

Sawtooth Control

SD Pinches¹

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* See the Appendix of F Romanelli et al., IAEA FEC Geneva 2008

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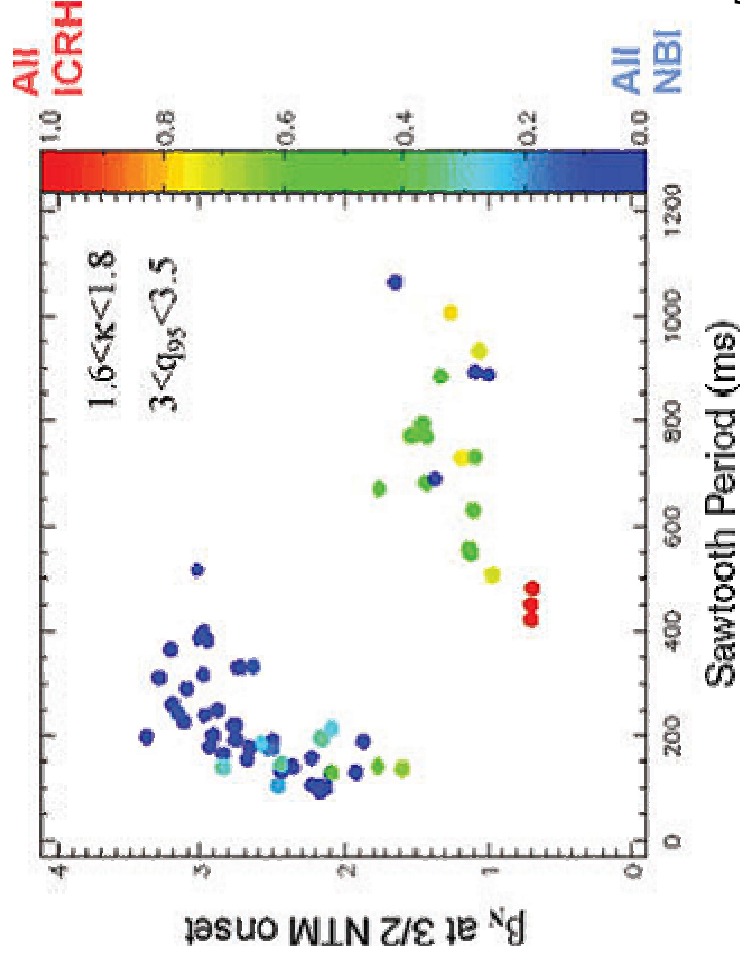
Why do we need to control sawteeth?

EFDA

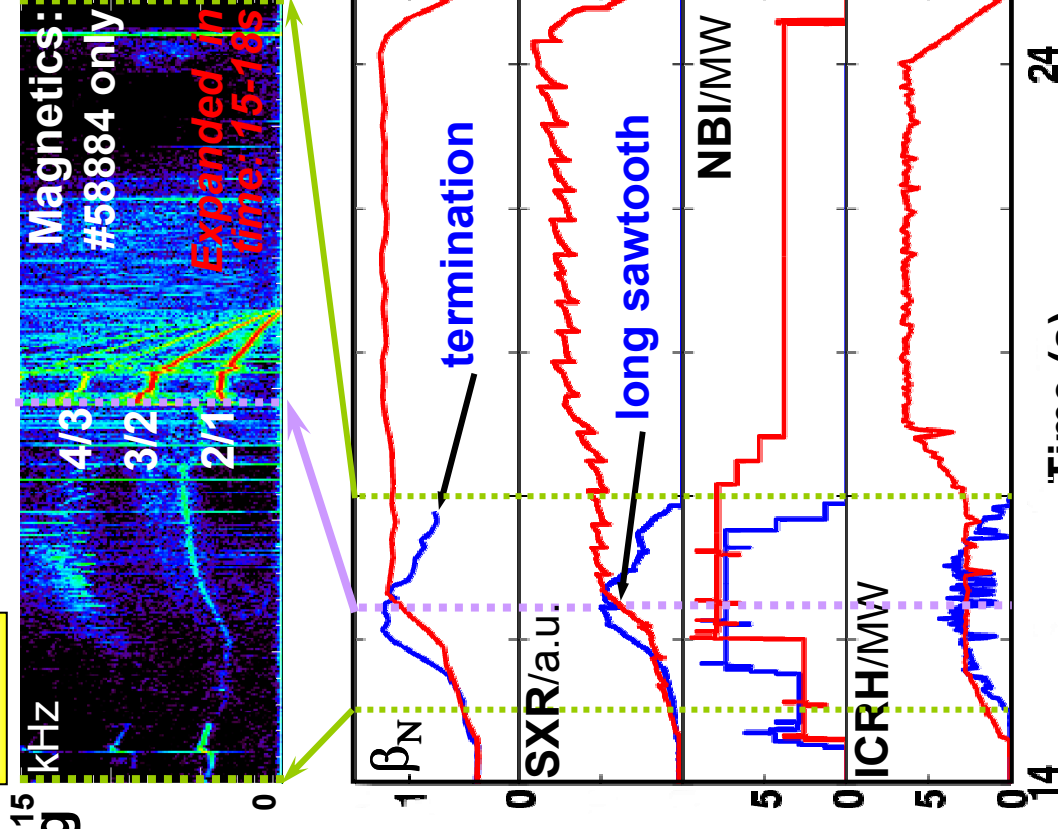
- Long Period Sawteeth have been shown to trigger Neo-classical Tearing

Modes (NTMs)

- Long Sawteeth $\rightarrow$ NTMs
- Short Sawteeth $\rightarrow$ Avoid NTMs



JET



Time (s)

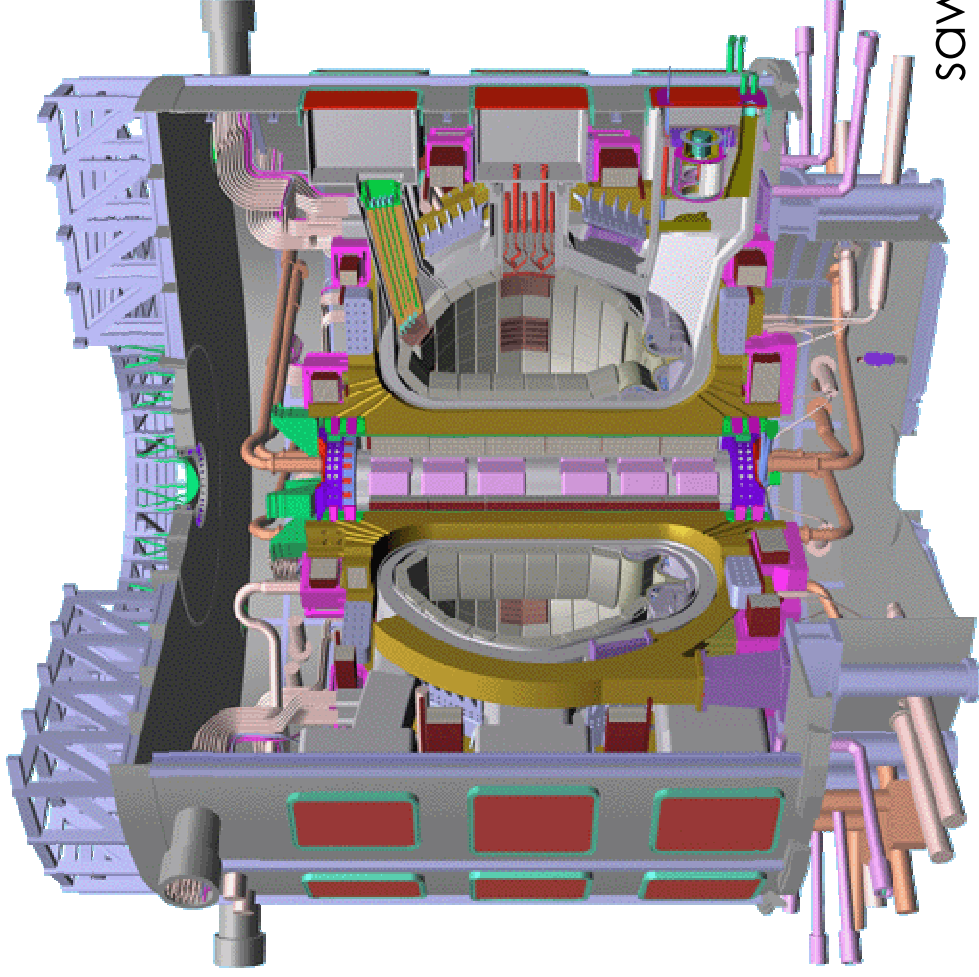


[Buttery, IAEA FEC, EX/7-1, 2004]

[Sauter et al, PRL, **88**, 2002]

Sawteeth are a bigger problem in ITER

- NTMs degrade plasma confinement or even cause terminations



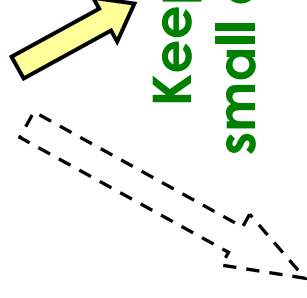
ITER will have lots of fusion-born alpha particles in the core



Long sawtooth periods



Trigger NTMs and cause confinement degradation



Keep sawteeth small and frequent

Deliberately stabilise sawtooth so it's longer than the pulse – is this possible?

Outline – Sawtooth Control

- **Motivation**
 - Sawteeth can trigger Neo-Classical Tearing Modes (NTMs)
 - Methods for Sawtooth Control
- **Developments in our understanding of sawtooth stability**
 - Co/Counter NBI Experiments on JET, MAST and TEXTOR
 - Effect of passing ions and sheared flows
- **Sawtooth Control Using Off-axis Co-NBI**
 - Experiments on JET, MAST and ASDEX Upgrade
- **Sawtooth Control Using ICRH**
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When will a sawtooth crash happen?

- Sawtooth is triggered when one of following criteria is met

[Porcelli et al, PPCF, 38, 2163 (1996)]

- Resistive instability:

$$\pi \frac{\delta \hat{W}}{s_1} < c_\rho \frac{\rho}{r_1} \quad \begin{array}{l} \text{Change in potential energy} \\ \text{of internal kink mode} \end{array} \quad \begin{array}{l} \text{Ion Larmor radius} \\ \text{Radius of } q=1 \text{ surface} \end{array}$$

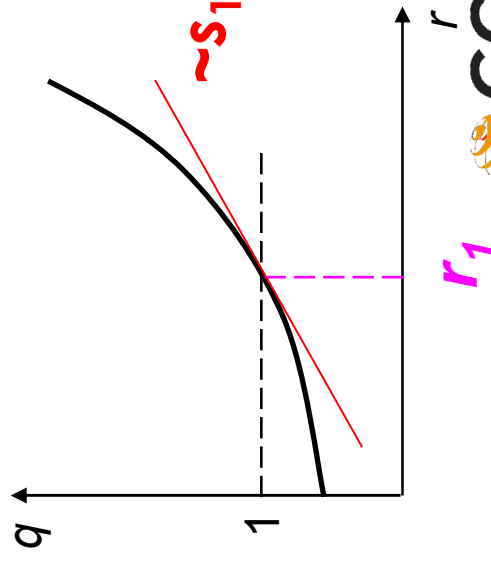
Magnetic shear at $q=1$ surface

$$\pi \frac{\delta \hat{W}}{s_1} < -\frac{\omega_{*i} \tau_A}{2}$$

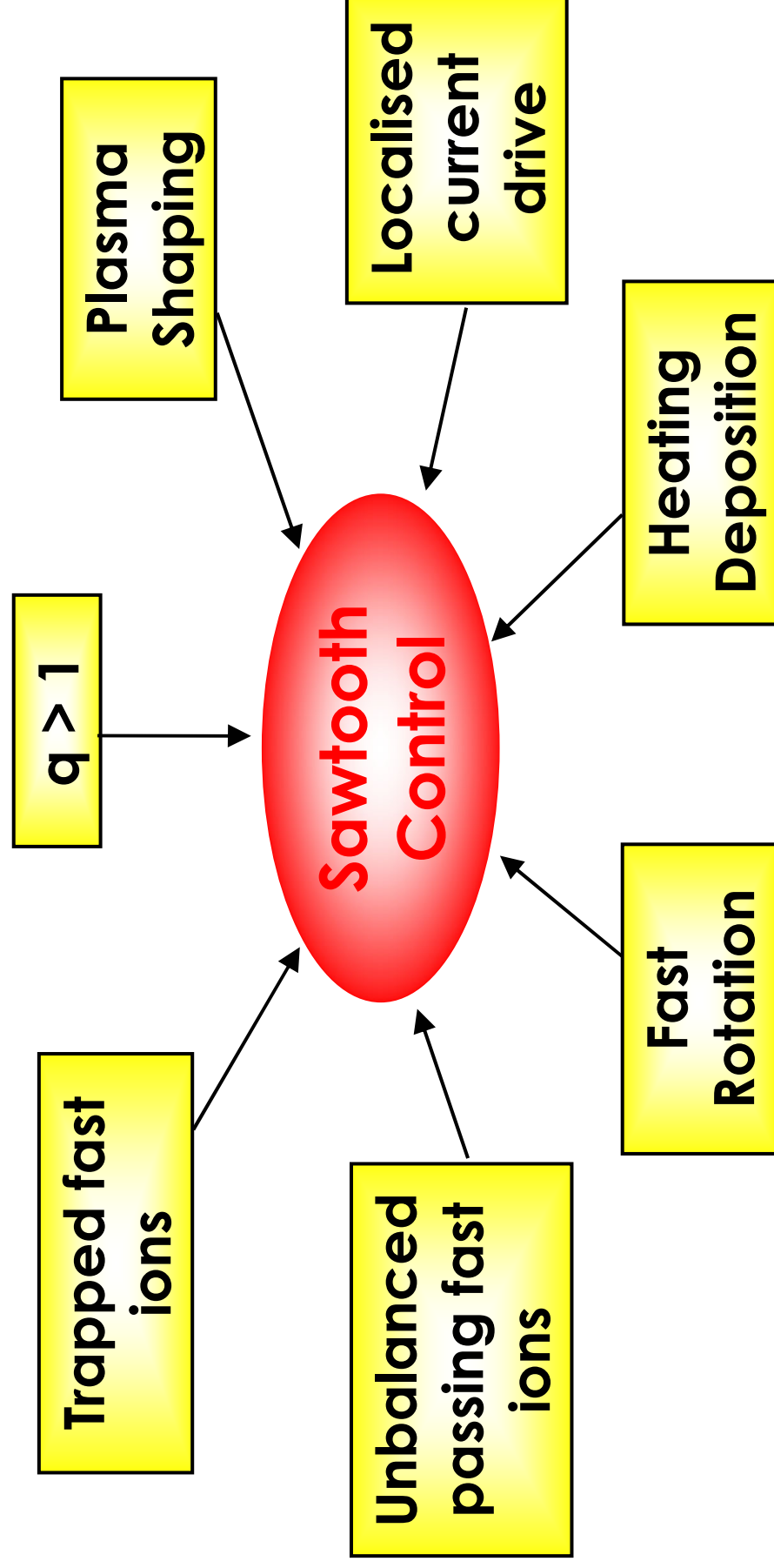
- Ideal Instability:

- So a sawtooth crash occurs when:

- The potential energy of the kink mode is sufficiently small
- The magnetic shear at $q=1$ is sufficiently large



How can we control sawtooth?

