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# Effect of 3d Fields near the Tearing Beta Limit

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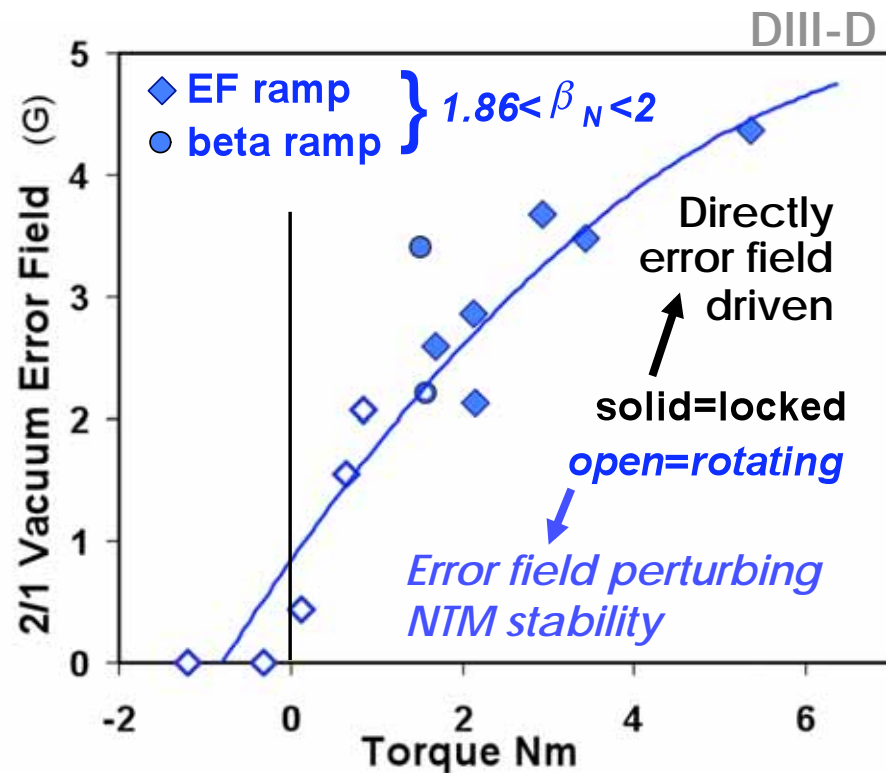
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*Work funded by the US DOE.*



# How do Error Fields Interact with Plasma?

*DIII-D experiments show resonant error field can act through two mechanisms to drive modes in high  $\beta$  plasmas:*



- Locked modes:
  - Influenced by proximity to
    - ideal kink beta limit?
    - classical tearing limit?
  - Role of rotation?
- Rotating modes:
  - EF perturbing classical or neoclassical stability?
    - Action through rotation or rotation shear?

→ EFs can probe NTM physics  
→ Measure error field response & correction requirements...

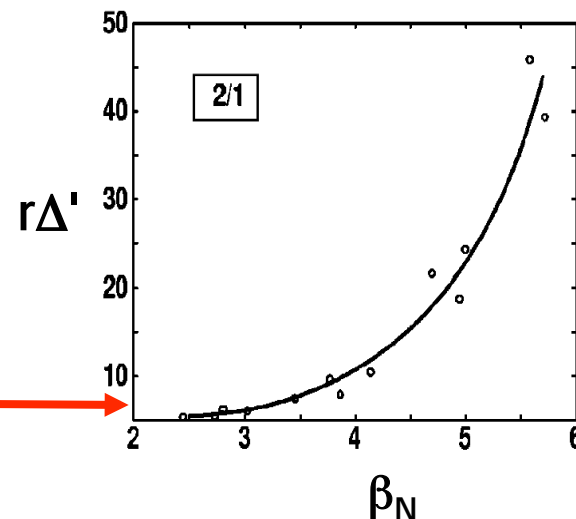
# 2/1 Tearing $\beta$ Limits May Be Governed by Pole in $\Delta'$

