appearance of current sheets tending to shield the rf current effect
  - **subsequently** a nonlinear **filamentation** of the island structure that eventually proceeds towards formation of secondary islands
  - The rf  $J$  profile spreads on  $\psi$  surfaces, clinging **also onto the small scale nonlinear structures** and enhancing them.
- ECCD control of NTM based on painstaking **tracking of island "phase"** is probably unnecessary
- Successful NTM control experiments are not at odds with this interpretation

[\*] J.D. Callen, C.C. Hegna, C.R. Sovinec, LP1.00062 at DPP-APS Meeting, Denver, CO, 24-28 October 2005



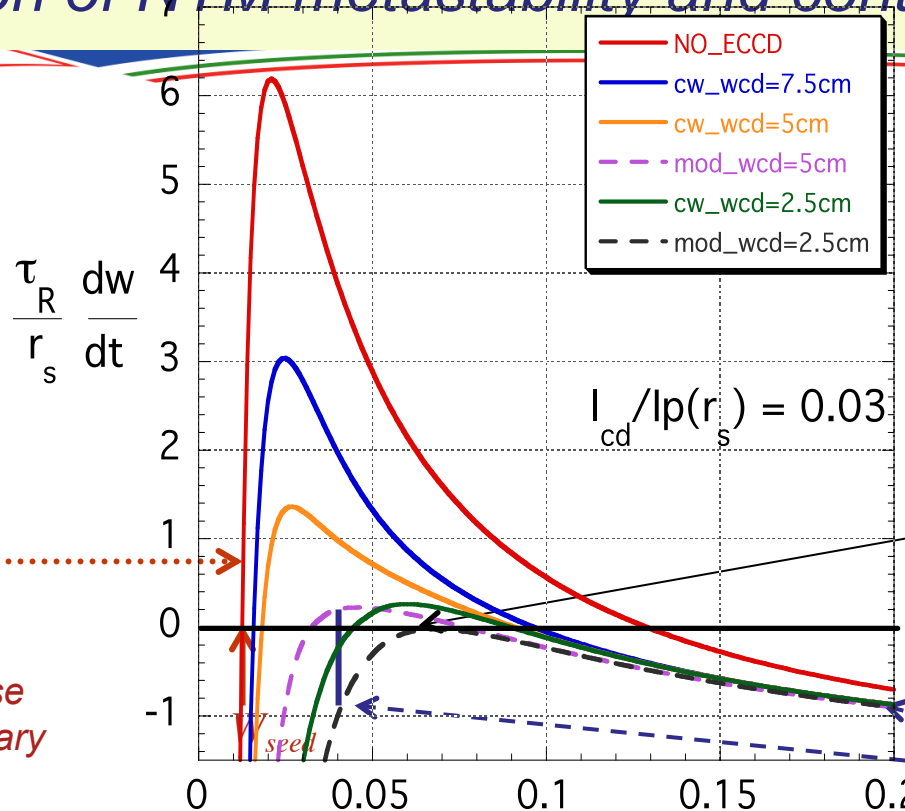
# THE END



*Further discussion  
with contribution of E. Tassi*



# Discussion of NTM metastability and control issues



$\beta_{cr}$  NTM excitation

$\beta_{mar}$  suppression

Hysteresis!

Squeezing a saturated island:  
maximum RF power required

$$\frac{\tau_R}{r_s} \frac{dW}{dt} = r_s \Delta'_0 + \beta_p \left( \frac{\epsilon^{1/2}}{s} \frac{r_s}{W_c} \frac{W/W_c}{1 + (W/W_c)^2} - r_s \Delta'_{pol} \right) + r_s \Delta'_{EC}$$

The term  $\Delta'_{boot}$  is indicated by a dashed line pointing to the  $\Delta'_0$  term. A green arrow points from the  $\Delta'_{pol}$  term to the equation below.

$$\Delta'_{EC} = \frac{8q\delta_{EC}}{\pi W^2} \eta \left( \frac{W}{\delta_{EC}} \right) \left( \frac{J_{EC}(t)}{J_{boot}} \right)$$

RF power deposition on  $q=m/n$  surface required

$$\Delta'_{pol} \approx g \frac{\omega(\omega - \omega_{*i})}{\omega_{*e}^2} \left( \frac{L_s}{L_n} \right)^2 \frac{\rho_{i\theta}^2}{W^3}$$

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## Dissipationless limit & Hamiltonian form

Faraday-Ohm

$$\frac{\partial \psi}{\partial t} + [\phi, \psi] = d_i [\exp p, \psi],$$

Shear-Alfvén

$$\frac{\partial U}{\partial t} + [\phi, U] = -[\nabla^2 \psi, \psi],$$

Parallel ion velocity

$$\frac{\partial v_{i\parallel}}{\partial t} + [\phi, v_{i\parallel}] = (1 + \tau_T) [\psi, \exp p],$$

Electron pressure

$$\frac{\partial p}{\partial t} + [\phi, p] = \frac{5}{3} [\psi, v_{i\parallel}] + \frac{5}{3} d_i [\psi, \nabla^2 \psi],$$

With:

$$\begin{aligned} \bar{t} &\rightarrow \frac{v_A}{L} t, & \bar{x} &\rightarrow \frac{x}{L}, & \bar{\psi} &\rightarrow \frac{\psi}{B_0 L}, & \bar{\phi} &\rightarrow \frac{\phi}{v_A L B_0}, \\ \bar{v}_{i\parallel} &\rightarrow \frac{v_{i\parallel}}{v_A}, & p &\equiv \ln \bar{p}_e \rightarrow \ln \left( \frac{p_e}{m_i n v_A^2} \right), & \bar{U} &\rightarrow \frac{L}{v_A} U, \end{aligned}$$

**Hamiltonian**

$$H = \int d^2 x \left( \frac{|\nabla \psi|^2}{2} + \frac{|\nabla \phi|^2}{2} + \frac{v_{i\parallel}^2}{2(1 + \tau_T)} + \frac{\exp p}{(5/3)} \right)$$