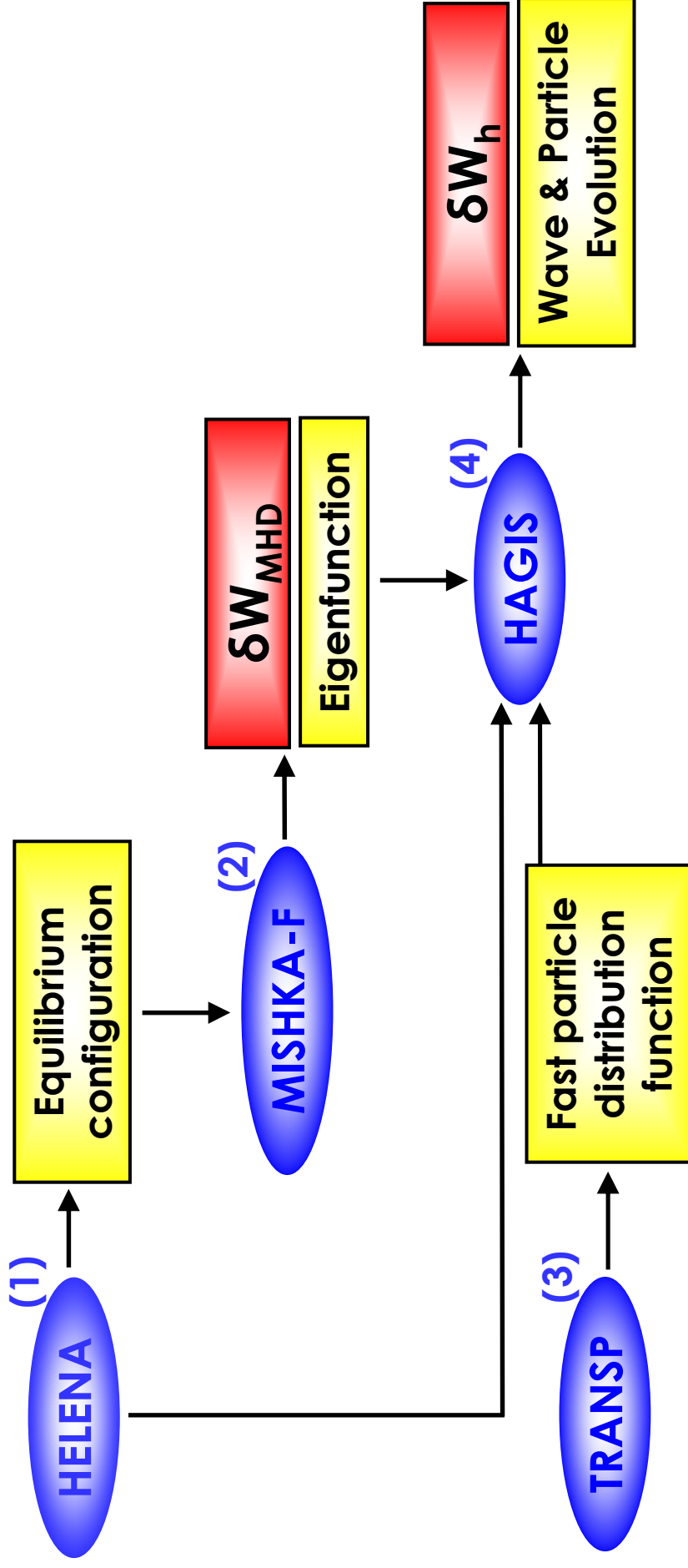


- **Two main techniques:**

- Drive current near $q=1$ surface to change magnetic shear
- Introduce energetic ions to change mode potential energy

Modelling Sawtooth Stability

- Model Stability of $n=1$ internal kink mode



(1) Huysmans et al, CP90 Conf on Comput Phys, p371 (1990)

(2) Chapman et al, Phys Plasmas, **13**, 062511 (2006)

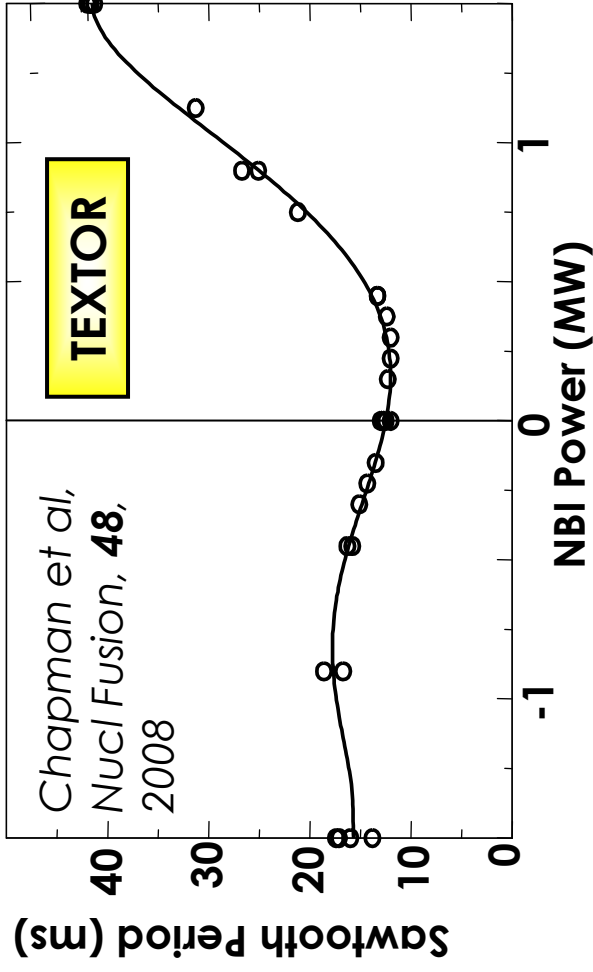
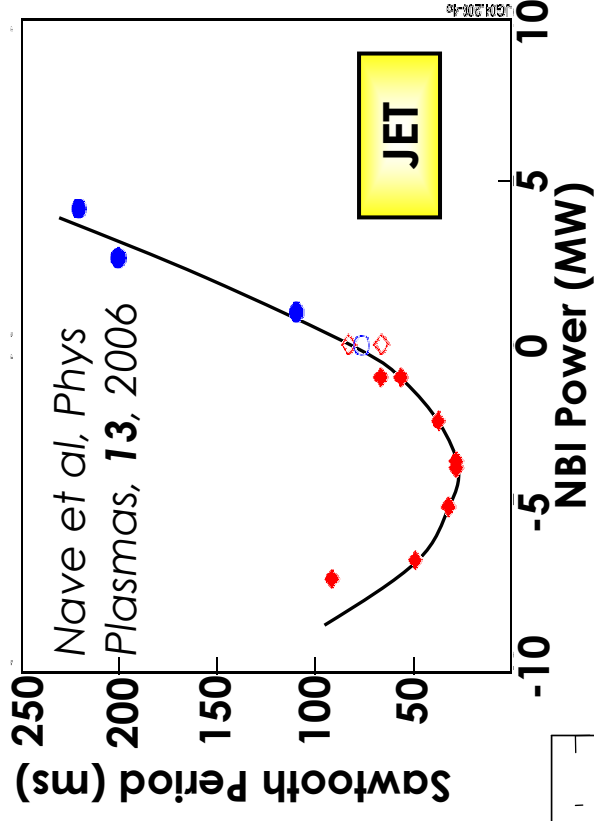
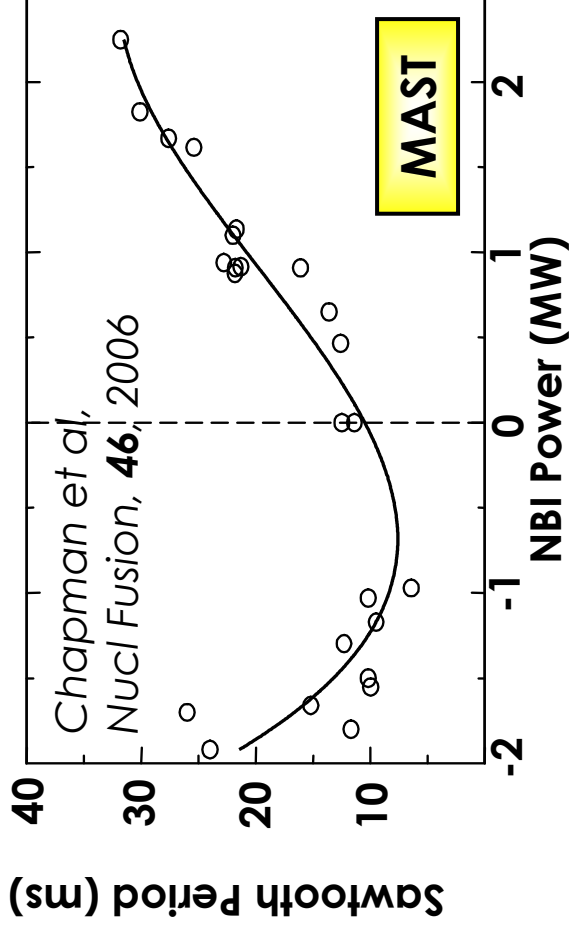
(3) Budny et al, Nucl Fusion, **32**, 429 (1992)

(4) Pinches et al, Comput Phys Commun, **111**, 133 (1998)

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Asymmetry in NBI-heated plasmas

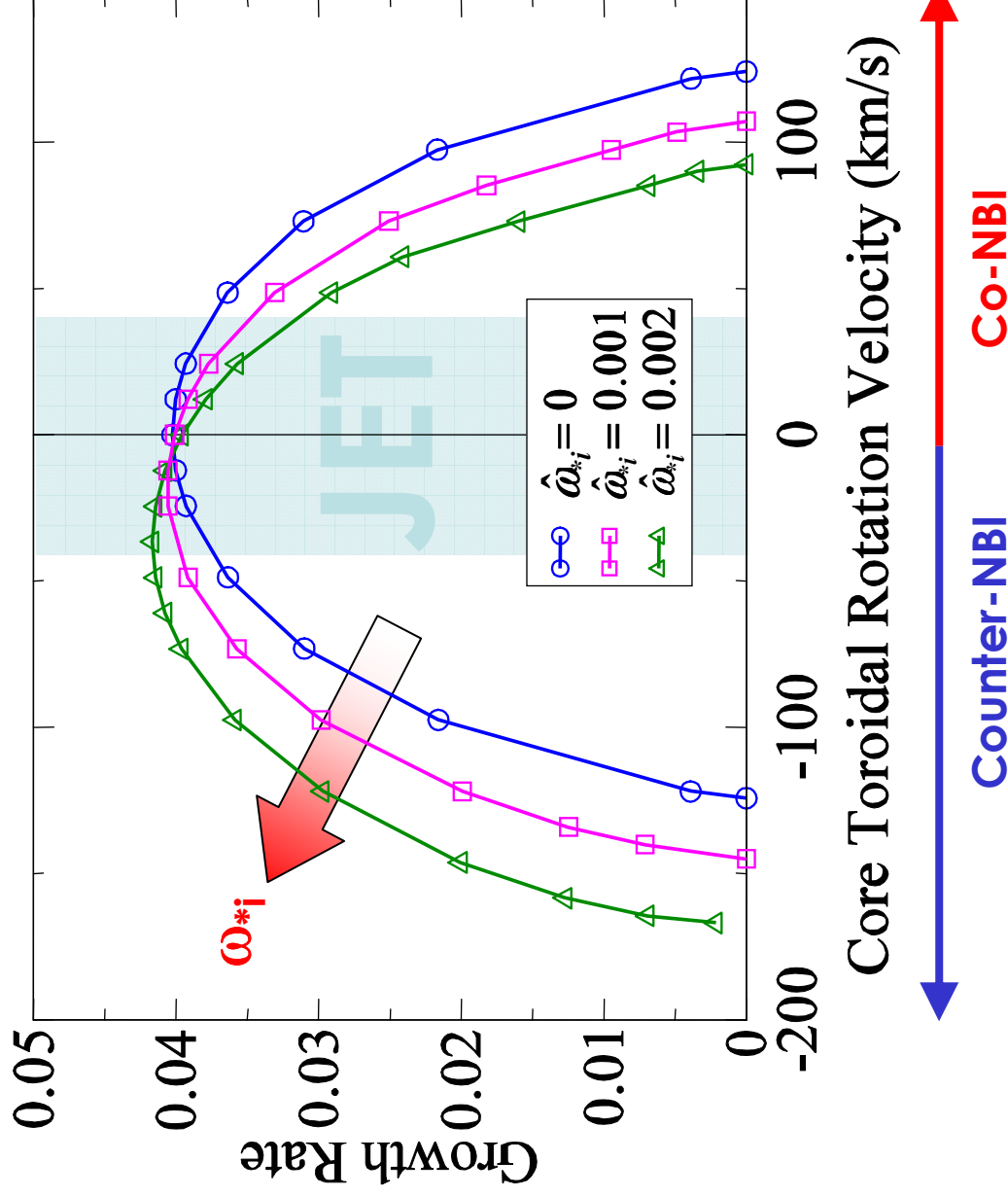


Counter-NBI Co-NBI

- Co v Counter Studies
 - Asymmetric behaviour
 - Minimum is not in Ohmic plasmas

