

Error Field Thresholds in H Mode Plasmas

by Richard Buttery¹

with Rob La Haye¹, Yueqiang Liu²,
Bob Pinsker¹, Jong-kyu Park³,
Holger Reimerdes⁴, Ted Strait¹,
and the DIII-D research team.

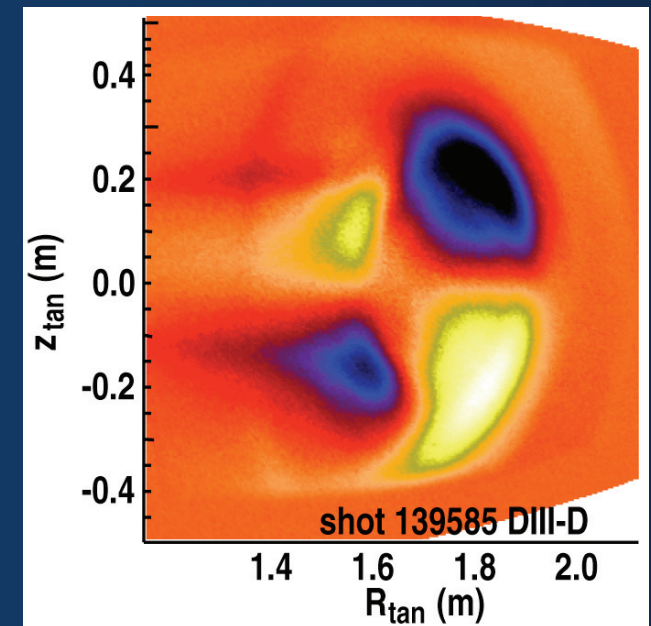
¹General Atomics, USA.

²Culham Centre for Fusion Energy, UK

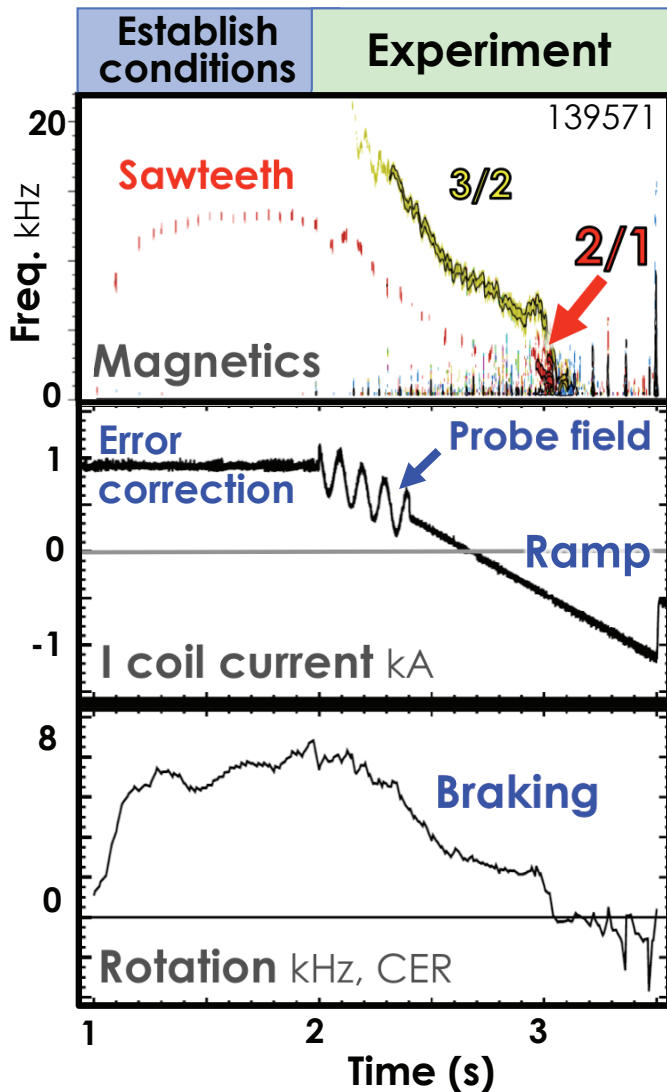
³Princeton Plasma Physics Laboratory, NJ.

⁴Columbia University, NY / CRPP Lausanne, Switzerland.

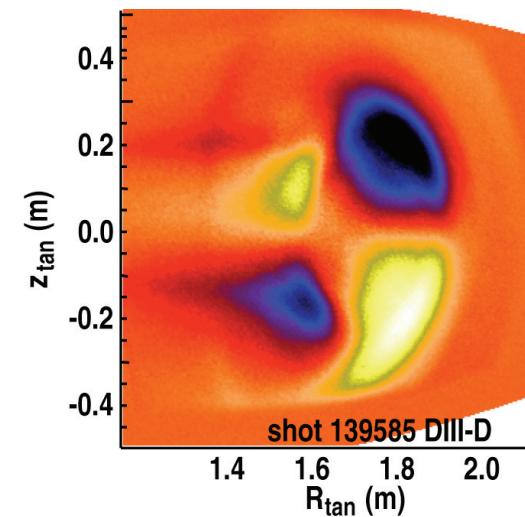
Work funded by the US DOE.



Low Torque H Modes are Susceptible to Error Fields



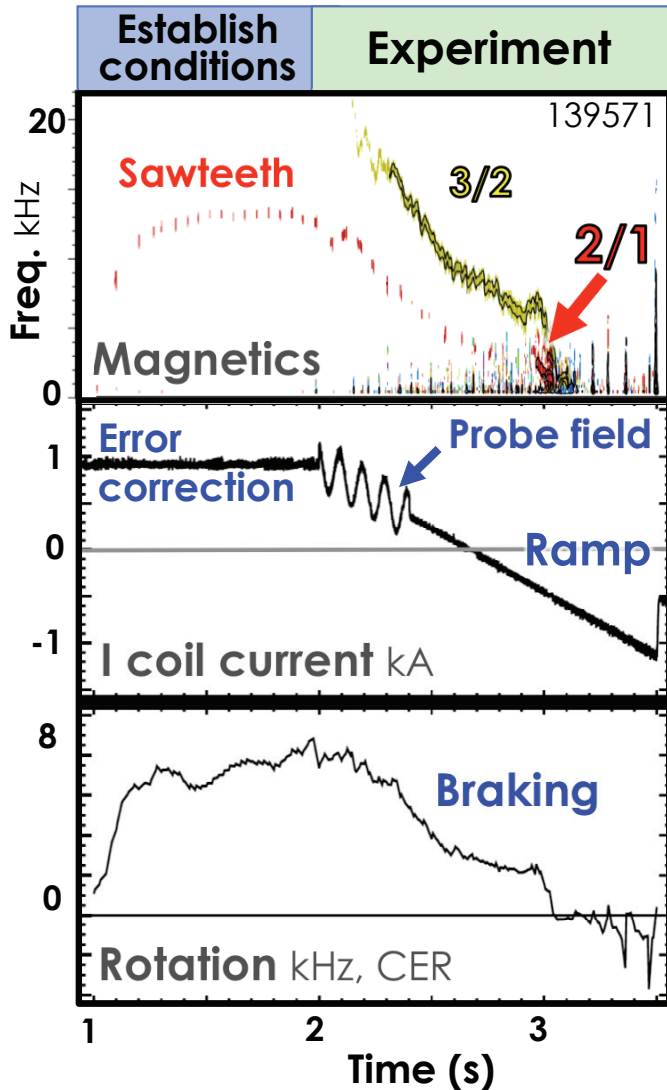
- Applying a *static* error field destabilizes a *rotating* $2/1$ tearing mode:



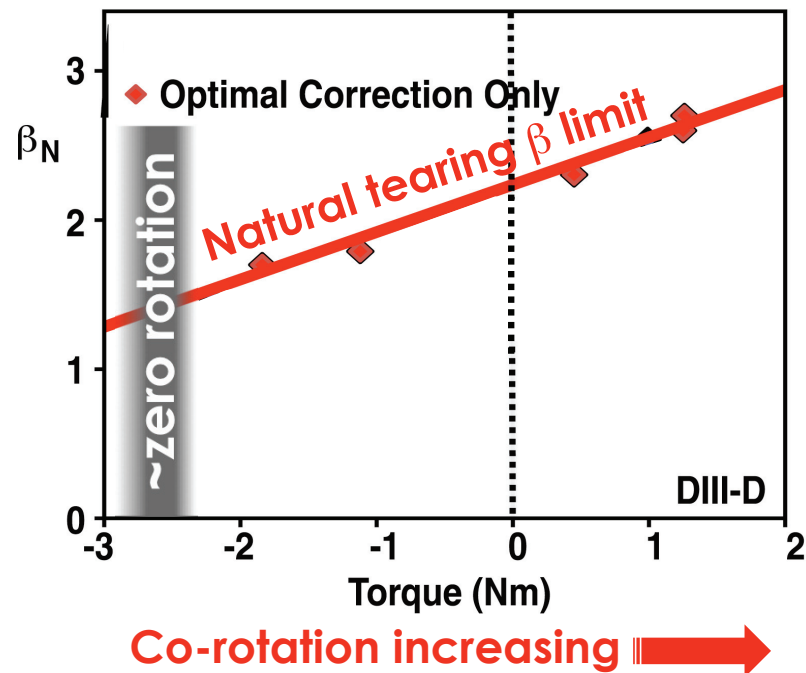
*1.8kHz Fourier decomposed
fast visible imaging*

Feedback
control of NBI
torque and β_N

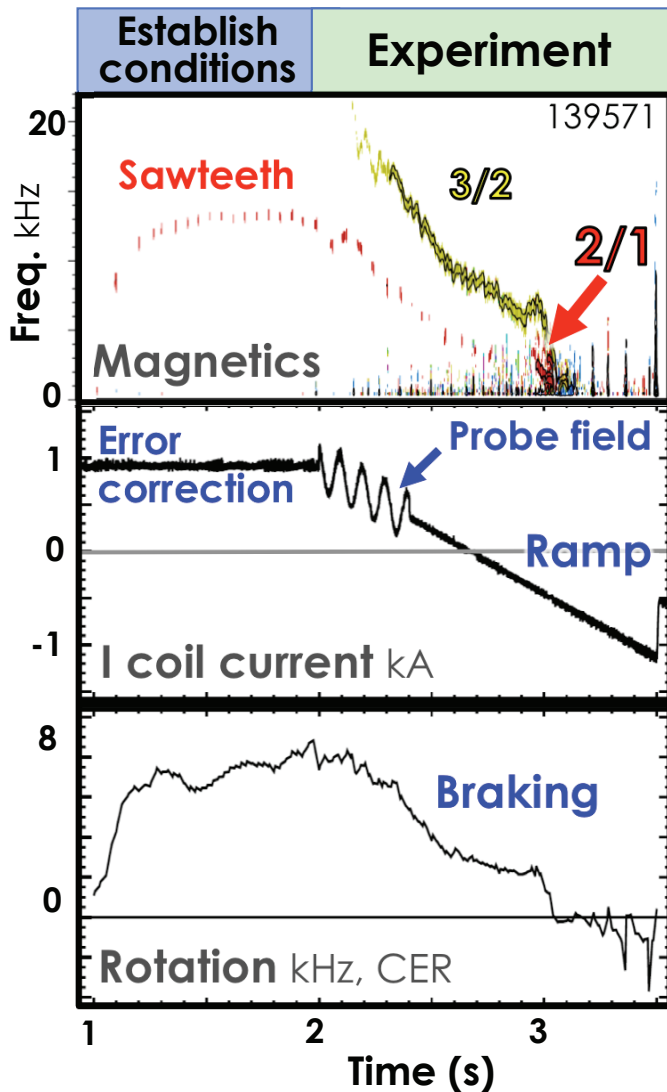
Low Torque H Modes are Susceptible to Error Fields



- Applying a *static* error field destabilizes a *rotating* 2/1 tearing mode:
 - Tearing β_N limit falls with rotation:

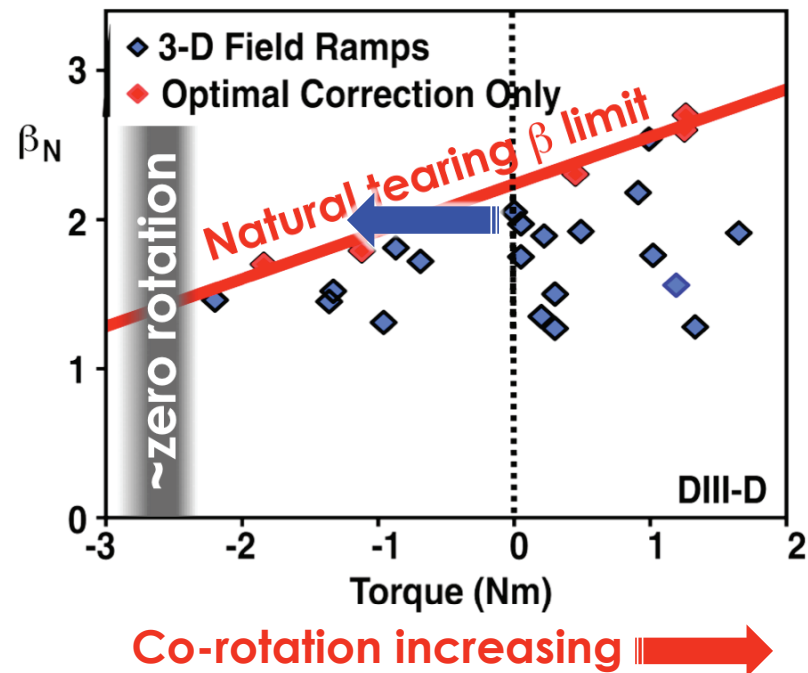


Low Torque H Modes are Susceptible to Error Fields



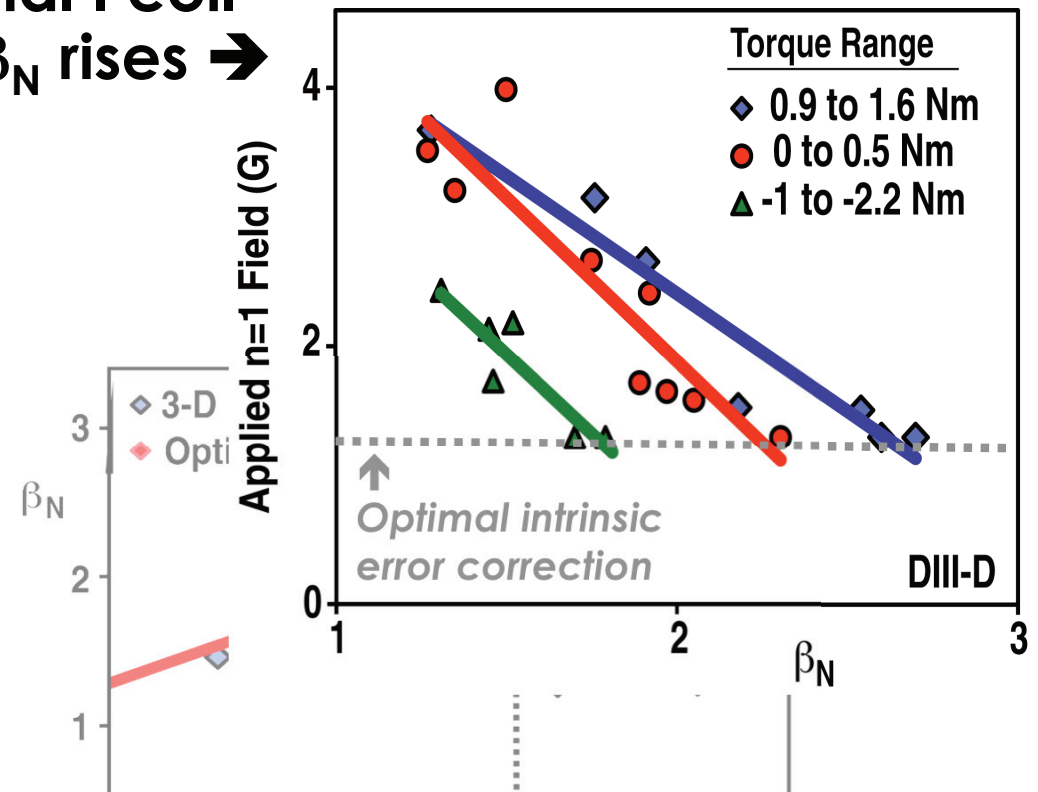
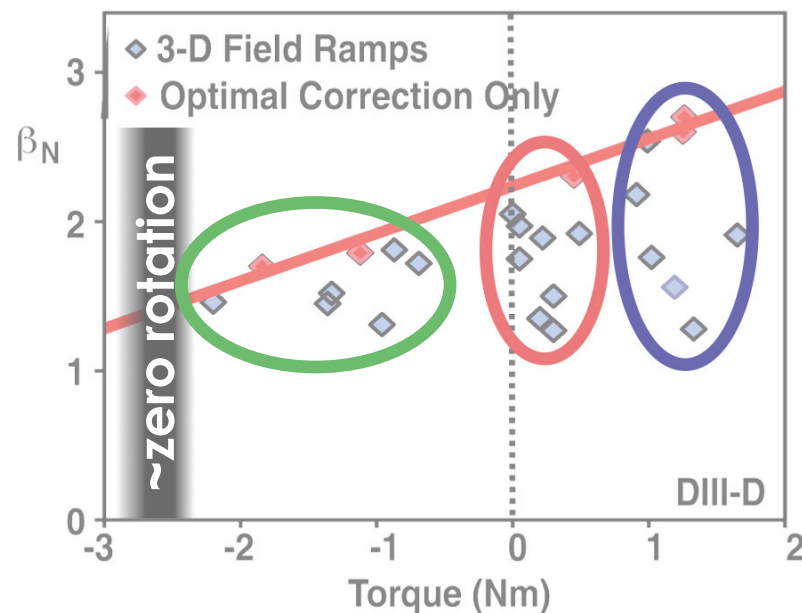
- Applying a *static* error field destabilizes a *rotating* 2/1 tearing mode:

- Tearing β_N limit falls with rotation
- Error field brakes plasma, accessing instability $\rightarrow$ mode grows & locks



Error Field Thresholds Exhibit β and Torque Dependence

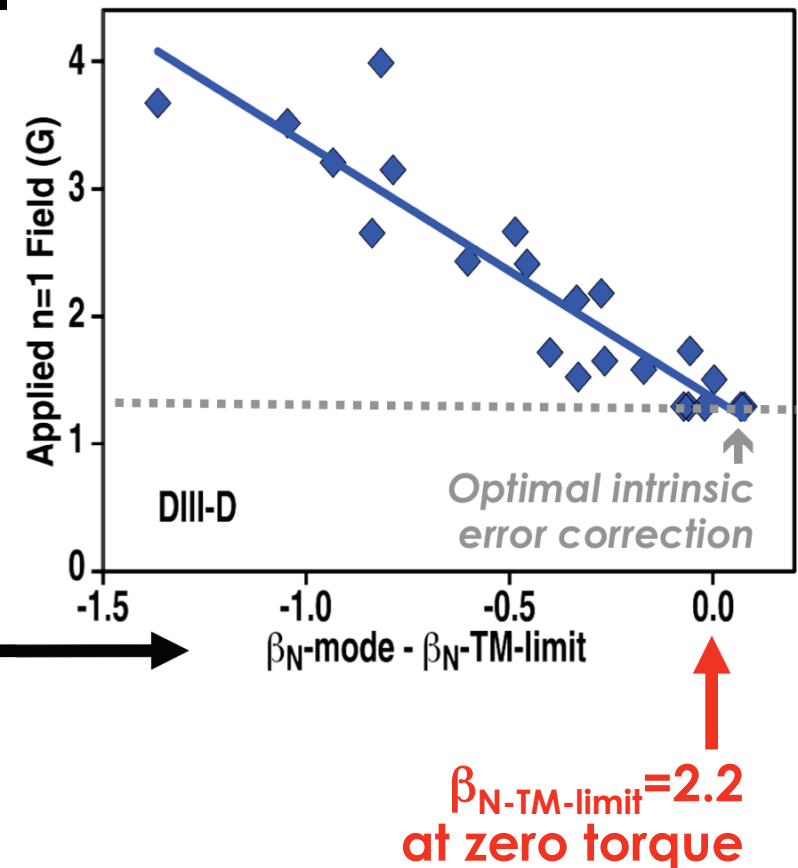
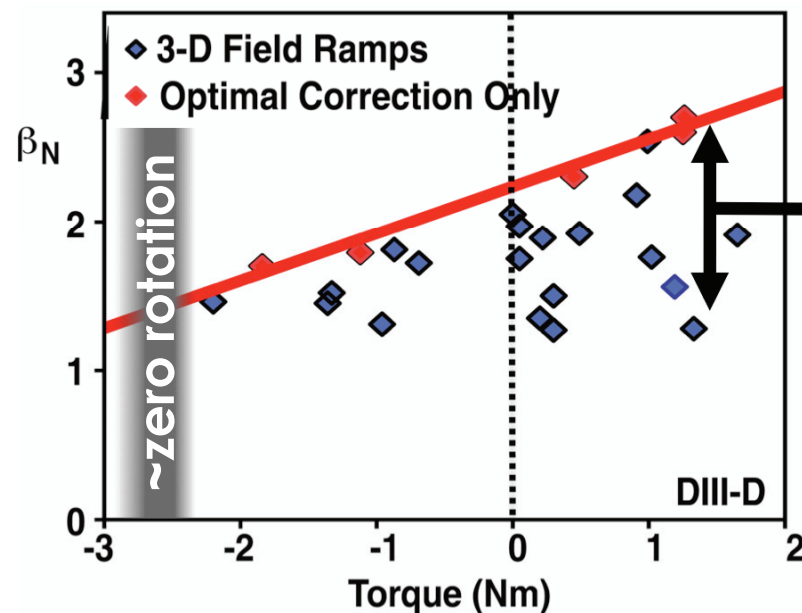
- Field thresholds reach optimal I coil correction level of 1.3G as β_N rises $\rightarrow$
- Torque dependence



Measure field as 2/1 resonant boundary field including ideal response via overlap integral with IPEC dominant mode

Error Field Thresholds Exhibit β and Torque Dependence

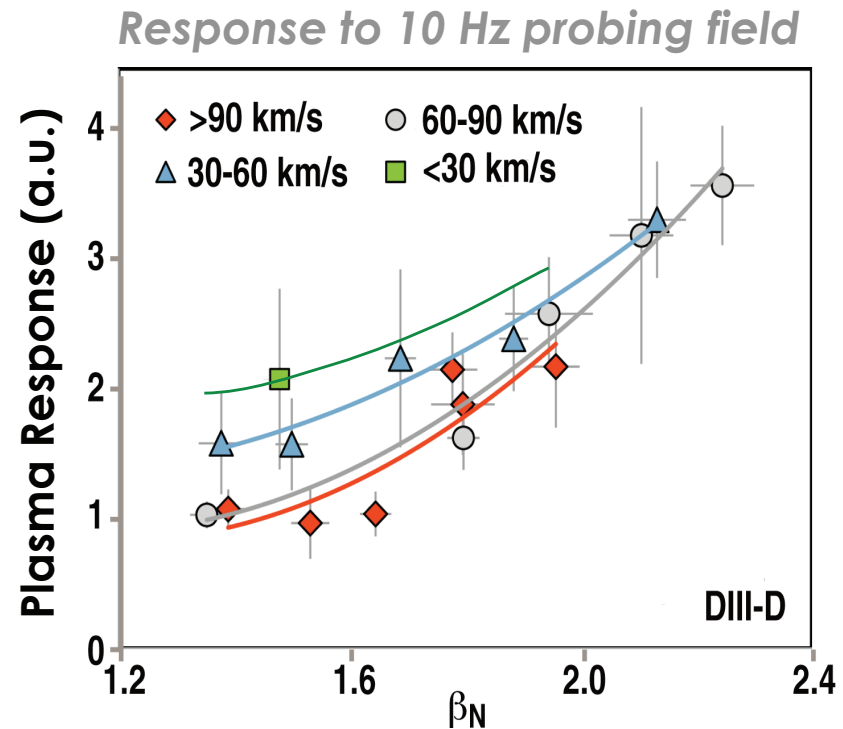
- Field thresholds reach optimal I coil correction level of 1.3G as β_N rises
- Torque dependence
 - Explained by proximity to $\rightarrow$ natural tearing β limit:
 - $\beta_{N-TM-limit} = 2.2 + 0.32T_{NBI}$



What is the nature of the plasma response?