– *Introducing dependency on current and flow profiles*

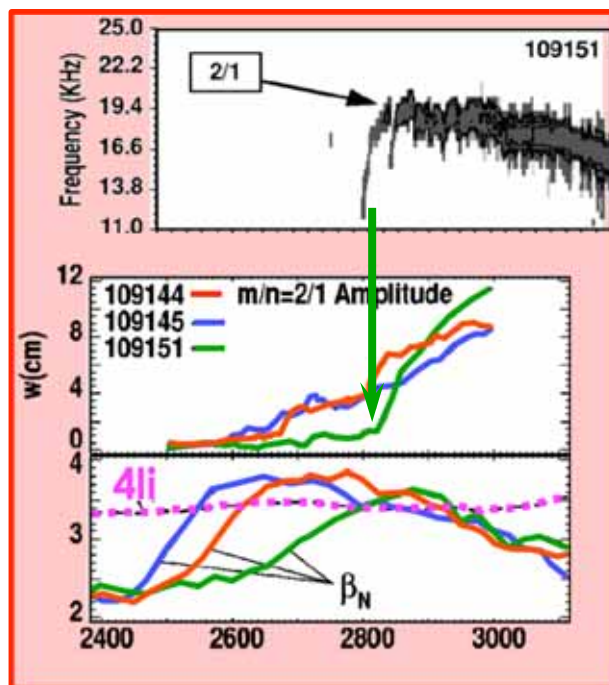
- Calculations show  $\Delta'$  rises as ideal  $\beta$  limit approached

Seedless 2/1 modes observed as  $\beta_N$  crosses ideal no-wall limit

- *Current profile governs baseline  $\Delta'$  & gives means to raise thresholds*



[Brennan et al, PP10, 1643]

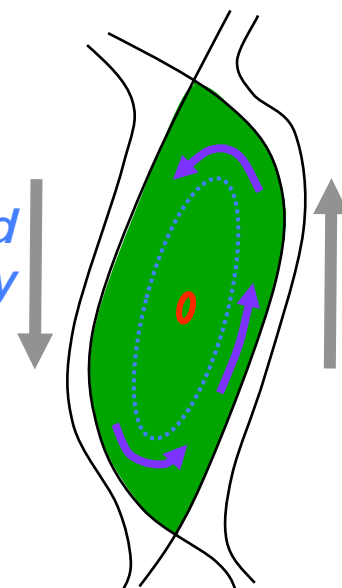


- Island stability may also be modified by flow shear:

– *Viscous coupling distorts island structure changing free energy*

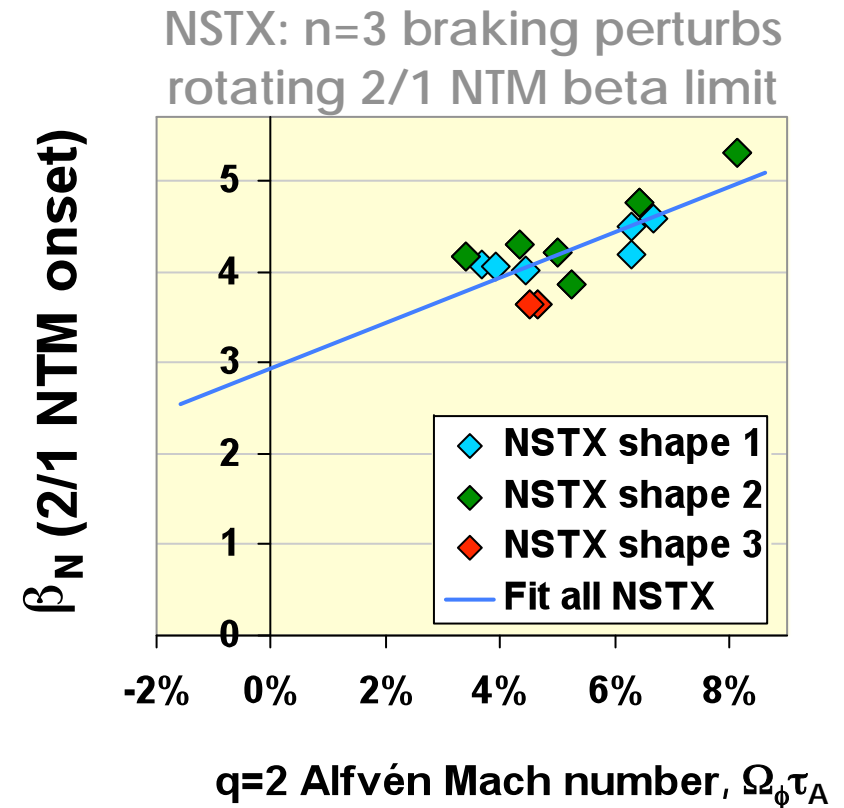
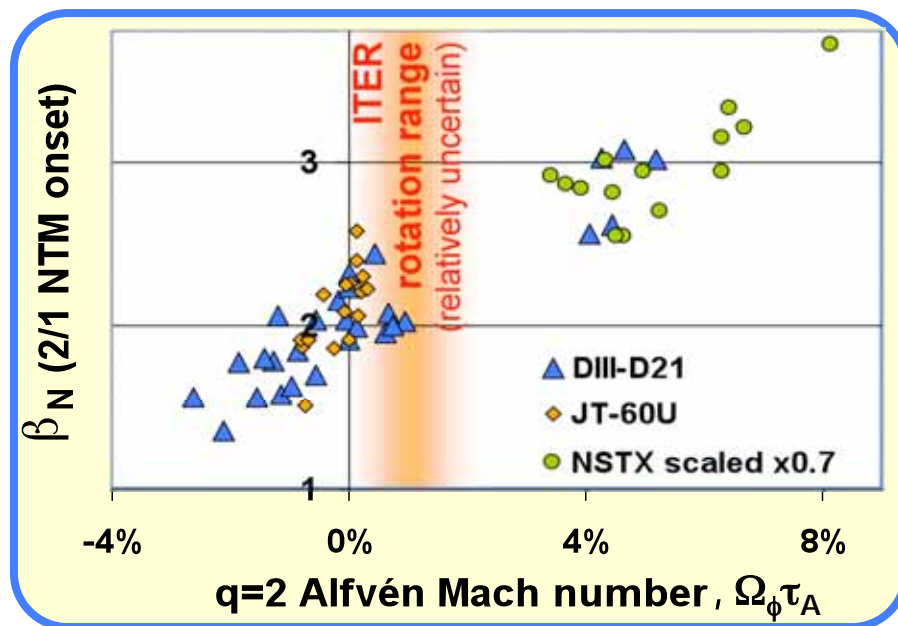
- Error fields can perturb flows in the plasma