Stability of $n=1$ kink mode at finite ion diamagnetism

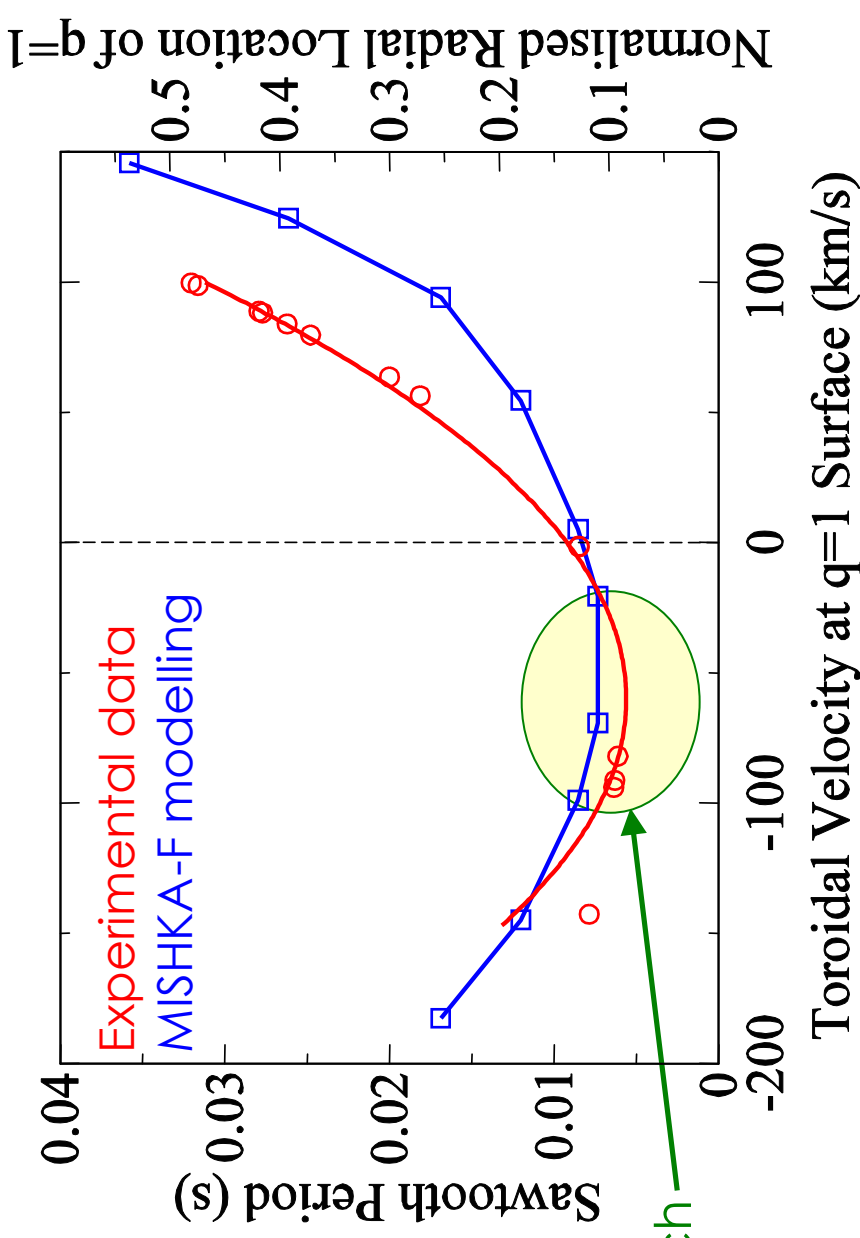
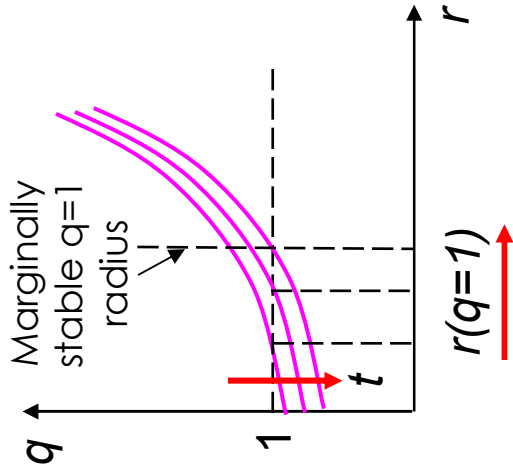
- Modelled the effect of toroidal flow on the ideal $n=1$ internal kink mode with finite ion diamagnetic frequency in MAST:



Modelling sawtooth stability with flow in MAST



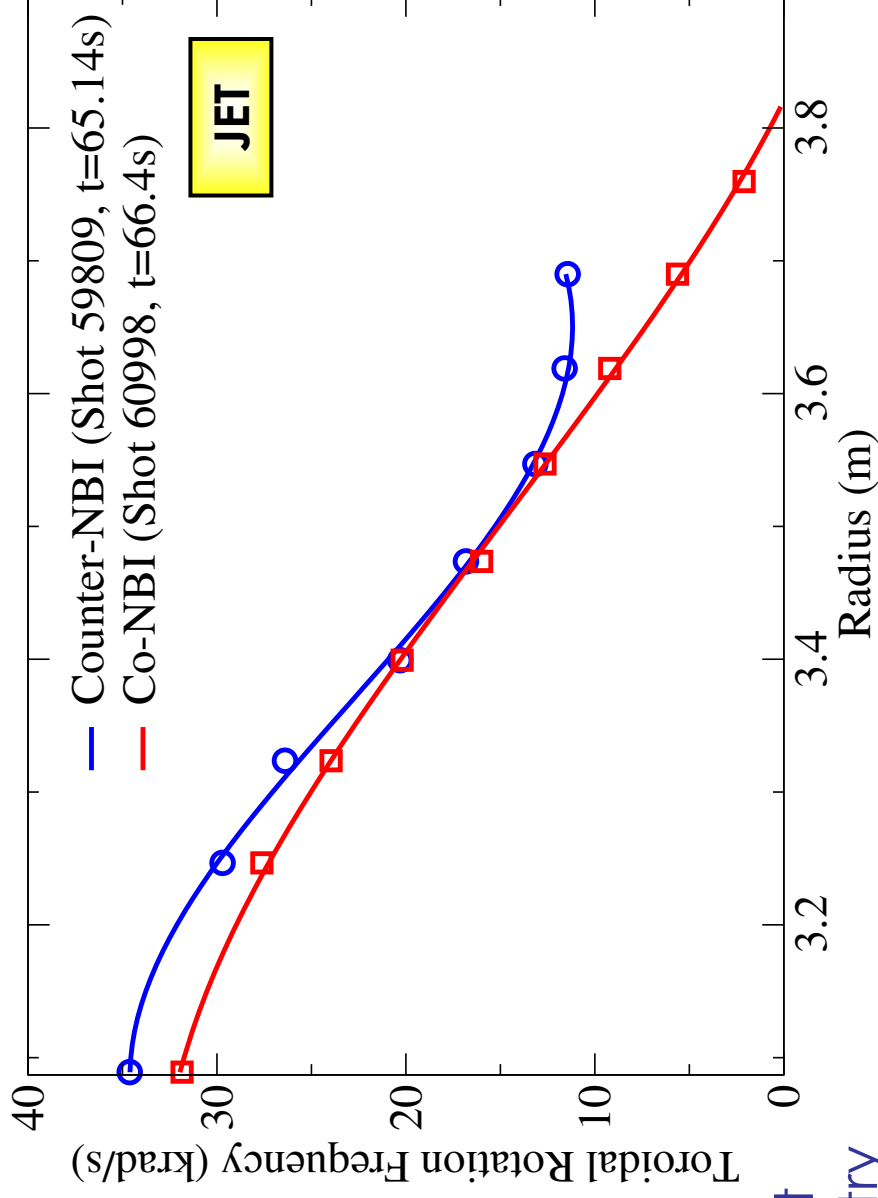
- **Kink mode stabilised by strong toroidal rotation**
 - As sawtooth period, τ_{st} , increases, radial location of $q = 1$ increases
 - Marginally stable $q = 1$ radius expected to correlate with τ_{st}



- Toroidal Rotation is an order of magnitude smaller than MAST

- Much **slower** **rotation speeds** than **MAST**, only small effect on stability of kink mode
- Strong flow **shear** at radial location of $q=1$ (compared to MAST)

⇒ At slower flows, what causes the asymmetry in sawtooth period in JET experiments?



(Rotation Profiles from Charge Exchange)

What is the rôle of trapped and passing particles?

- Sawtooth stabilisation by energetic particles is usually attributed to the presence of trapped fast ions [Porcelli, PPCF, 33, 1991]

- In JET, fast beam ions are

mainly passing

- Passing ions can be stabilising when co-NBI, but destabilising when counter-NBI.

[Graves, PRL, 92, 2004]

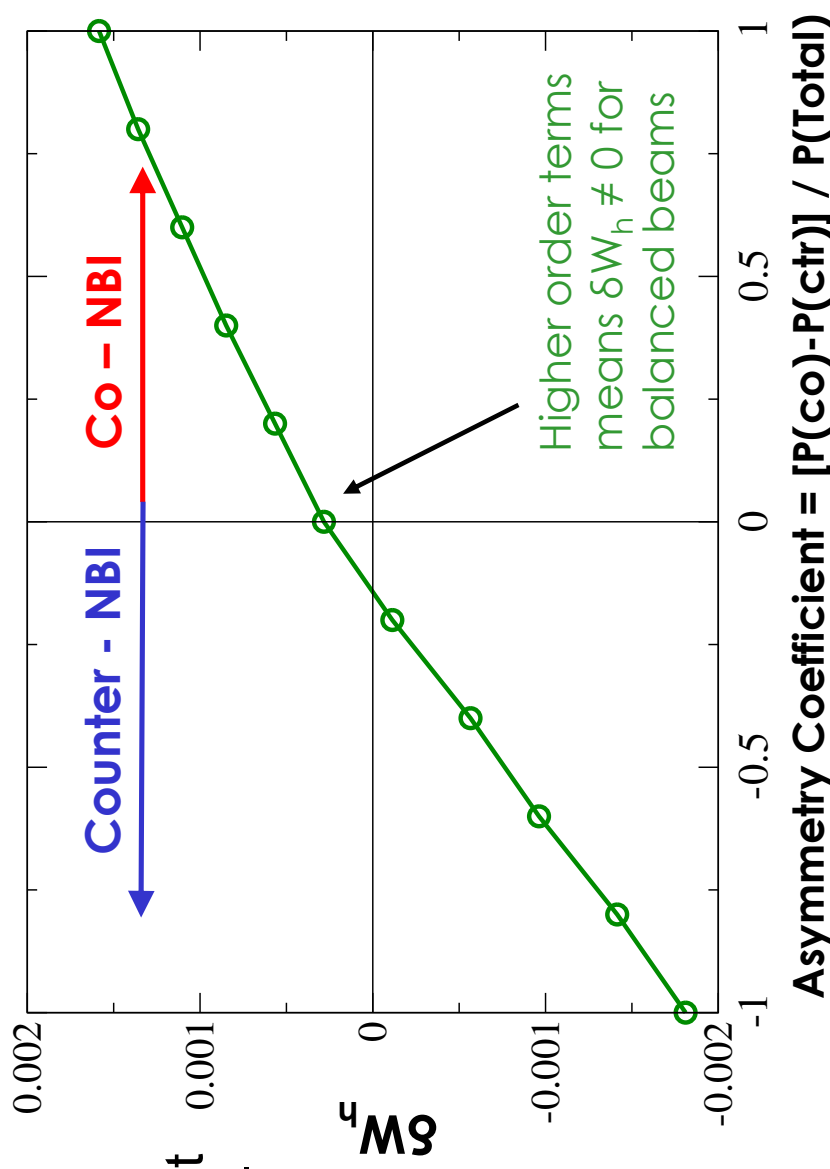
$$\sum_{\alpha} \epsilon_{\alpha}$$

- **HAGIS code**

- Drift Kinetic code for exploring wave-particle interactions
- Calculates change in potential energy:

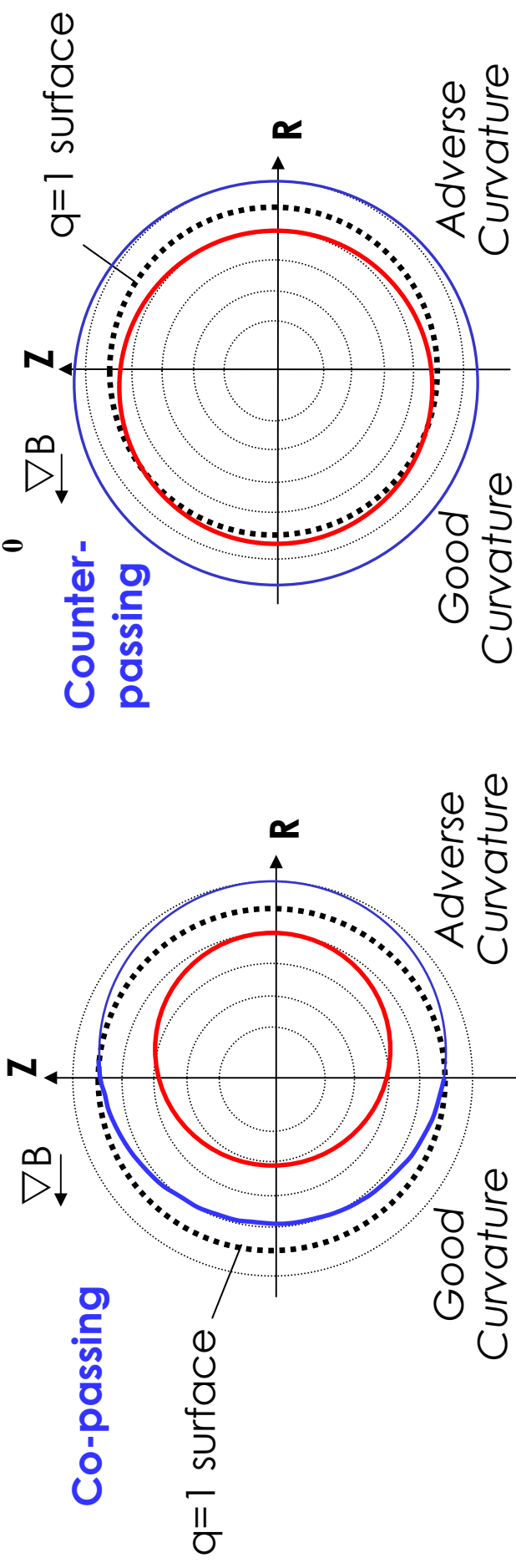
$$\delta W_h = \frac{1}{2} \int (mv^2 + \mu B) \delta \kappa \cdot \xi^* d^3x d^3v$$

Pinches, CPC, 111, 1998



Passing Particle Stabilisation Mechanism

δW has a term dependent upon curvature: $\delta W \sim - \int_0^{r_1} (\xi \cdot \nabla \langle P_h \rangle) (\xi \cdot \kappa) dr$