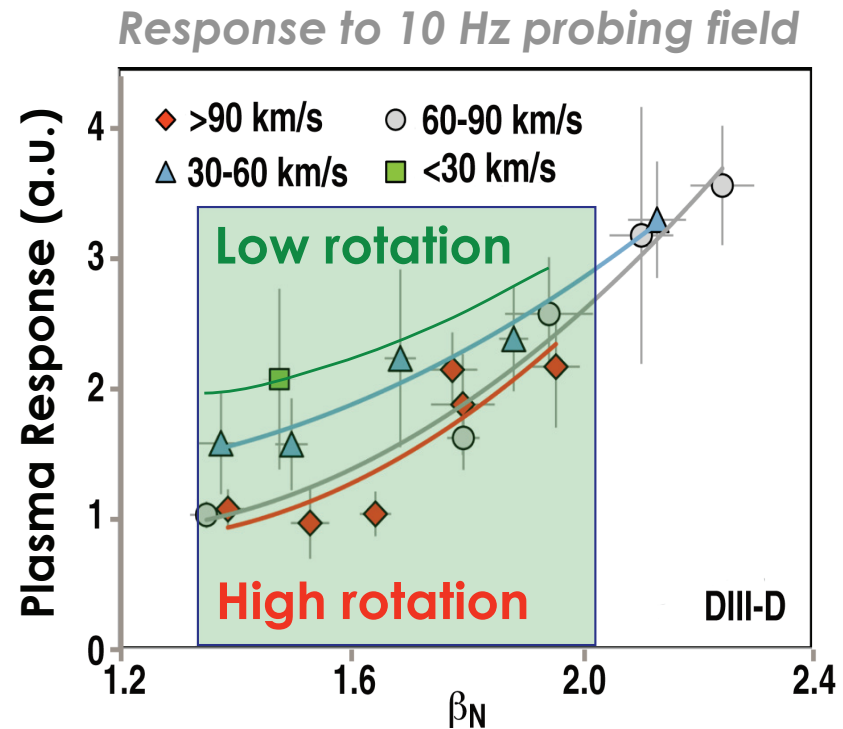
Magnetic Probing Data & Modeling Suggest Both Ideal and Resistive Responses Occurring

- β_N dependence $\rightarrow$ ideal response



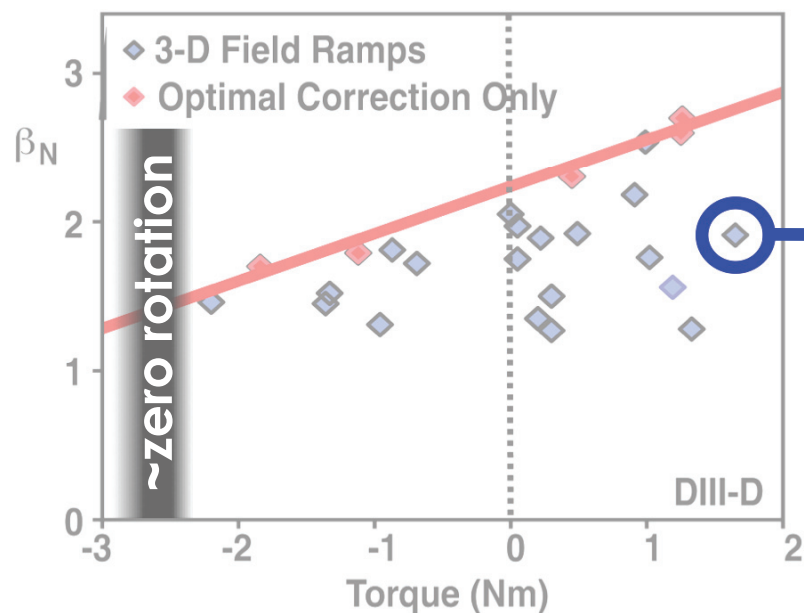
Magnetic Probing Data & Modeling Suggest Both Ideal and Resistive Responses Occurring

- β_N dependence $\rightarrow$ ideal response
- Rotation dependence $\rightarrow$ resistive?
 - Break down of screening response?

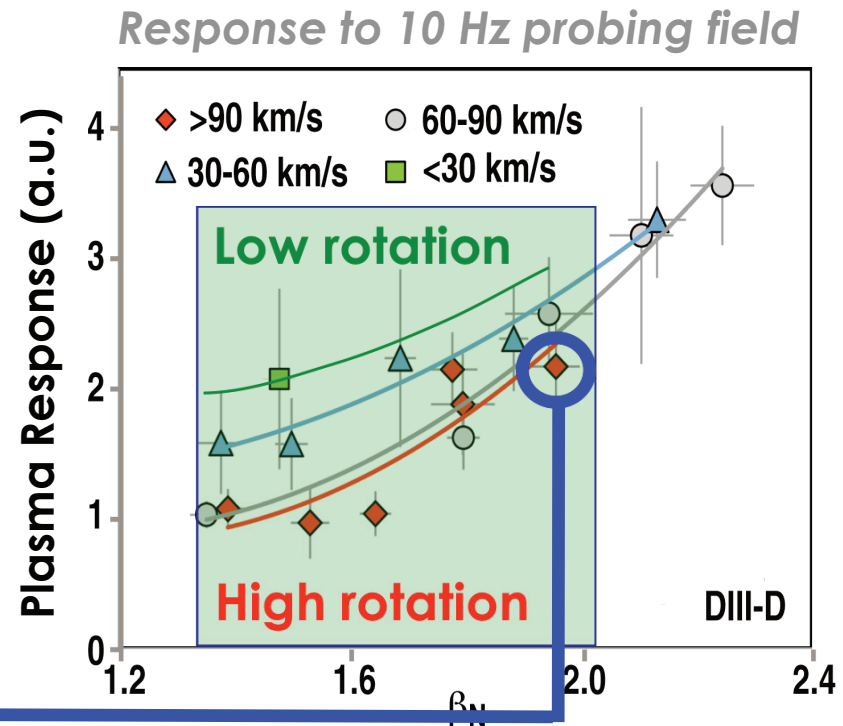


Magnetic Probing Data & Modeling Suggest Both Ideal and Resistive Responses Occurring

- β_N dependence $\rightarrow$ ideal response
- Rotation dependence $\rightarrow$ resistive?
 - Break down of screening response?
 - *Explore with MARS-F modeling...*



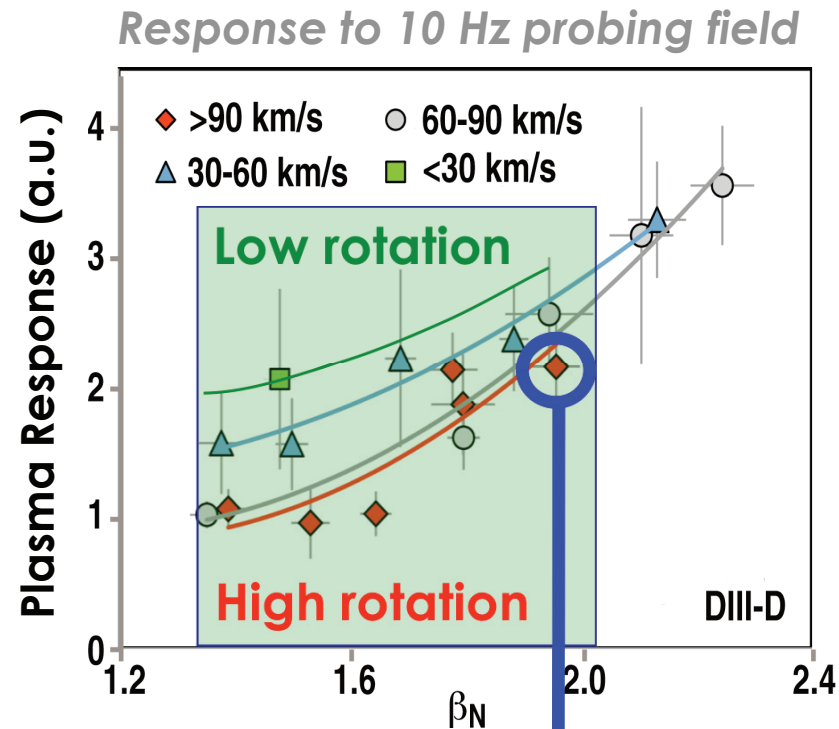
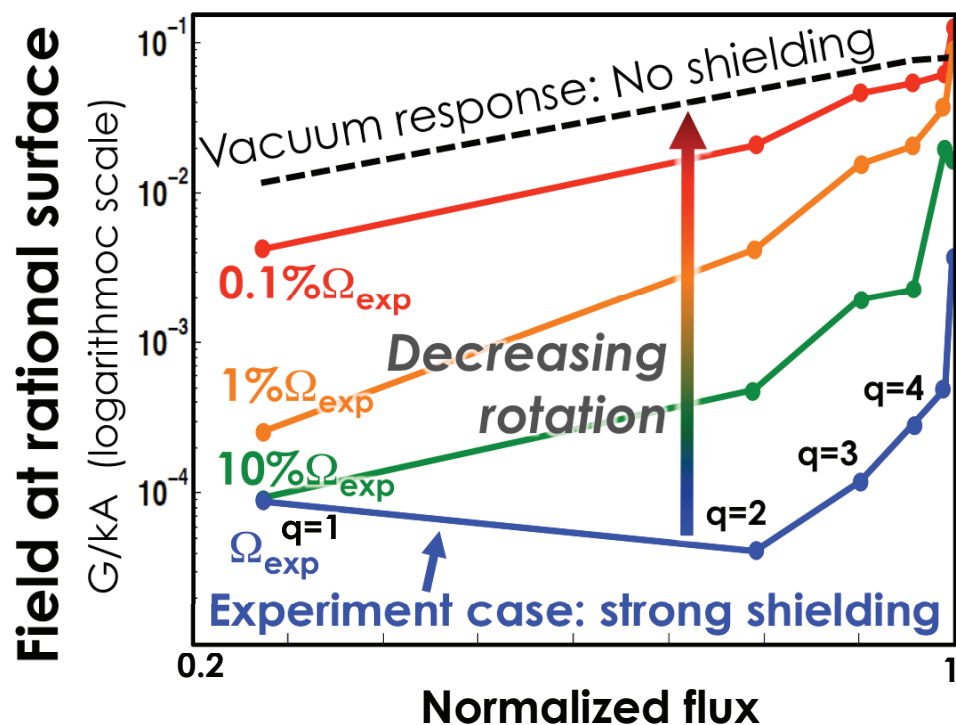
Considered case