– *Response to error fields may depend on plasma stability  $\leftarrow \beta_N, \Delta'$*



# NSTX Studies Have Shown a Rotation Effect in Error Field Interaction & Impact on NTM $\beta$ limit

- n=3 braking showed 2/1 NTM thresholds rise with rotation
- Consistent with rotation trends from beam mixing studies on DIII-D & JT-60U:



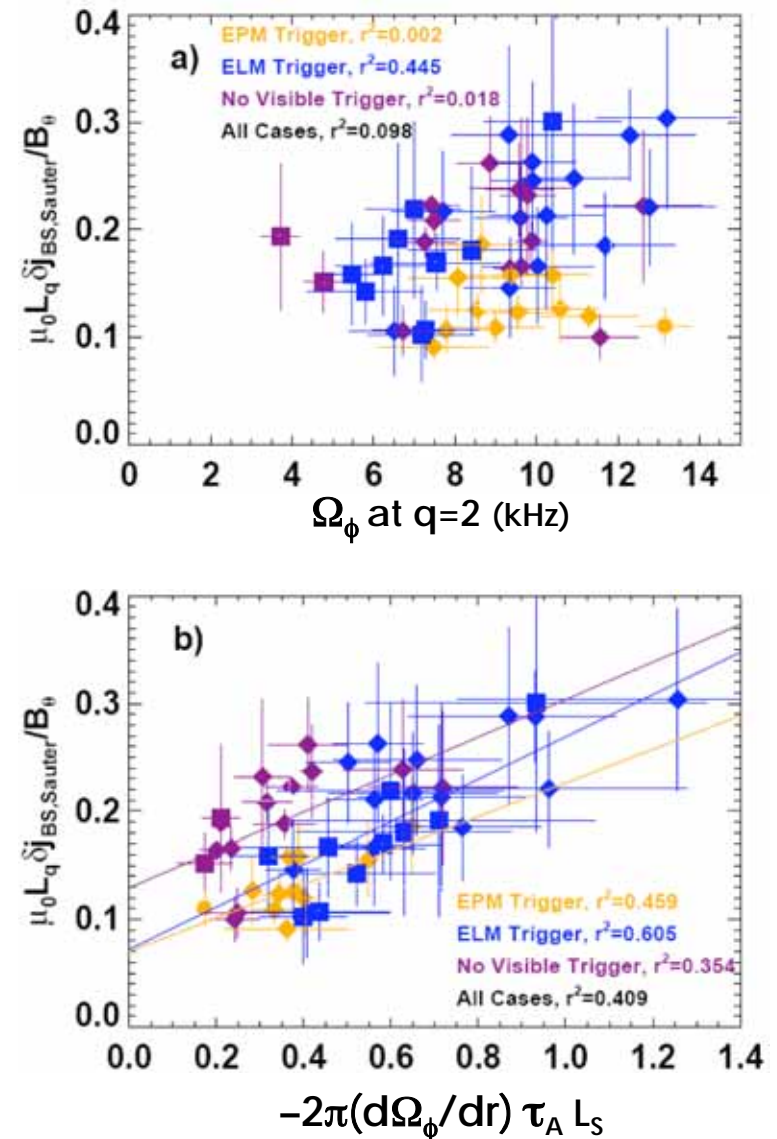
- *How is rotation acting on NTM stability?*
- *What are practical error field limits?*