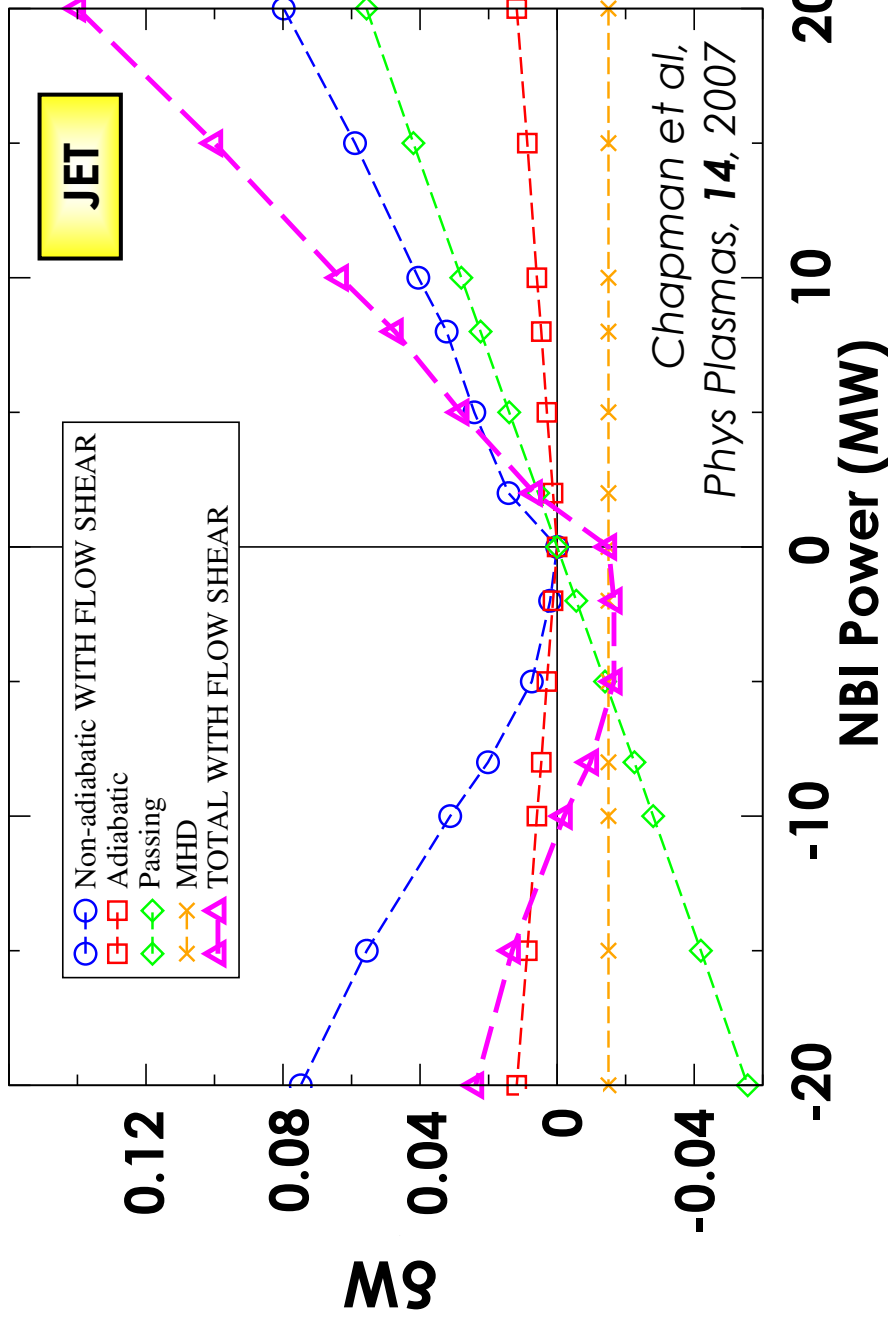


Co-pass, $\langle P_h \rangle' |_{r_1} < 0 \rightarrow$ stabilising
 Co-pass, $\langle P_h \rangle' |_{r_1} > 0 \rightarrow$ destabilising
 Ctr-pass, $\langle P_h \rangle' |_{r_1} < 0 \rightarrow$ destabilising
 Ctr-pass, $\langle P_h \rangle' |_{r_1} > 0 \rightarrow$ stabilising

- Increasing effective orbit width leads to large passing ion effect
 - Large thermal velocity (NNBI, ICRH)
 - Large fraction of barely passing ions (JET NBI, ICRH)

Do passing fast ions explain JET result (low rotation)? EFDA JET

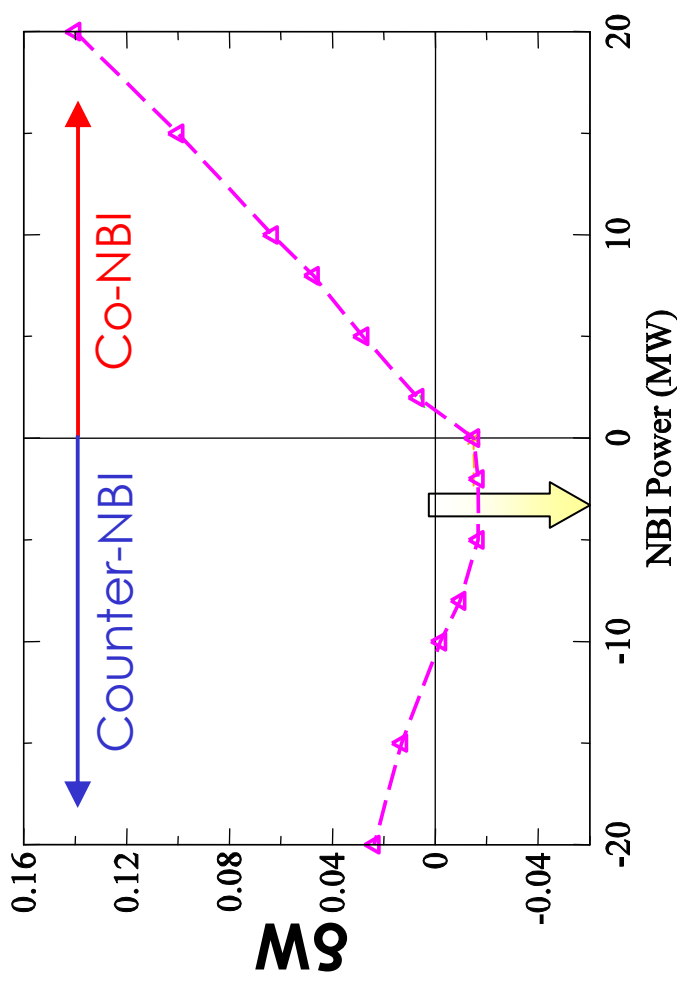
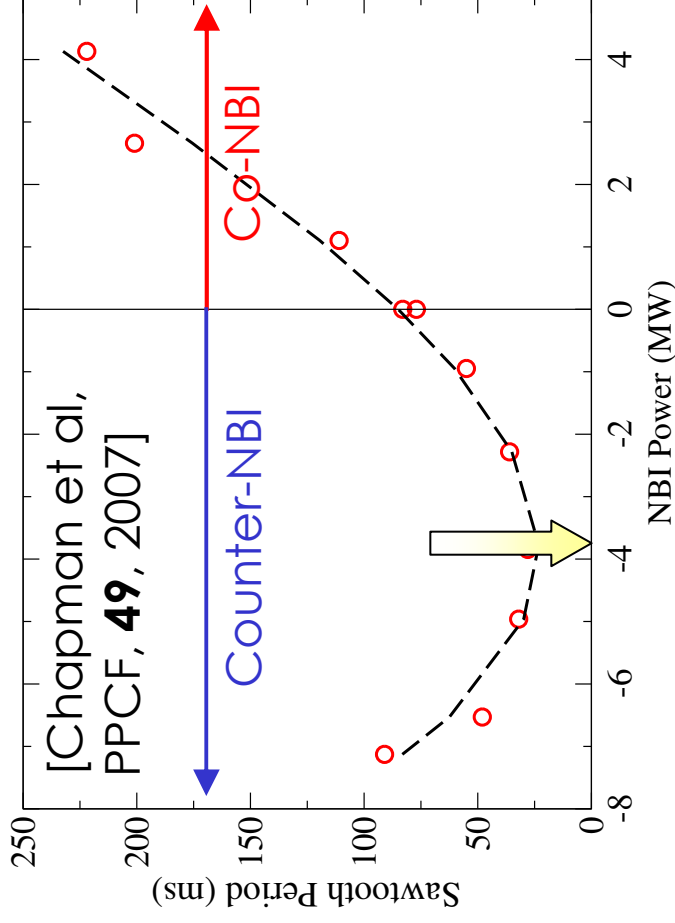
- Modelling the effect of fast ions on $n=1$ kink mode



- New understanding about fast ions and sawtooth behaviour:

- Passing fast ions play a key role (low v_ϕ & NBCD) [Graves PRL 2004]
- Effect of trapped ions influenced by flow shear [Graves PPCF 2000]

How does it compare to experiment? EFDA JET

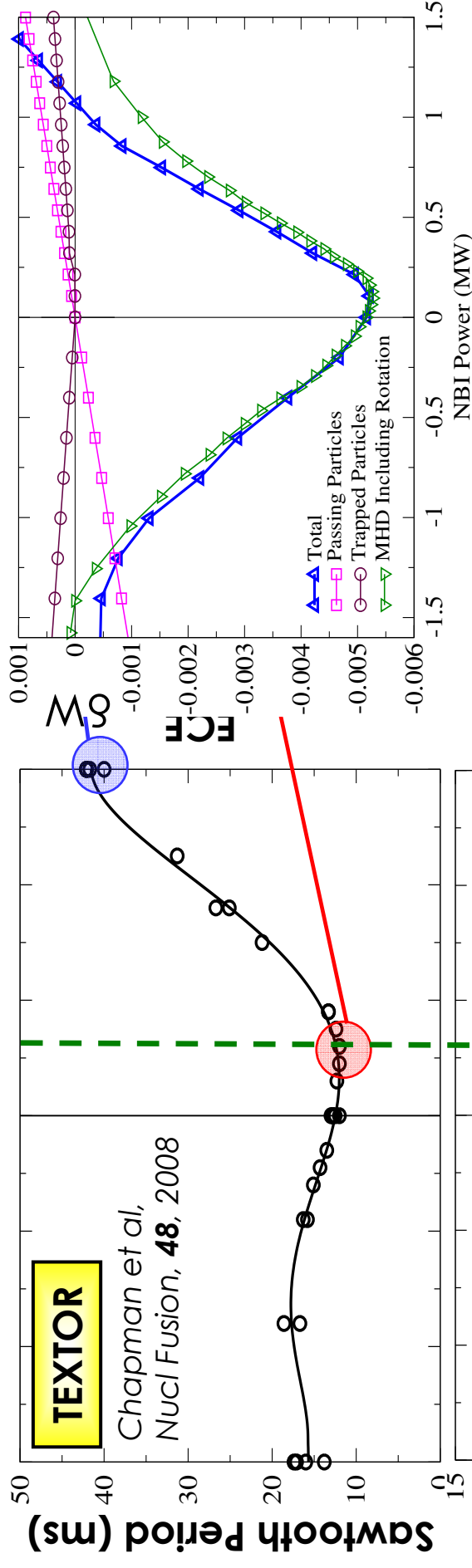


- Minimum in sawtooth period and δW_h agrees well (at $\sim 4\text{MW}$)
- In **JET**, asymmetry and minimum is explained by **energetic particle effects**
- In **MAST**, asymmetry and minimum is explained by **flow effects**

Sawtooth Behaviour with NBI in TEXTOR



• TEXTOR exhibits different sawtooth behaviour with NBI



- Minimum in sawtooth period when plasma rotation stops (precursor frequency $\rightarrow 0$)
- Minimum τ_{ST} occurs when NBI rotation balances intrinsic flow
- Counter-passing fast ions destabilise kink mode & dominate when flow tends to upper limit



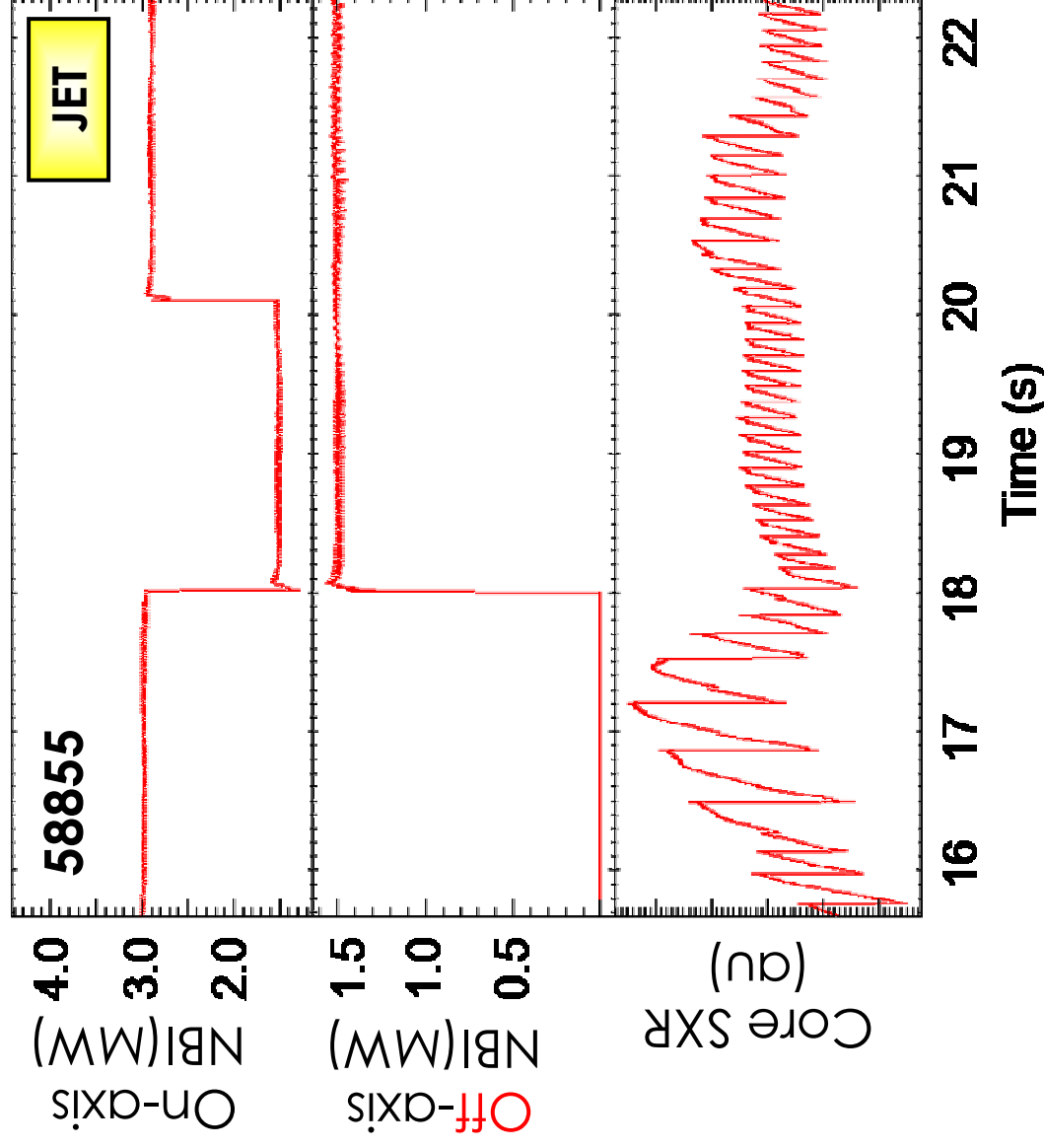
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Sawtooth Control Using Off-Axis Co-NBI EFT-4