Linear calculation with resistivity
Many thanks to Y Liu

Magnetic Probing Data & Modeling Suggest Both Ideal and Resistive Responses Occurring

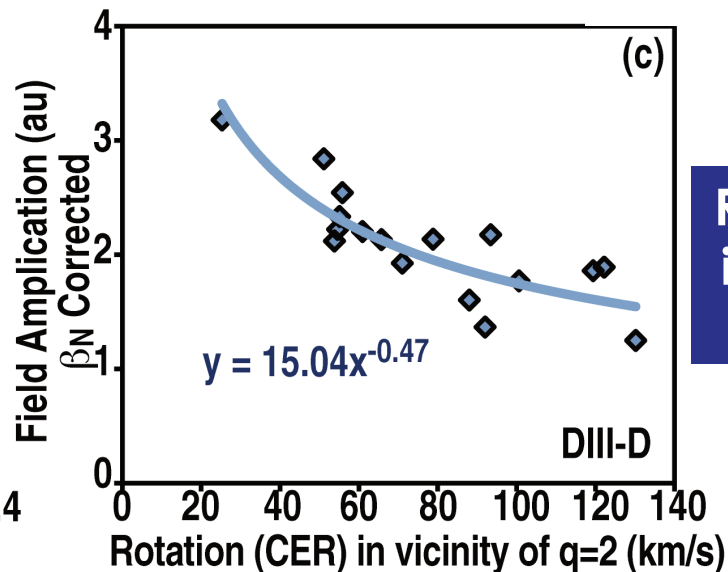
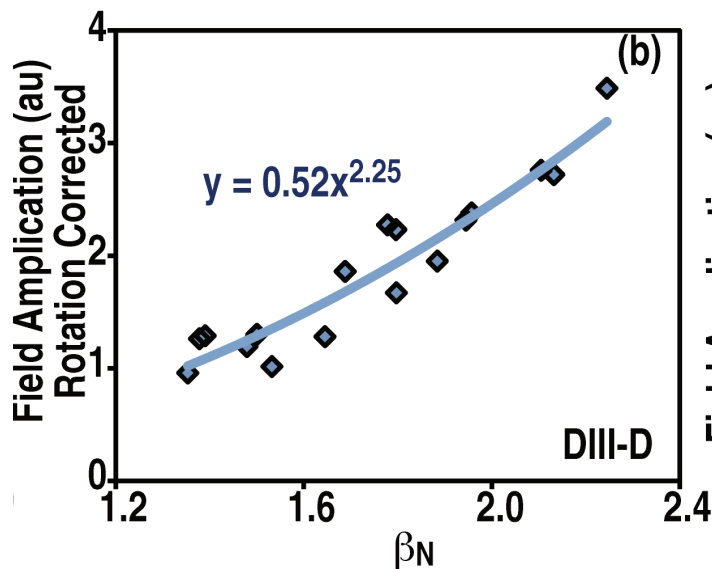
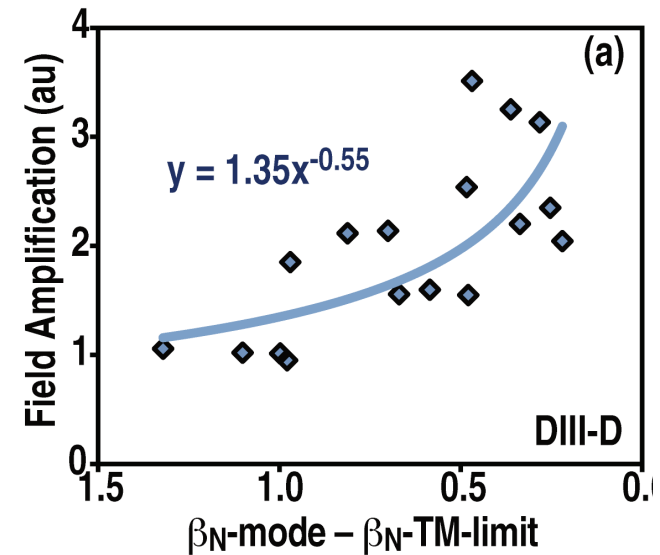
- β_N dependence $\rightarrow$ ideal response
- Rotation dependence $\rightarrow$ resistive?
 - Break down of screening response?
 - *Found to be an effect in MARS-F:*



Linear calculation with resistivity
Many thanks to Y Liu

Fitting Confirms “Two Knobs” Needed to Explain Plasma Response – *not simply ideal or resistive*

- Simple 1-D fit of response to tearing → limit proximity does not do good job
- 2-D fit shows β and rotation response needed



Rotation dependence identified – indicative of resistive response

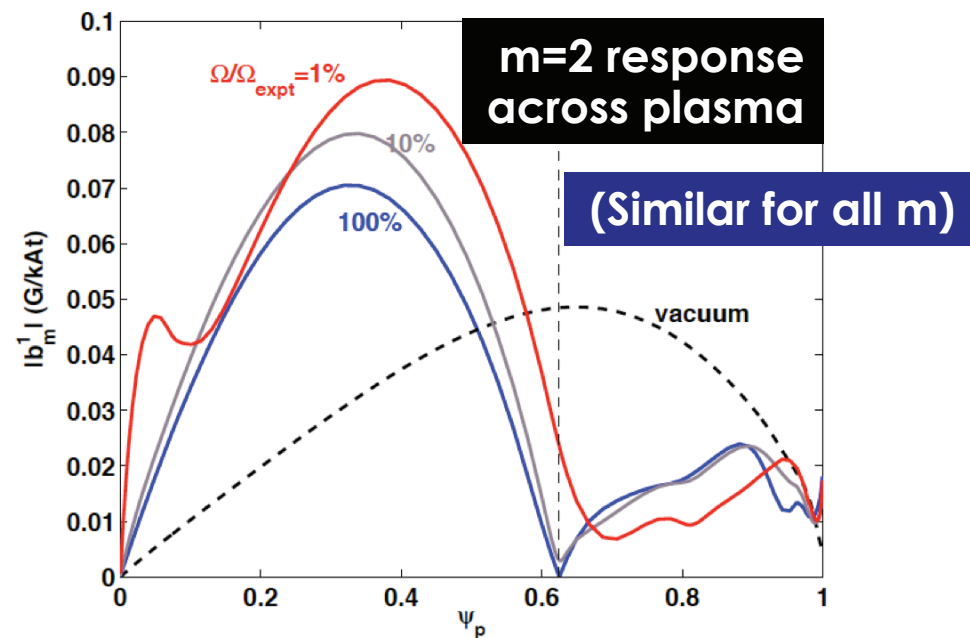
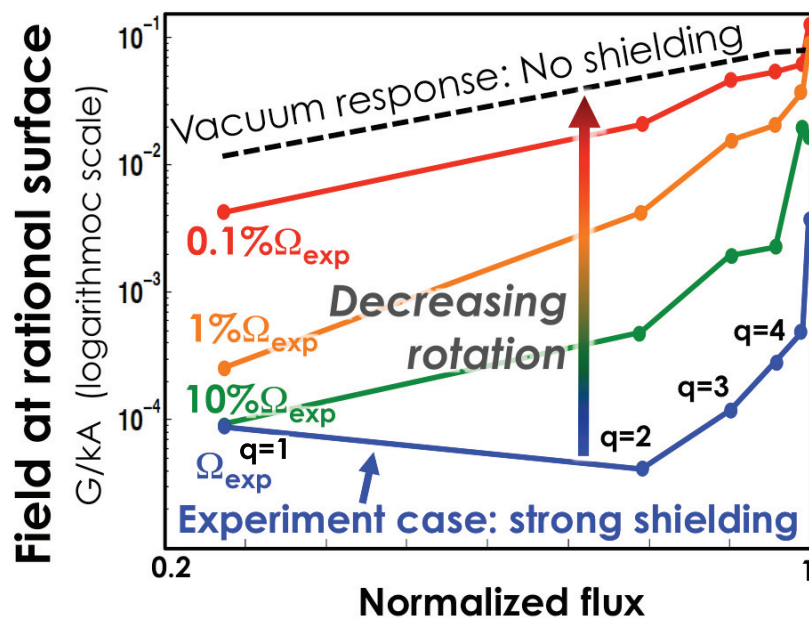
Understanding the plasma response...