# NSTX Database Study Suggested Rotation Acts Through the Local Rotation Shear at the Island

- Gerhardt analysis<sup>1</sup> compared trends for different types of NTM trigger across NSTX 2007 campaign
  - no n=1 braking in this data set

*Goal 2009: Controlled study of error field effect in constant conditions:*

- Decouple rotation roles further with n=1 and n=3 fields
- Learn about error field interaction
- *Achieved reproducible scans by tuning H mode:*
  - shape, gas, lithium

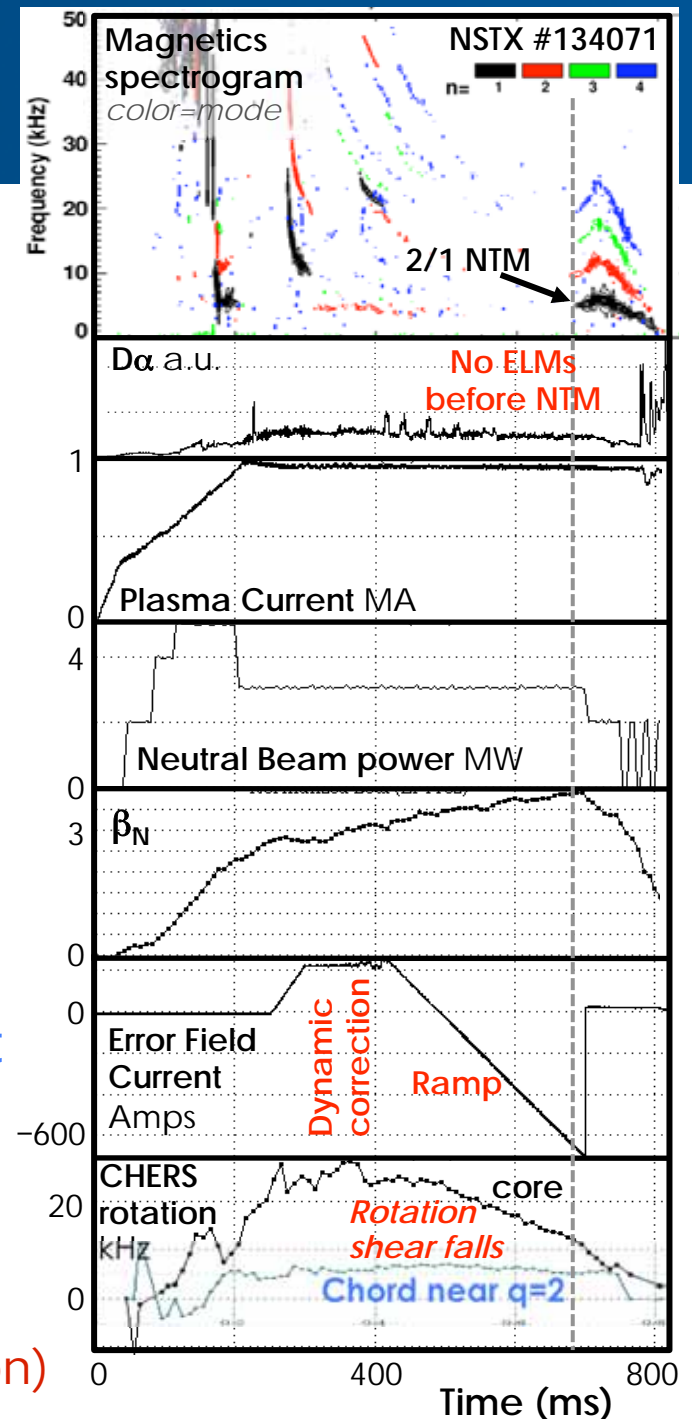


# New NSTX Experiment: Ramp Error Fields to Make Mode

- Vary ratio  $n=1:n=3$  fields shot to shot
- Typically ELMs are small (due to lithium)
- No clear NTM trigger in most shots
  - ‘Seedless’ – must be  $\Delta'$  triggered