- Sawtooth period can be shortened by applying off-axis NBI

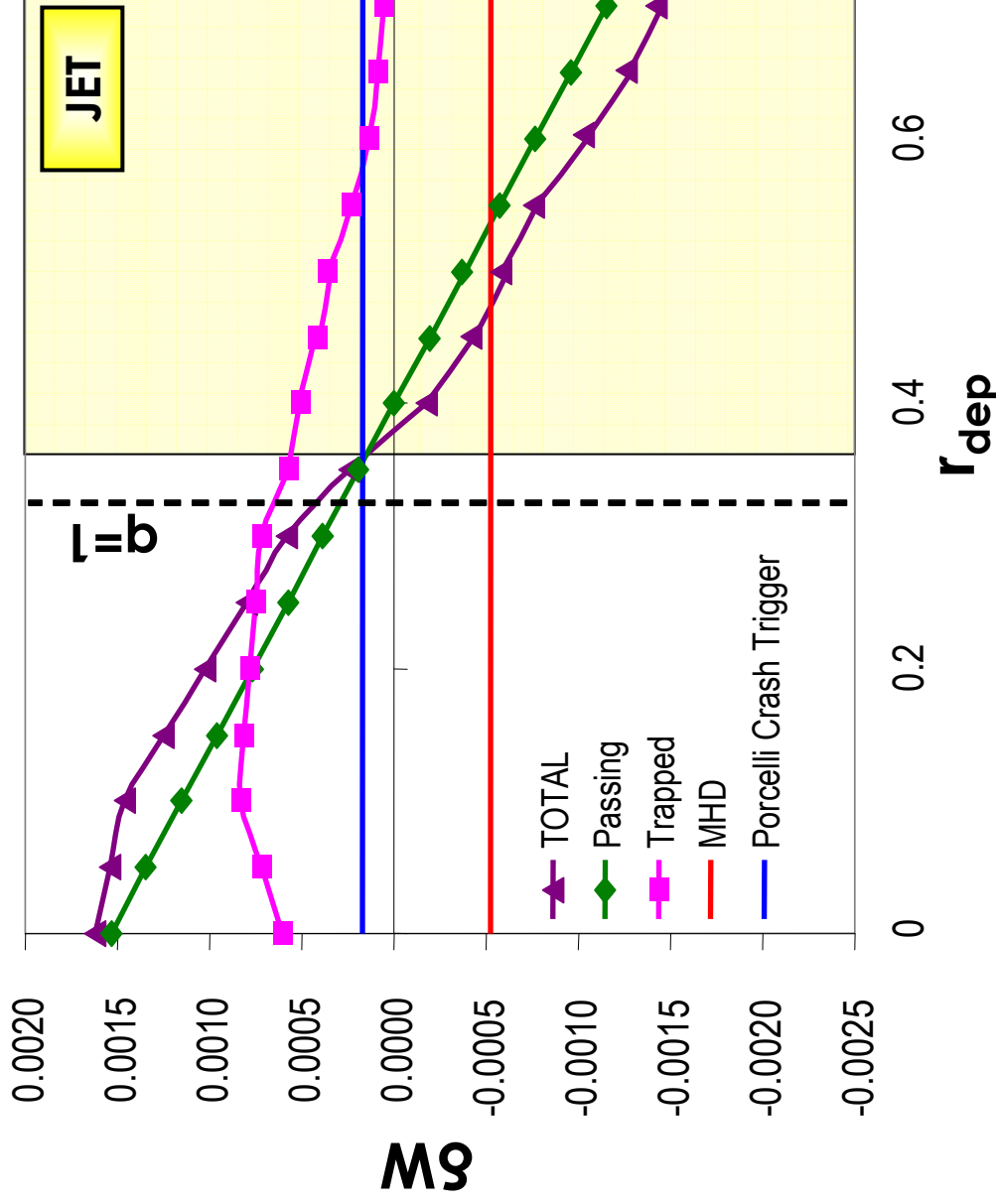


- Off-axis NBI can control sawteeth which have been stabilised by on-axis NBI
- Explained by destabilising contribution from passing fast ions born outside $q=1$
- Modelling shows fast ion effects dominate and NBCD effect is very small

[Chapman et al, Nucl Fus **49** 2009]

Modelling Off-axis NBI Effects

- Move deposition location of peak of fast ion distribution wrt $q=1$
 - When fast ions peaked just outside $q=1$, kink mode unstable

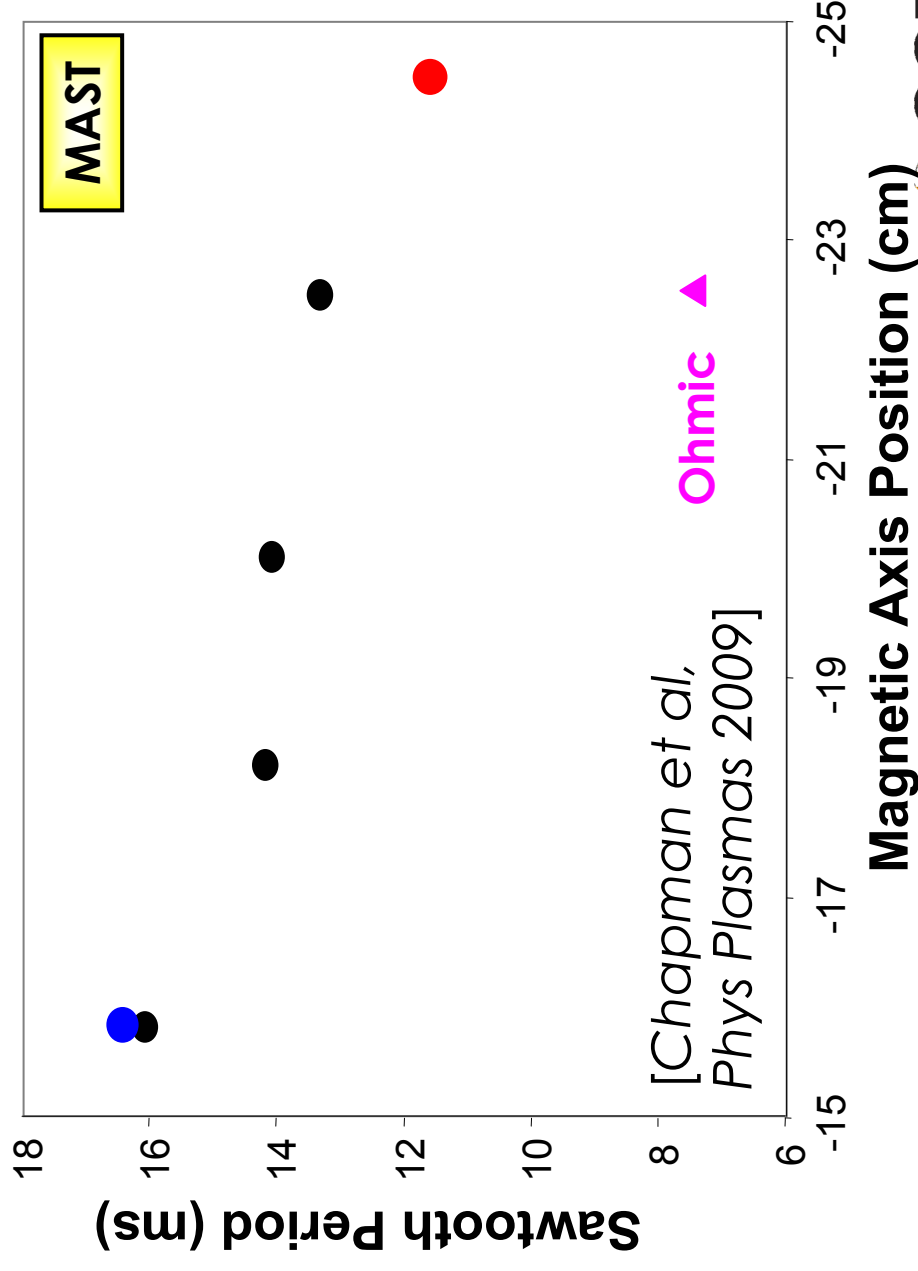
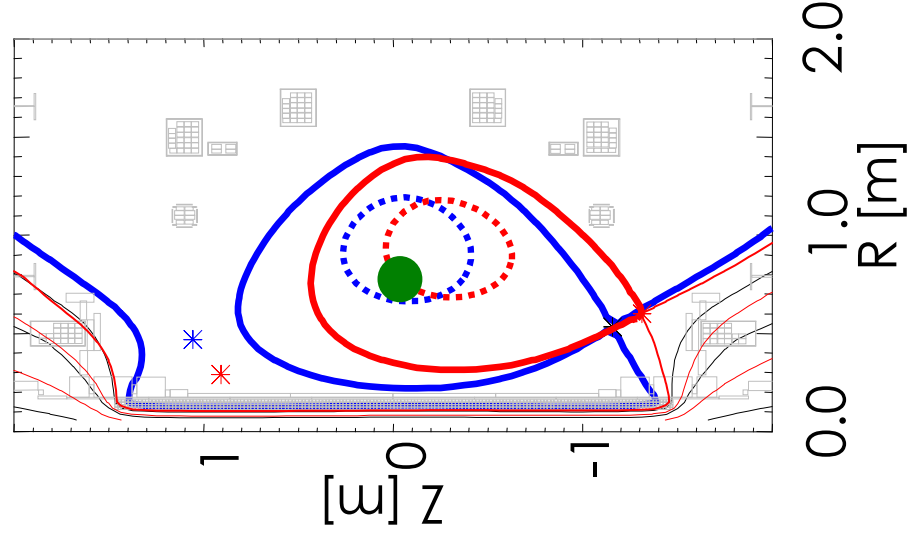


Chapman et al,
PPCF, 50, 2008

Off-axis NBI Effects in MAST



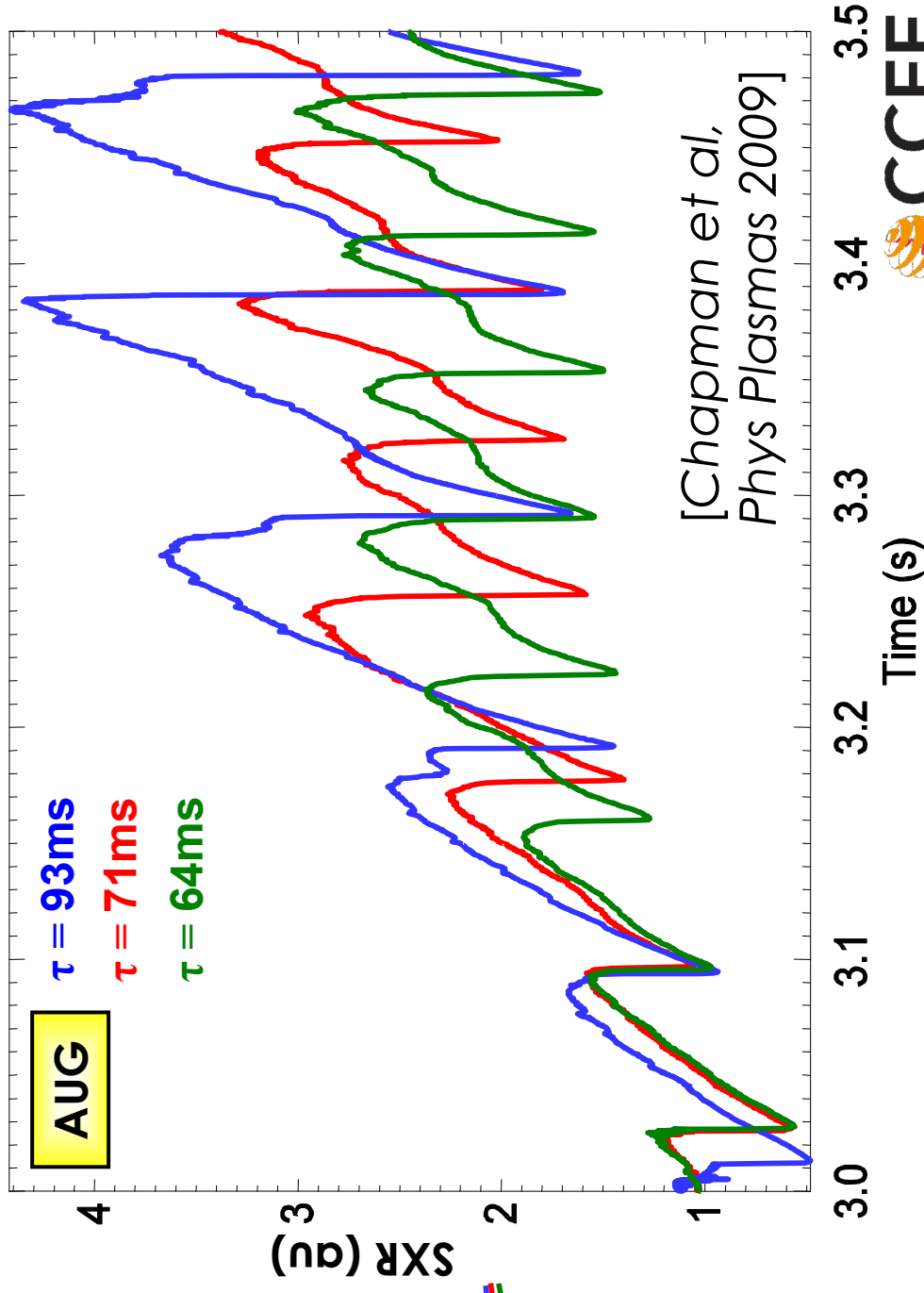
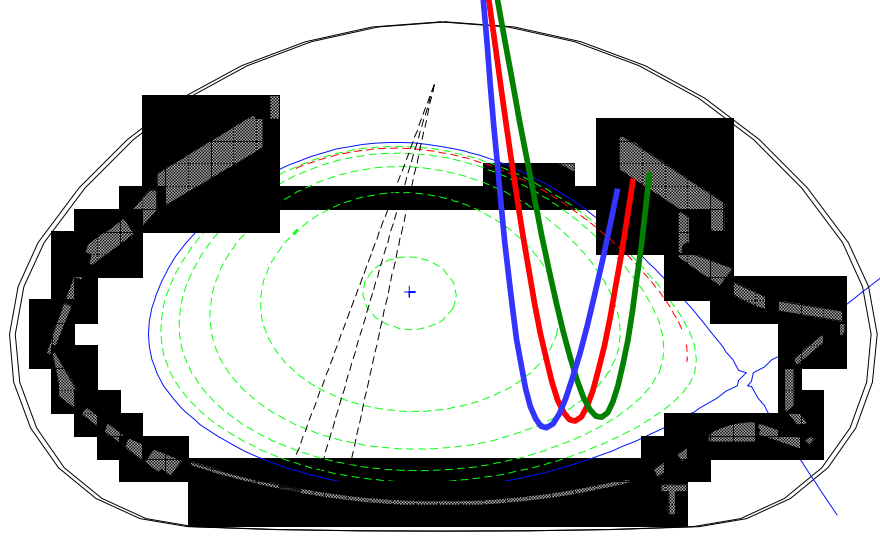
- Scan the deposition location by moving plasma vertically
 - Sawtooth behaviour affected by deposition location relative to $q=1$
 - Passing ion effects dominate over change in NBCD, v_ϕ , shape etc