– MARS-F modeling:

- *Is this about proximity to tearing β limit at low rotation?*

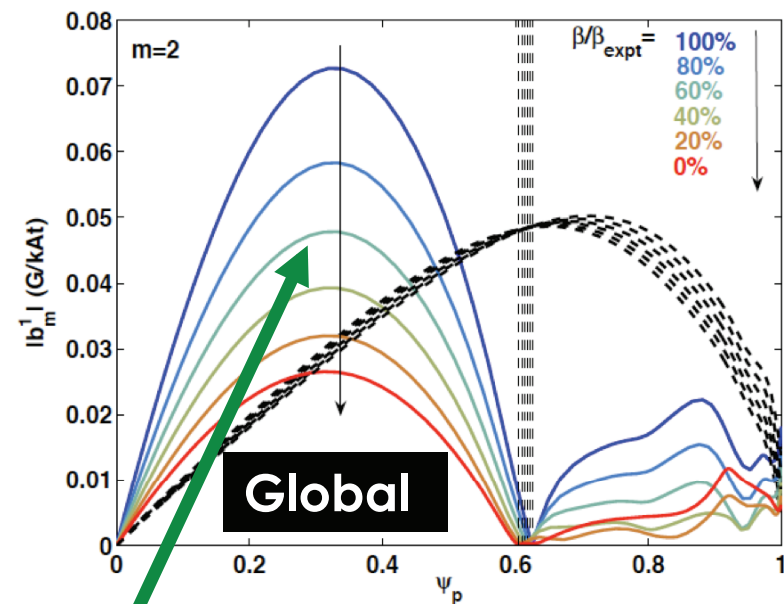
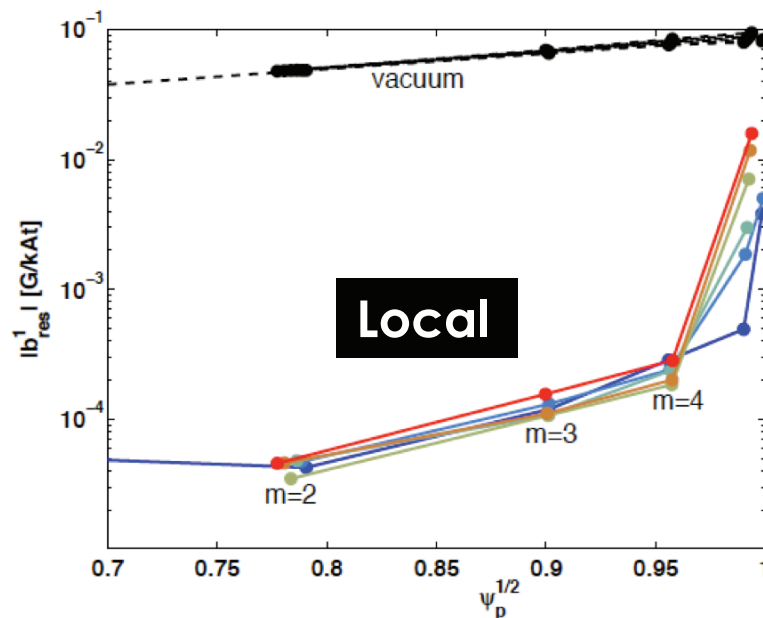
MARS-F Shows Local $q=2$ Response with Rotation but Global Response is Weak

- Magnetic probing results would require larger response across plasma to give observed x2 at sensor
 - *Is this just an artifact of linear nature of calculation?*
 - Non-linearly: breakdown of shielding will raise torque, change phase of response, and give more amplification
 - *Note all MARS modeling linear in next few slides...*



Beta Dependence in Response is the Expected Linearity in the High Rotation Base Case...

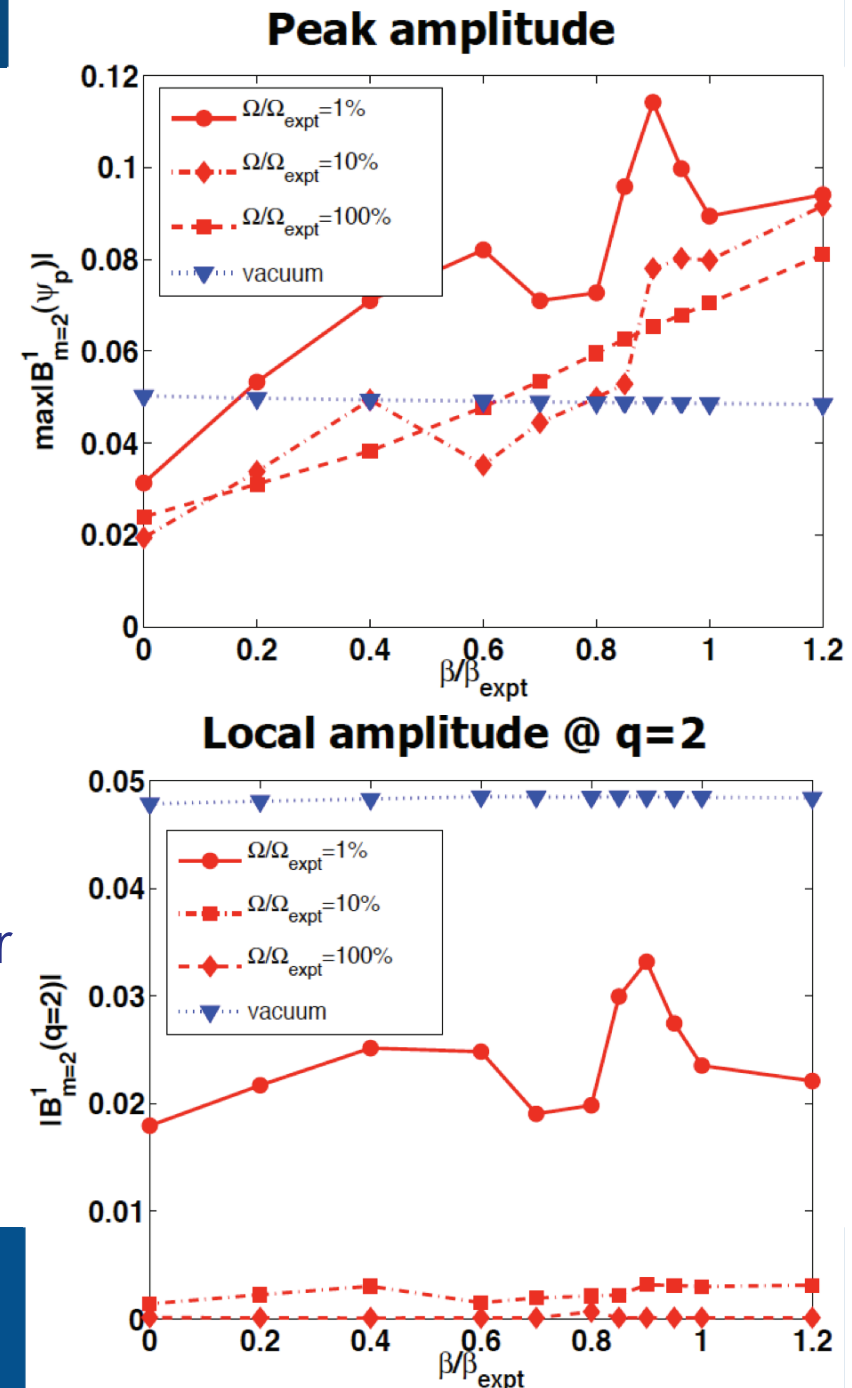
- Global response just scales with β
- Local residual field remains tiny
 - Strong shielding maintained at the high rotation of these points