Off-axis NBI Effects in ASDEX Upgrade

IPP

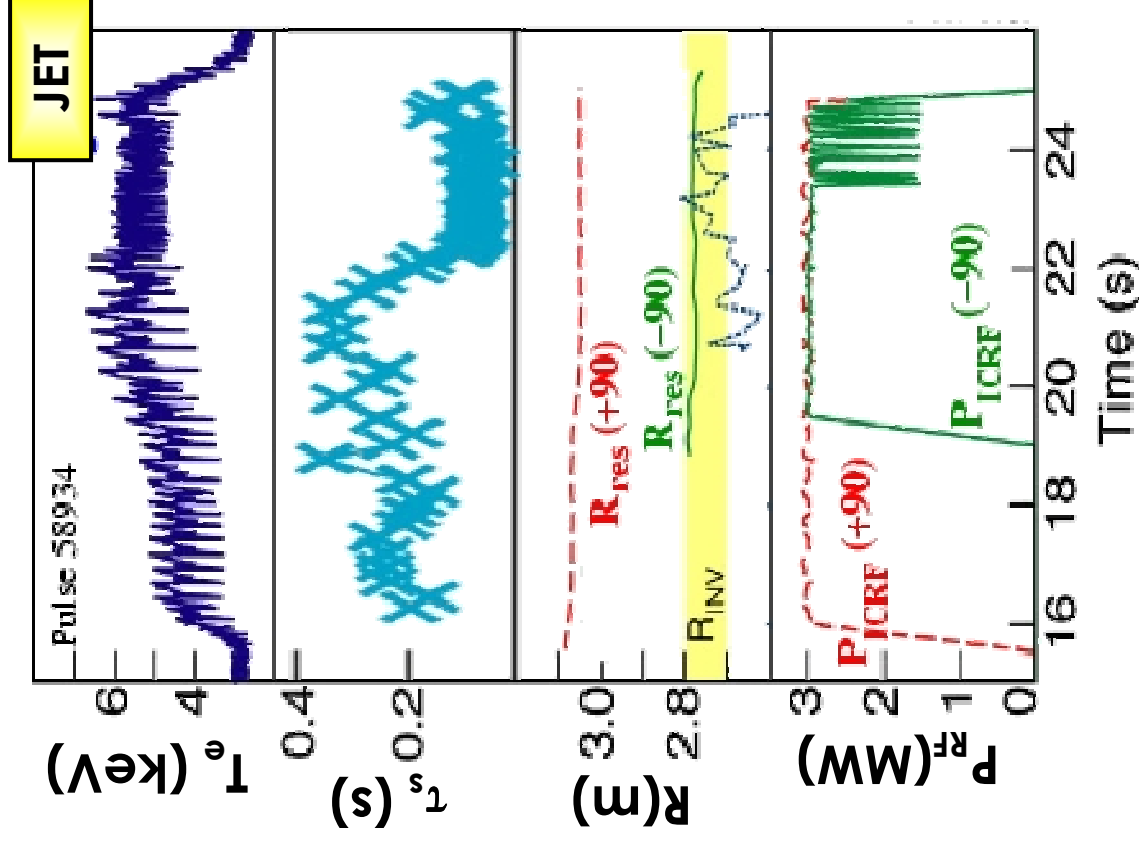
- Off-axis NBI affects sawtooth behaviour
 - As f_h moves further outside $q=1$, τ_s decreases by ~50%
 - Modelling again shows passing ions dominate over NBCD



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ICRH Sawtooth Control in JET EPJEA



- On Axis ICRH strongly stabilises sawteeth due to hot trapped ions [Campbell, White, Porcelli et al]
- Off Axis Counter-propagating ICRH (-90) destabilises long sawteeth (which were stabilised by on-axis fast ion population)
- Initially **expected** that control mechanism would be from **shear modification at $q=1$**
- Modelling of recent JET discharges [Coda, EPS 2007] confirms that change to shear from -90 ICRH is typically small

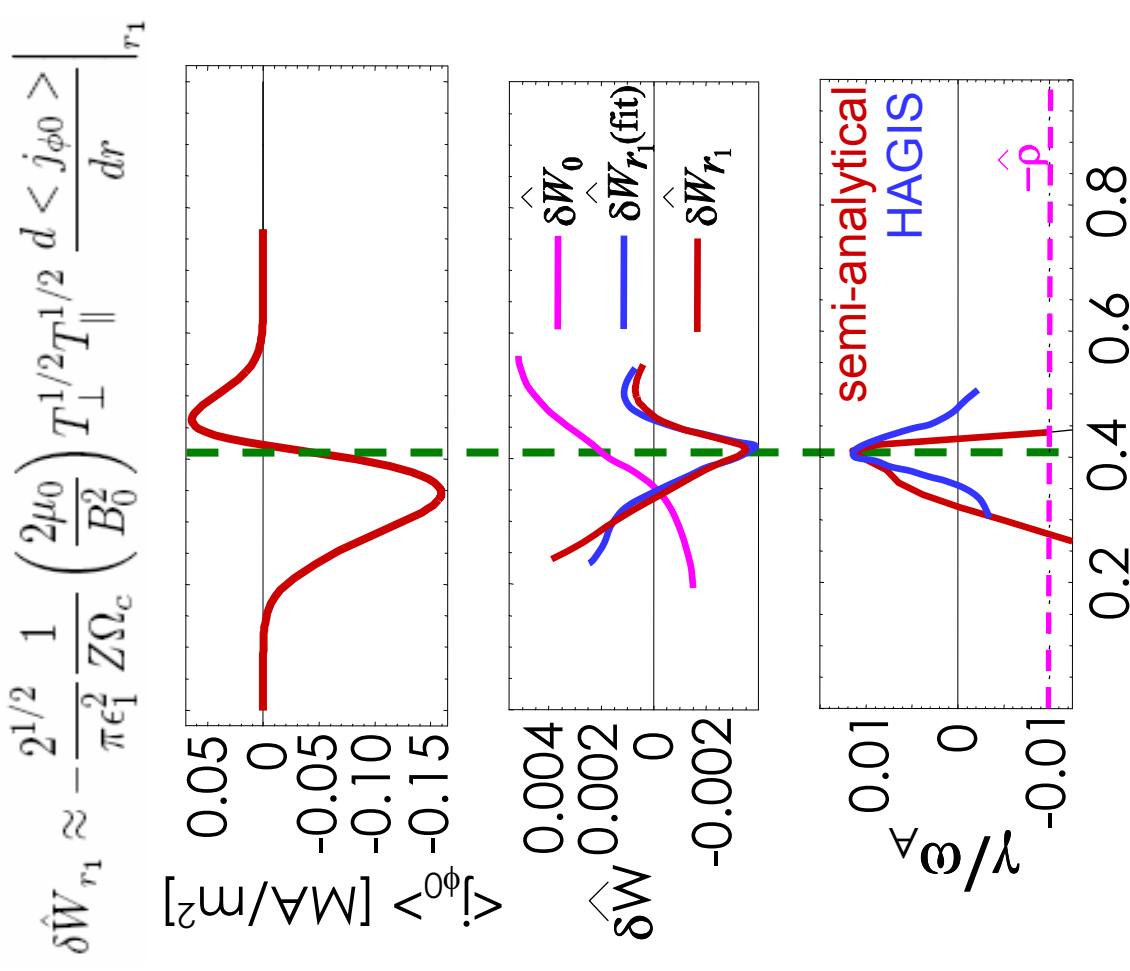
Eriksson, PRL, **92**, 235004 (2004)

- New theory shows that **control is determined by the asymmetry in $v_{||}$ of passing ion distribution**

- Fast ion growth rate is proportional to the radial gradient of the passing fast ion current density profile at $q=1$

- Results confirmed using SELFO code (for f_h^{RF}) and HAGIS (for δW)

- In He³ minority scenarios in ITER an **electron drag current** results in small change to shear but **does not affect fast ion mechanism** [Laxåback, *Nucl Fusion*, **45** 2005]

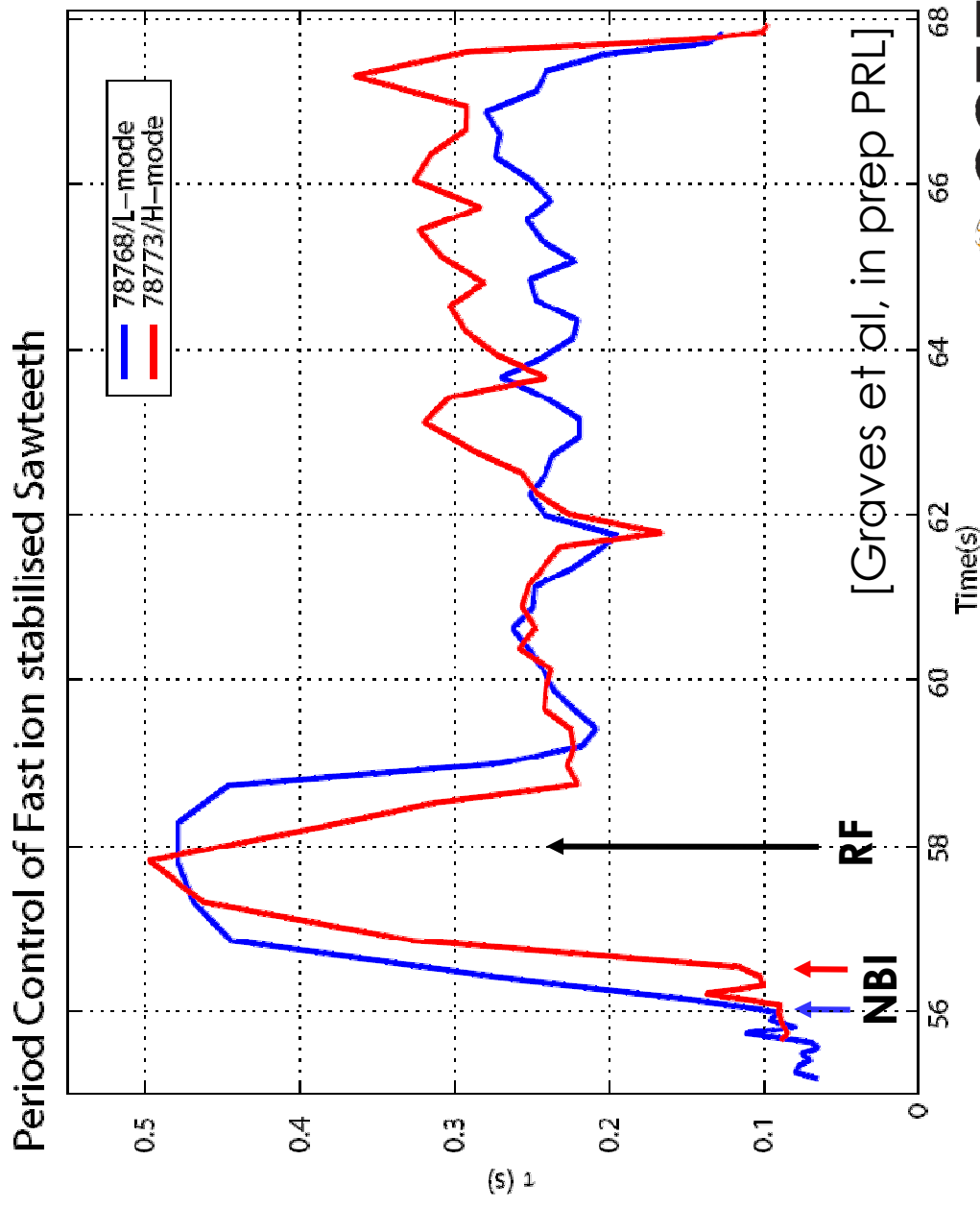


Sawtooth Control with ICRH in JET (and ITER?) EFDA

- **Control with ICRH shown to be fast ion effect**
 - Use ^3He minority as electron drag results in negligible ICCD

- **Can significantly destabilise long period sawteeth**

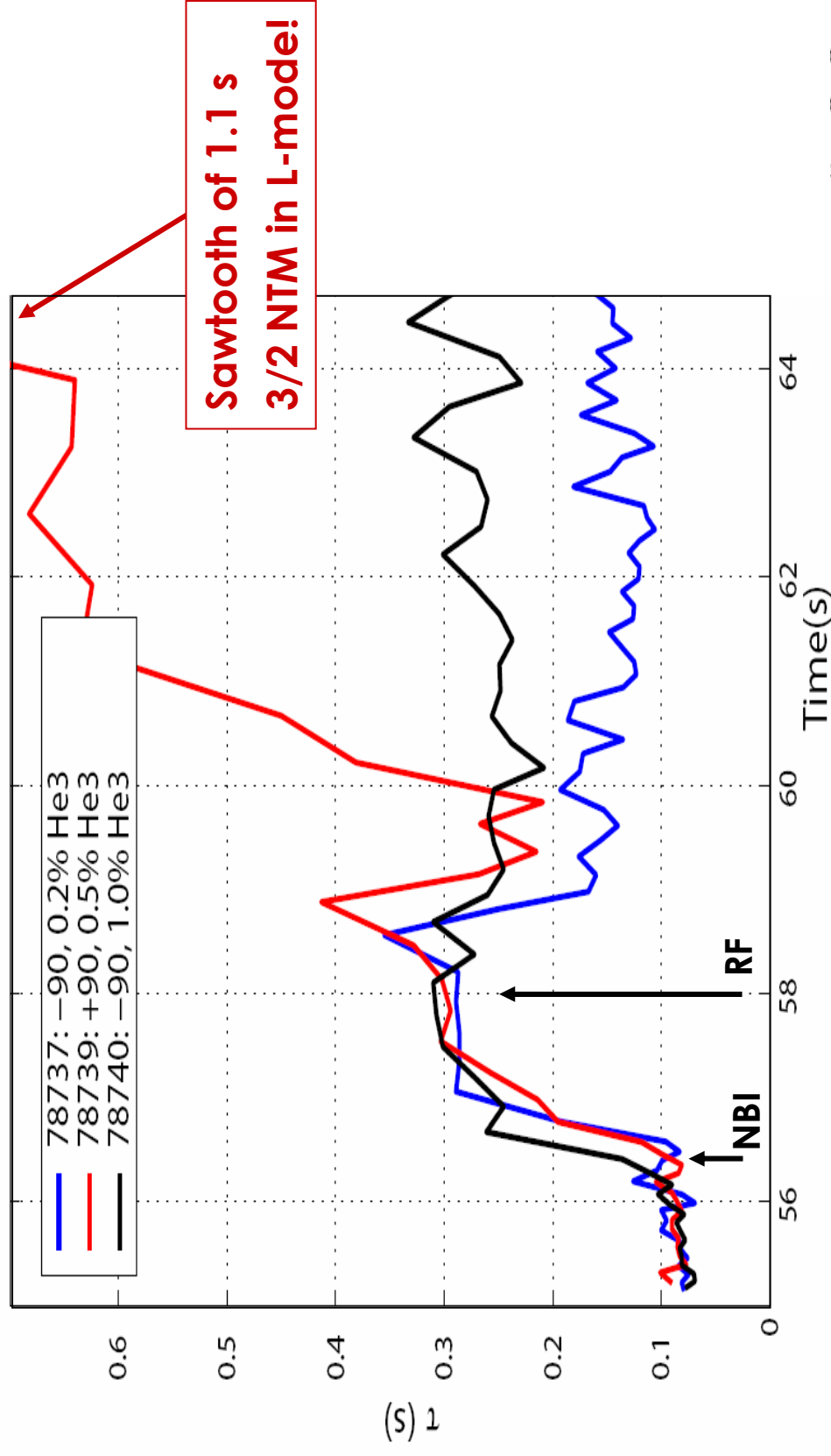
- Stabilised by NBI (as ITER-like ICRH not available)
- Decreased τ_{saw} by factor of 2, even in H-mode plasmas
- Direct evidence of importance of control - get NTMs with long s.t. period



Sawtooth Control with ICRH in JET (and ITER?) EFDA

- Lower ^3He concentration $\rightarrow$ shorter τ_{saw} (high energy ions in distribution tail)
- Co-propagating waves are stabilising, counter-propagating are destabilising

Sawtooth Period (78737, 78739, 78740): $B / I = 2.9\text{T} / 2.0\text{A}$

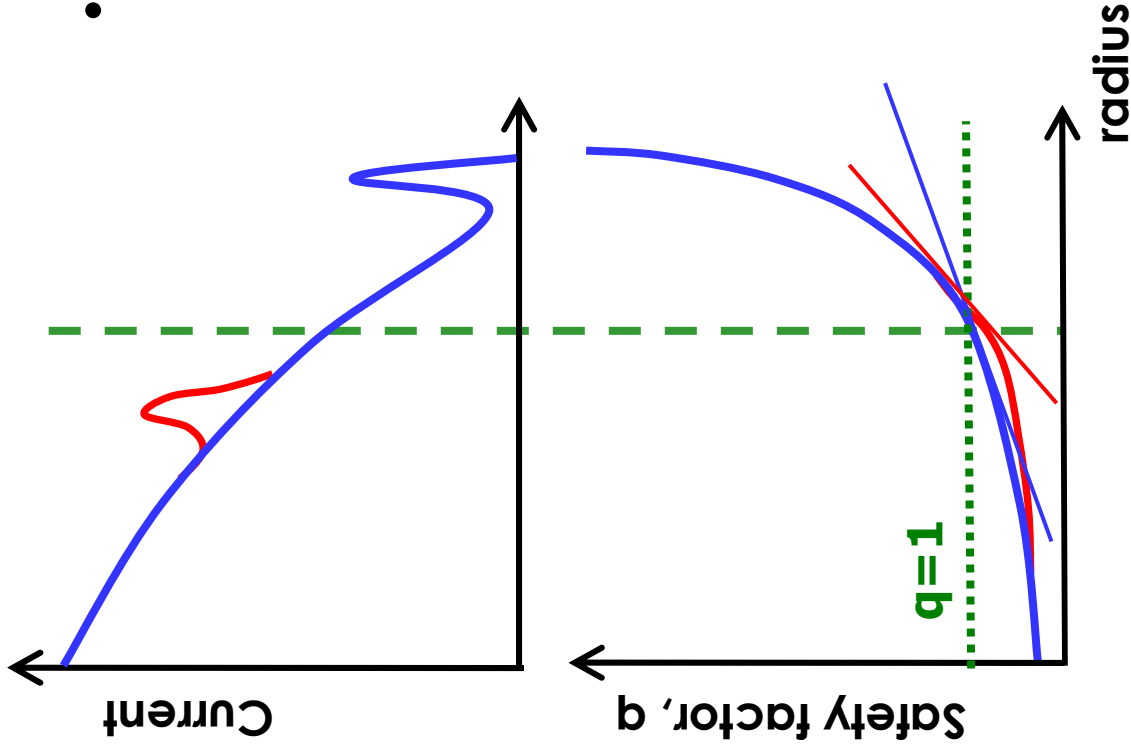


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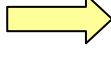
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How does driving current trigger sawteeth?

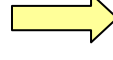
- Trigger condition: $\pi \frac{\delta \hat{W}}{s_1} < c_\rho \frac{\rho}{r_1}$



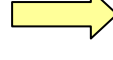
A perturbation is applied to the initial current profile (inside $q=1$)



More current means more poloidal field, so q drops



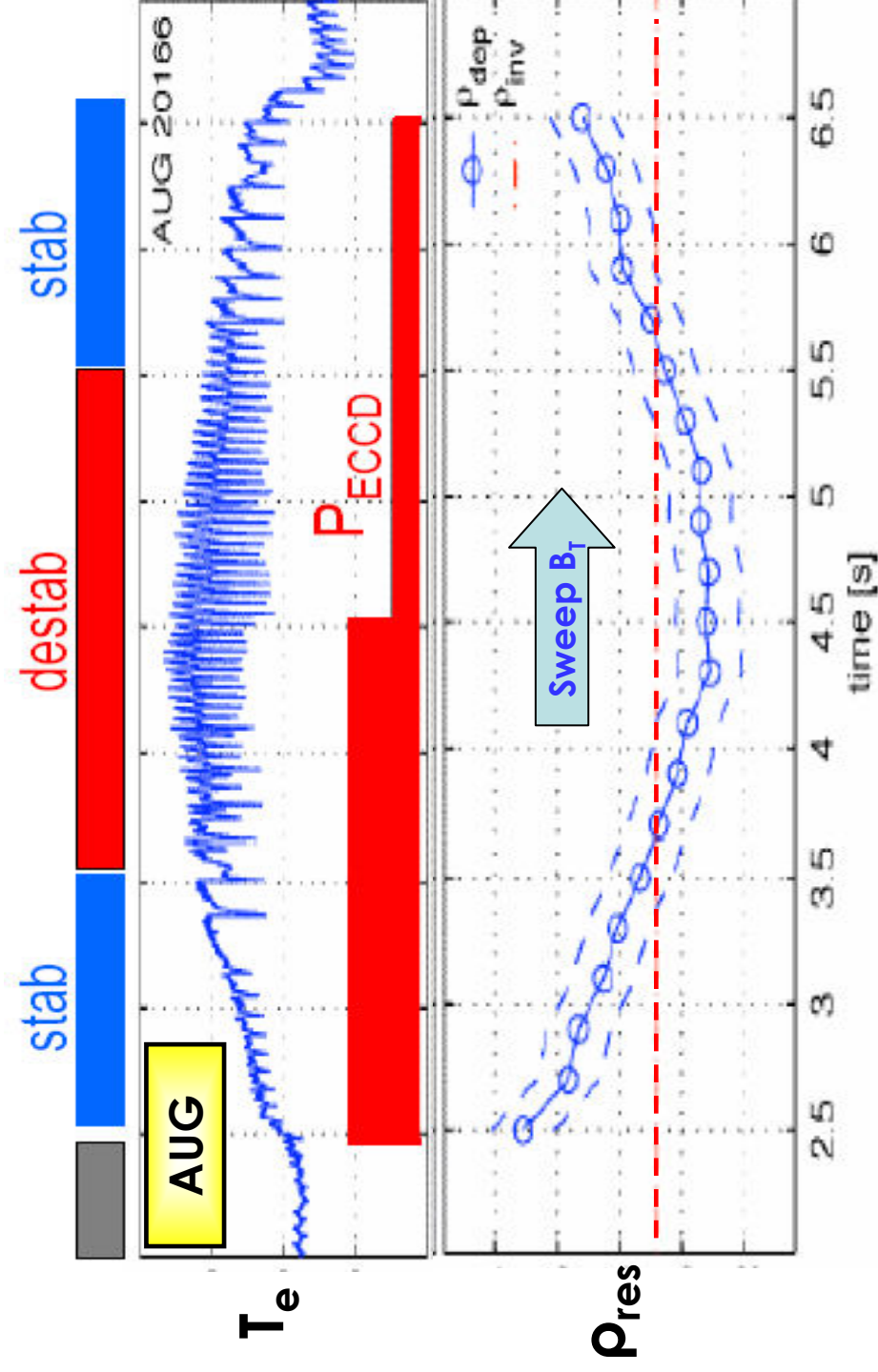
$q=1$ is moved outwards



Magnetic shear at $q=1$, s_1 (~gradient of q) increases

Current drive can shorten sawtooth periods

- Current drive shown to destabilise sawteeth in ASDEX Upgrade, DIII-D, TEXTOR, JT-60U, TORE SUPRA, TCV, HL2A....



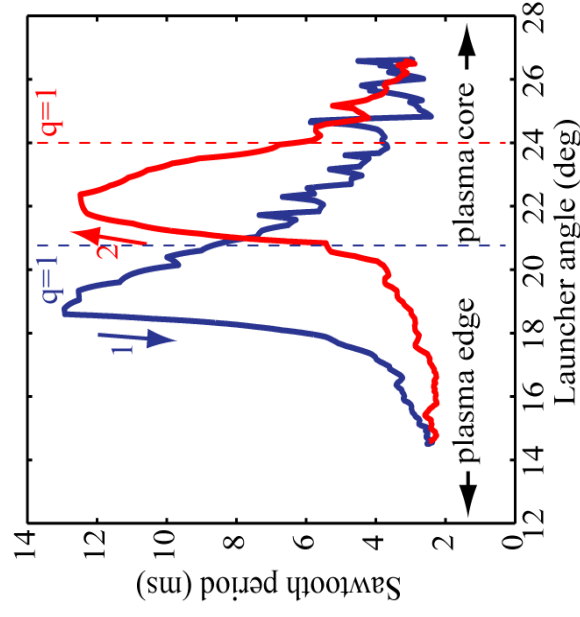
Mück et al, Plasma Phys Cont Fus, **47**, 2005

Manini et al, 14th Joint Workshop on ECE and ECRH, Santorini, 2006

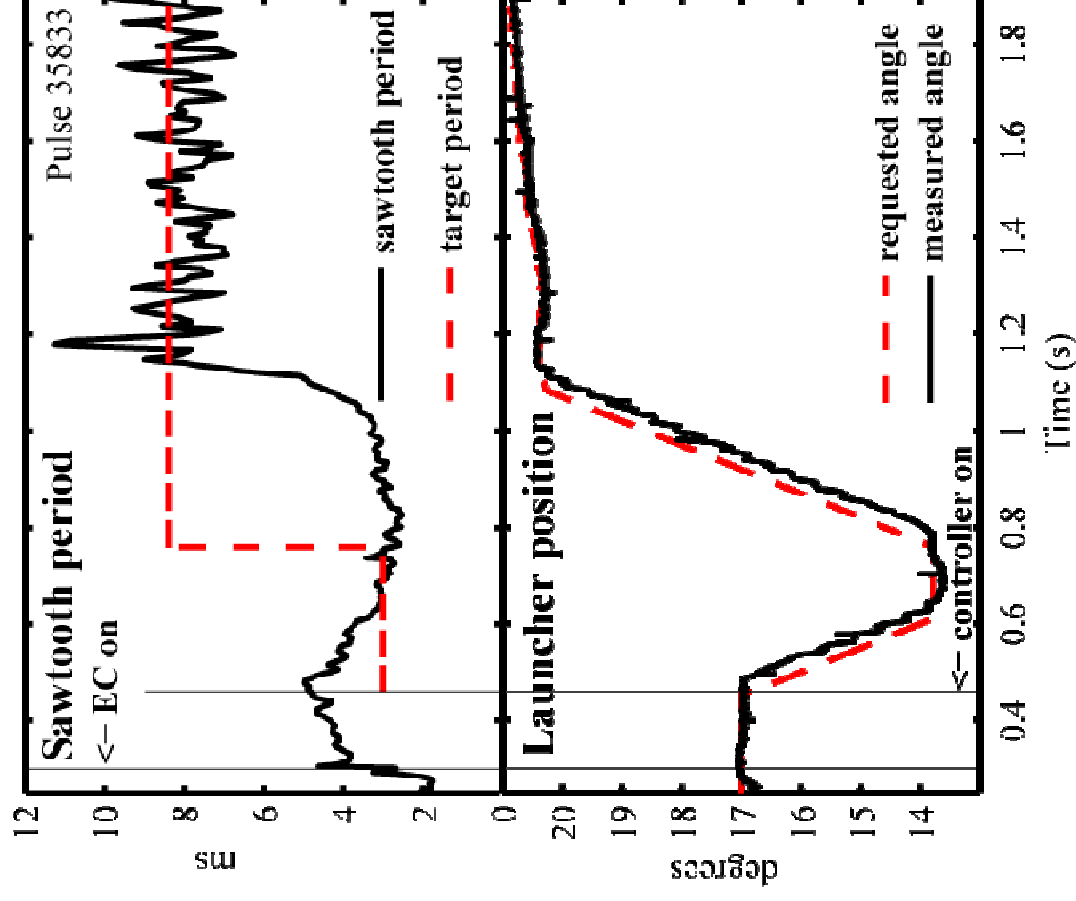
ECCD Real-time control in TCV



- Controller obtains and tracks target reference period by tailoring EC deposition to be just outside $q=1$
 - Launcher moved to larger angle to increase period, smaller angle to decrease
- Maximum period acquired and tracked despite changing plasma conditions