Note peak values
– used next slide

But β Resonances Observed Close to Tearing β Limit if Rotation Dropped

- **Peak of response across plasma:**
 - Linear at high rotation (---)
 - Peaks near tearing β limit at low rotation (—)
- **Local $q=2$ response behaves similarly**
 - Proximity to tearing β limit changes plasma response due to partial breakdown of screening at low Ω
 - But global response hints at broader resonance close to tearing limit



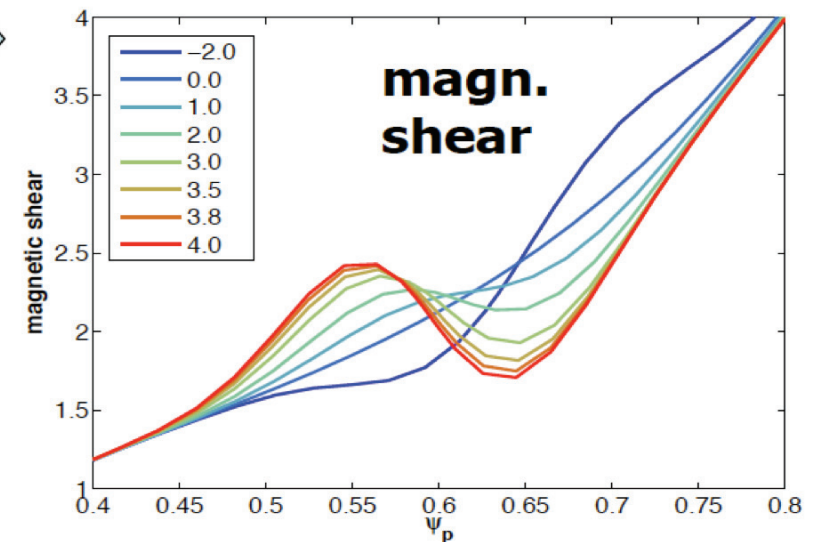
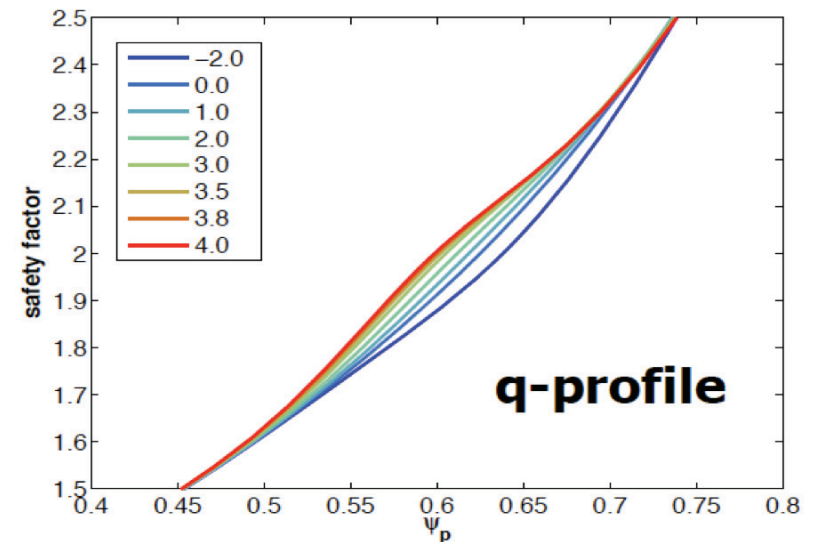
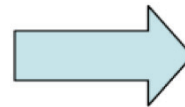
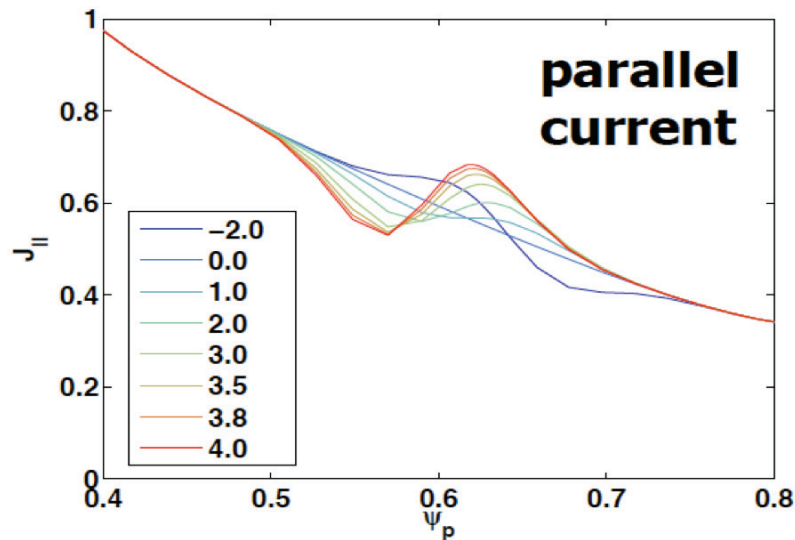
Is Delta-Prime Important?

Test with current profile changes:

$$J_{\parallel}^{new} = J_{\parallel} - aJ'_{\parallel q=2}(x - x_{q=2}) \exp\left[-\left(\frac{x - x_{q=2}}{b}\right)^2\right]$$

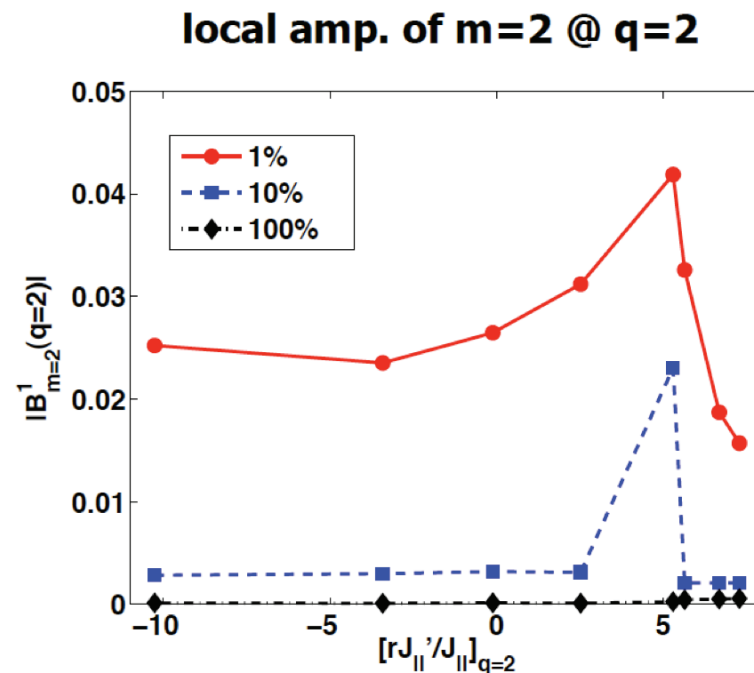
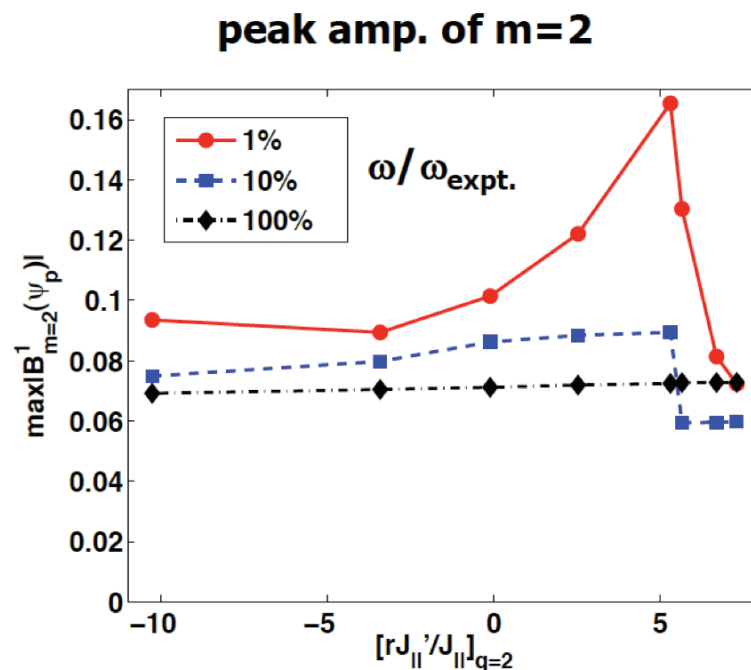
$$x = \sqrt{\psi_p}$$