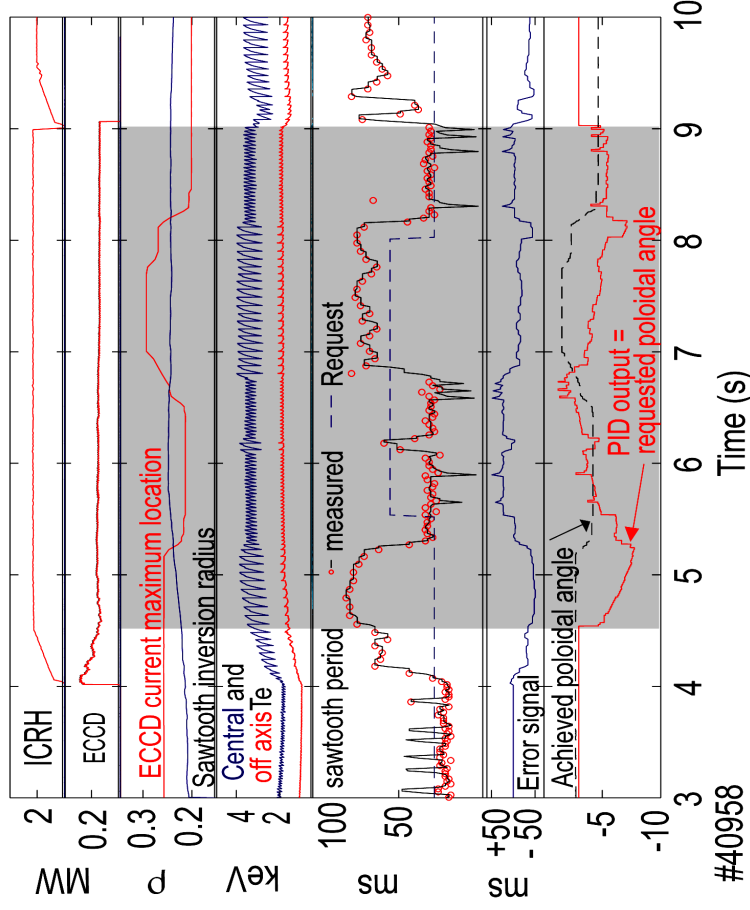
TCV



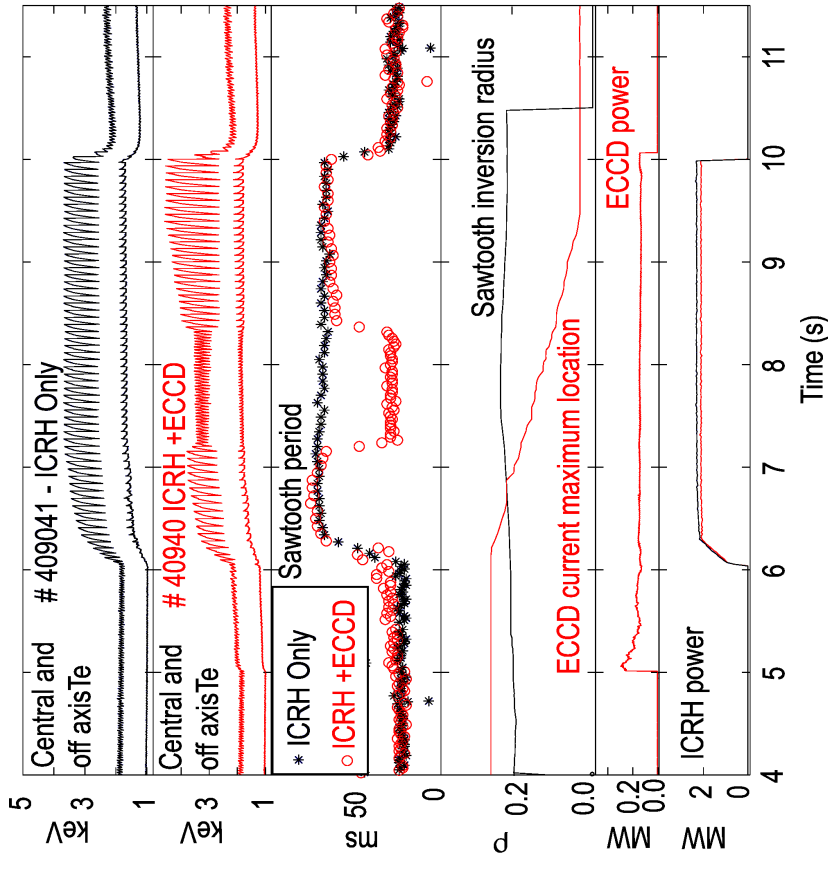
- **Open loop – ICRH + scan ECCD**

- 2MW ICRH: $\tau_{\text{saw}}=70\text{ms}$ ($\tau_{\text{Ohm}}=30\text{ms}$)
- Add 300kW ECCD: $\tau_{\text{saw}}=30\text{ms}$
- Abrupt change in period

- Tentative explanation due to S_{crit} trigger dependence upon fast ions



[M Lennholm et al, PRL, 102 (2009)]



- **Progress with RT control**

- Can maintain distance between sawtooth inversion radius and ECCD location using real time inversion radius measurement

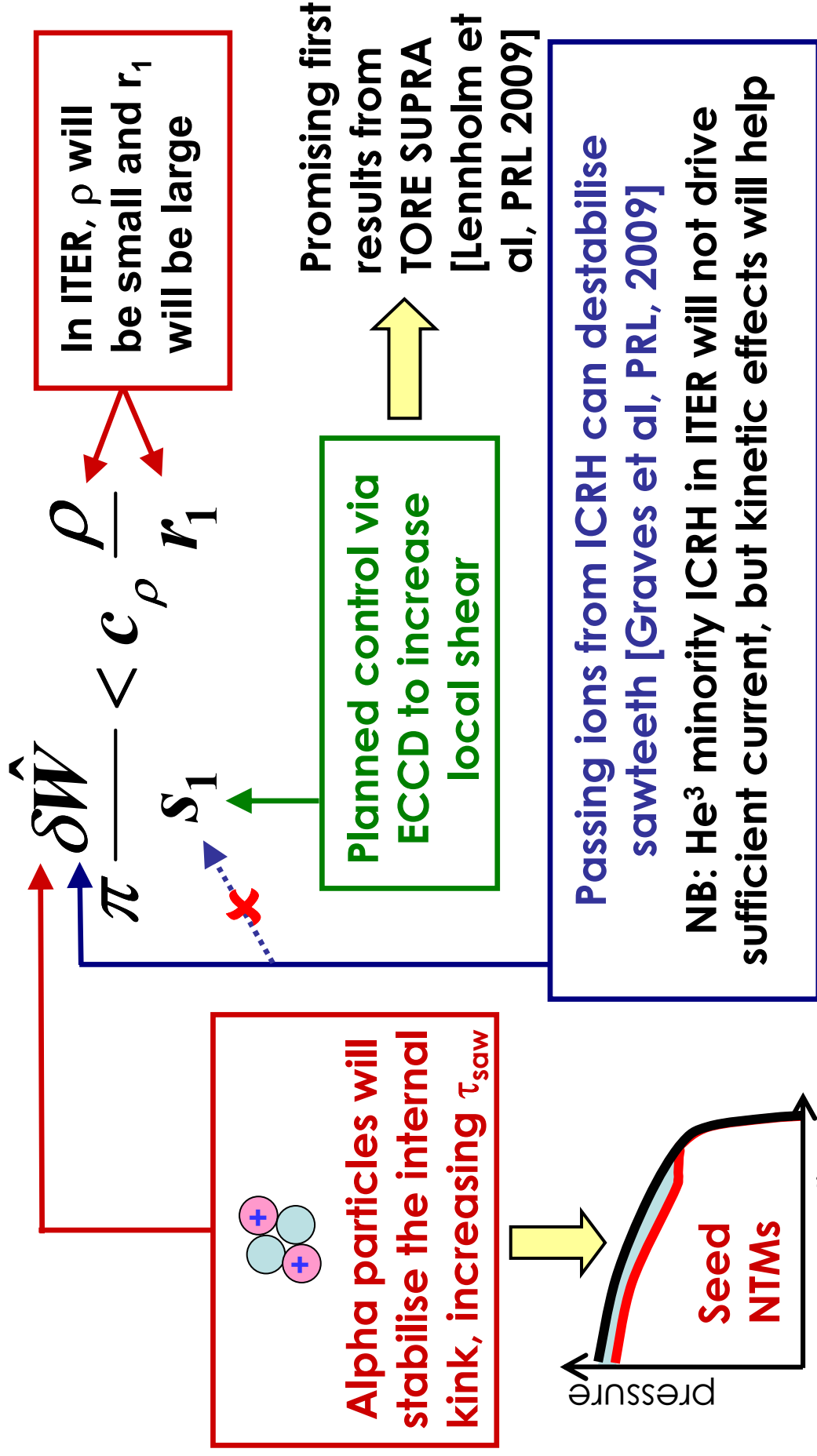
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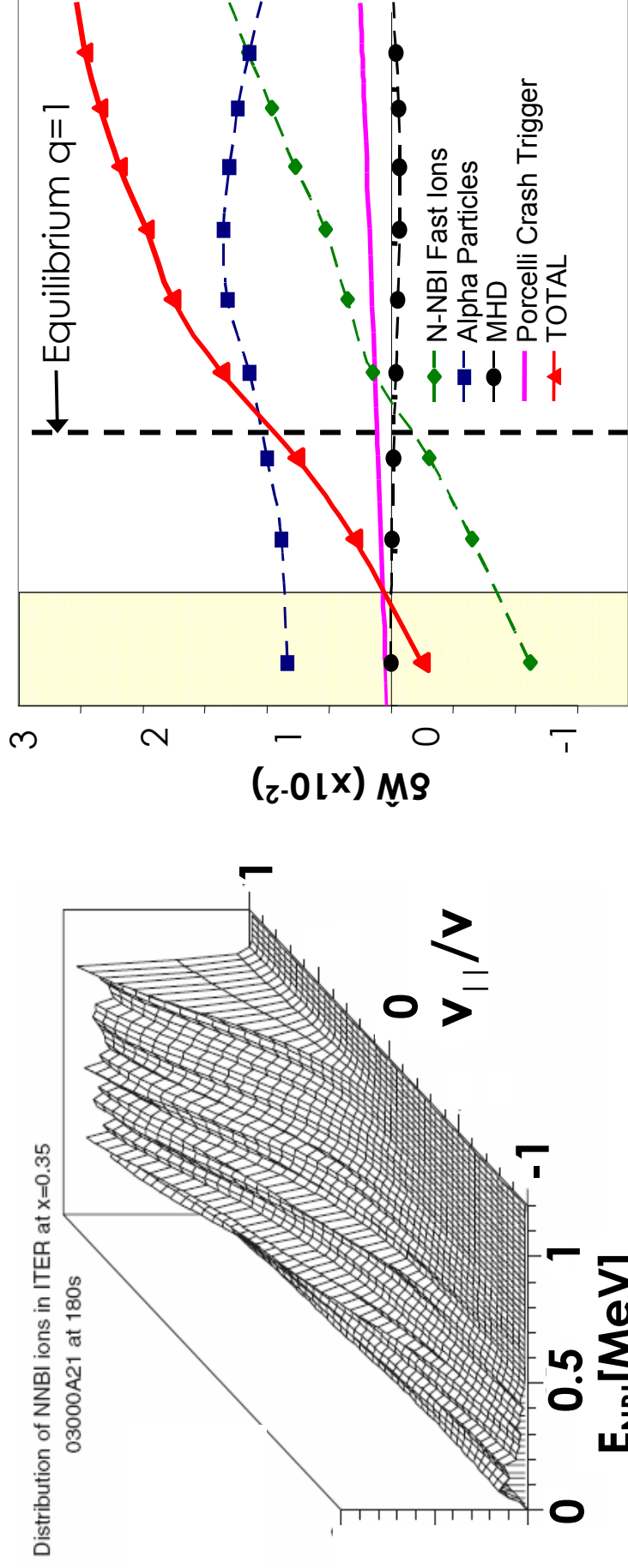
General Comments on Sawtooth Control in ITER

- Triggering criteria for resistive $n=1$ kink [Porcelli, PPCF, 1996]



ITER Sawtooth Control with NBI

- Sawtooth control even more important in ITER where the α particle population is likely to lead to long period sawteeth
 - Could off-axis NNBI co-passing ions be used?
 - Passing NNBI ions significantly influence sawtooth stability
 - Only destabilising if $q=1$ is very core localised ($r_1/a < 0.2$)
 - With broad $q=1$ expected in Scenario 2, NNBI ions strongly stabilising!



$E_{\text{NBI}} [\text{MeV}]$

Budny, NF, **42**, 2002

Chapman, PPCF, **50**, 2008

ITPA MHD Working Group

- **MHD Group has initiated high priority near-term ITER tasks**
 - WG3: Assessment of the power requirements for ECRH and ICRH for control of sawteeth (Chair: Ian Chapman)
- **Sawtooth control strongly influenced by fast ions**
 - Need accurate fast ion distribution function arising from ICRH (i) in the core for heating and (ii) near $q = 1$ for mode control
 - Early assessments made using SELFO code (T Johnson)
 - Need accurate fast ion distribution function arising from N-NBI in core
 - Early assessments made using TRANSP code (R Budny)
- **Sawtooth control achieved by changing magnetic shear at $q=1$**
 - Need assessment of local current drive at $q = 1$ achievable with ECCD
 - Some work using GRAY code (C Zucca, O Sauter)

The future for sawtooth control research

- **ECCD Control in presence of fast ions**
 - Need robust experimental verification that ECCD can destabilise sawteeth in the presence of fast ions (eg ICRH to represent α particles)
 - Initial assessment made on TORE SUPRA
 - Though still some unexplained behaviour
 - Also to be addressed on ASDEX Upgrade, DIII-D, KSTAR...
- **Will require real-time feedback in ITER (if ECCD control works)**
 - Some positive signs that real-time feedback can be achieved
 - Need to show robust *minimisation* of sawtooth period
 - Work continuing on TCV, AUG, TORE SUPRA, FTU...

Conclusions

- Sawtooth Behaviour in different machines has been explained by a model **including flow and kinetic effects**
 - Local effects of passing fast ions found to be very important
 - Flow shear can affect kink mode stability as well as trapped ion response

ON-AXIS NBI HEATING	FLUID EFFECTS	KINETIC EFFECTS
MAST	✓	
JET		✓
TEXTOR	✓	✓

SAWTOOTH CONTROL	INCREASE S_1	REDUCE δW_{hot}
ECCD	✓	
ICRH		✓
OFF-AXIS NBI	?	✓