Fix $b=0.05$, varying $a \rightarrow$
local variation of current density shear



Plasma Response to Current Profile Change

- High rotation once again insensitive to changes
- But low rotation opens the door to plasma response as screening breaks down
 - As expected [Fitzpatrick] current profile & rotation matter in the tearing resistive response



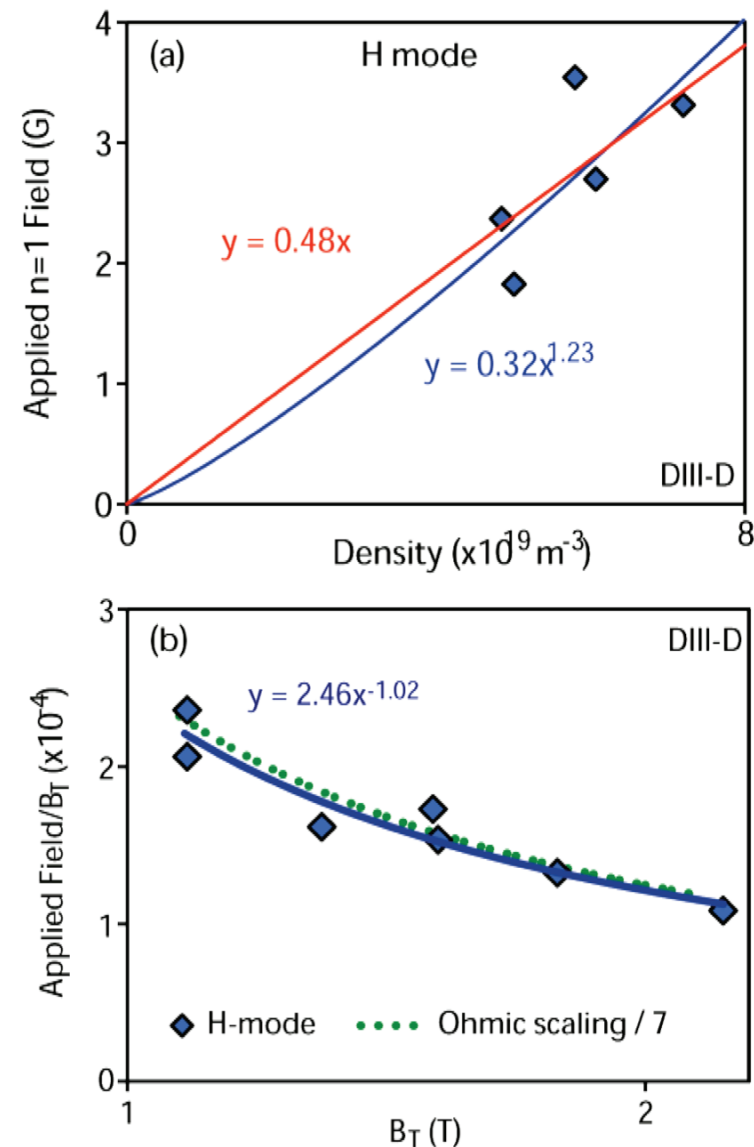
Moving on...

- So, low torque H modes exhibit an increased response to 3-D fields due ideal and resistive effects
 - Ideal: increases with β_N
 - Resistive: decreased screening at low rotation
 - Opens door to parameters governing tearing effects like Δ'
- This brakes the plasma to access natural tearing instability
- *What does this imply for error field sensitivity & tearing mode β limits in devices like ITER?*

Extrapolate to ITER by Measuring Density and B_T

Scaling of Threshold in Torque Free H-modes

- **ITER baseline-like SND at $\beta_N=1.8$** (but $q_{95}\sim 4.3$)
 - ITER heating systems low in torque
 - ‘torque-free’ reasonable approximation
 - Enables rotation to be treated as hidden variable
- **H mode scalings broadly consistent with previous Ohmic scalings...**
 - Linear in density (within error bars)
 - Inverse with B_T



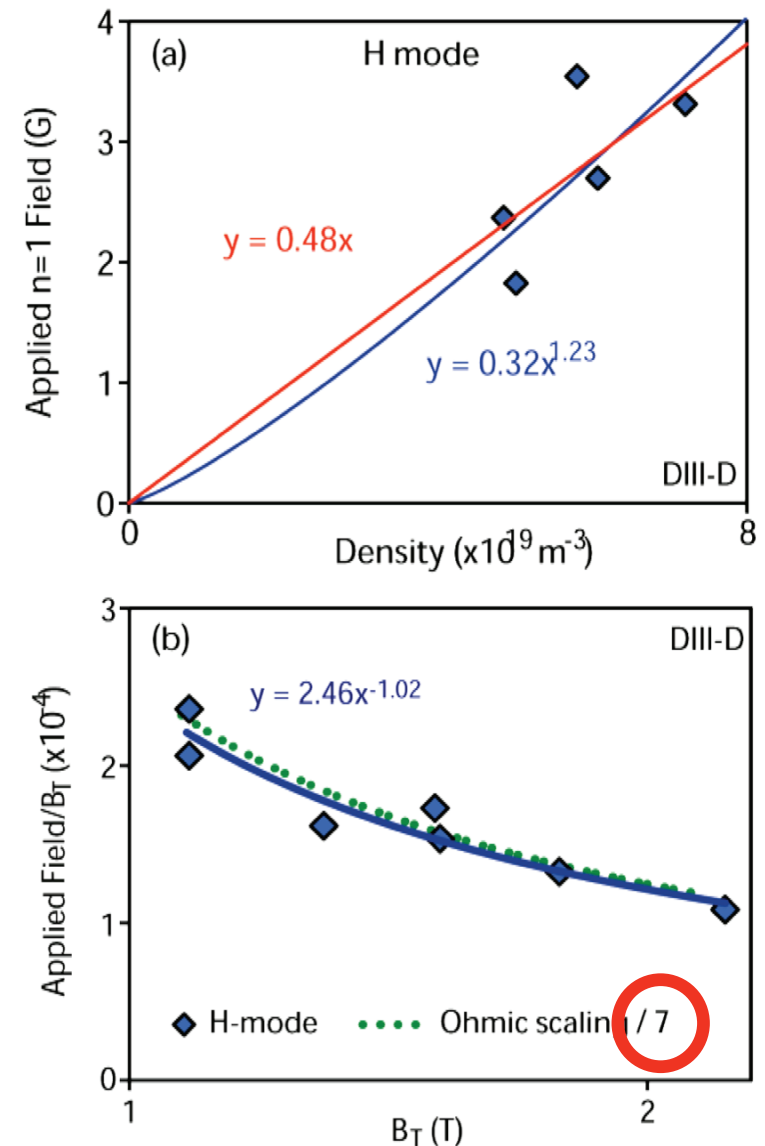
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But 7 times lower threshold !

- **As expected of course:**
 - Increased ideal & resistive response
 - More braking to trigger mode



New ITER H mode Error Field Threshold Scaling

Infer size scaling from dimensional invariance to obtain:

$$\frac{B_{pen}}{B_T} = (1.72 - [\beta_N - 1.8]) \times \frac{\left(n_e / 10^{20} m^{-3}\right) (R / 6.2m)^{0.725}}{(B_T / 5.3T)^{1.02}} \times 10^{-4}$$

- DIII-D threshold of 1.4×10^{-4} scales to 1.7×10^{-4} in ITER
- Lower than projections for ITER low density Ohmic phase
 - Ohmic threshold of 2.9×10^{-4} for I-coil-like fields in these variables

Note: ITER was designed to minimize $m=1,2,3$ fields

- *We now understand $m=4-8$ are key harmonics driving ideal response*

Important to re-evaluate ITER's error field and its correction in the relevant parameters for the ITER baseline scenario

Conclusions

- **Plasma resistive response becomes important in low torque H modes close to tearing stability limits**
 - Error fields open the door to tearing β limit via braking & a decrease of resonant screening
- **New threshold scalings predict error fields are a major concern for torque free H modes, even at low β_N**
 - Implications for ITER & future low rotation devices
 - Manipulating q profile and rotation will help