## Other shot details:

- Early strong heating for H mode
- MHD at 300ms when  $q=2$  appears
- Reproducible conditions & front end to eliminate  $q$  profile changes shot-shot
  - From evaporating lithium each shot
- But note  $q$  relaxing towards  $q=1$  (when bad MHD would occur)
  - (Role of  $q_{\min}=1$  with EF under investigation)





# Applied Error Fields

## Mix of $n=1$ & $n=3$ from Midplane Coils

- $n=1$  field computed for various shots across the scan:

- Vacuum field is  $\sim 2.5\text{G/kA}$  ( $m=2$   $n=1$  at  $q=2$  surface)
- Including plasma response from other surfaces (IPEC) raises **total field** at  $q=2$

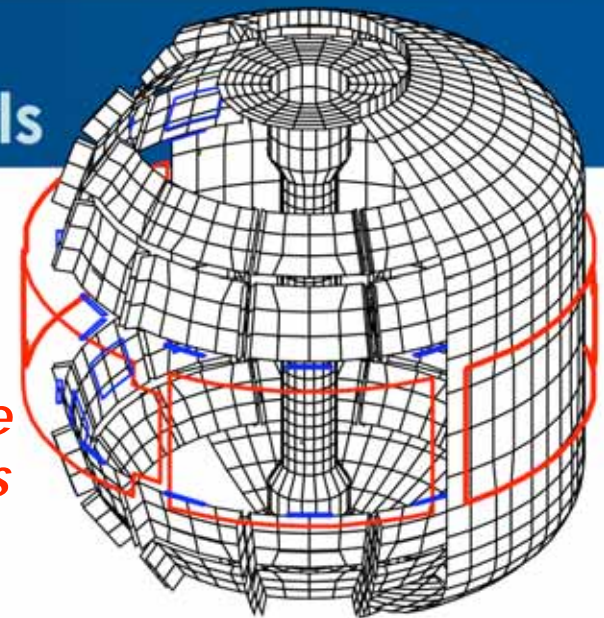
*Midplane field coils*



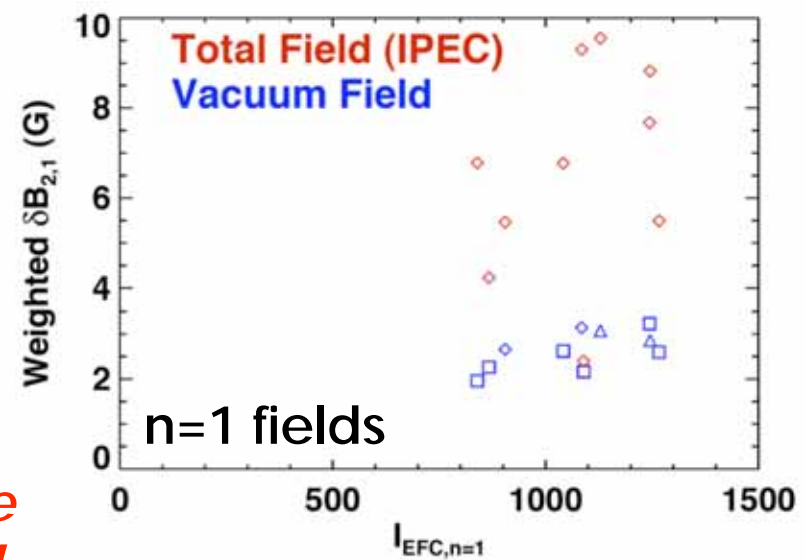
- $n=3$ : no similar formalism to compare size (as non-resonant)

- Typical surface averaged  $|B|$  is a few Gauss
- *But may be best to compare relative magnitudes in terms of coil currents!*

- *Gives better idea of relative field strengths*

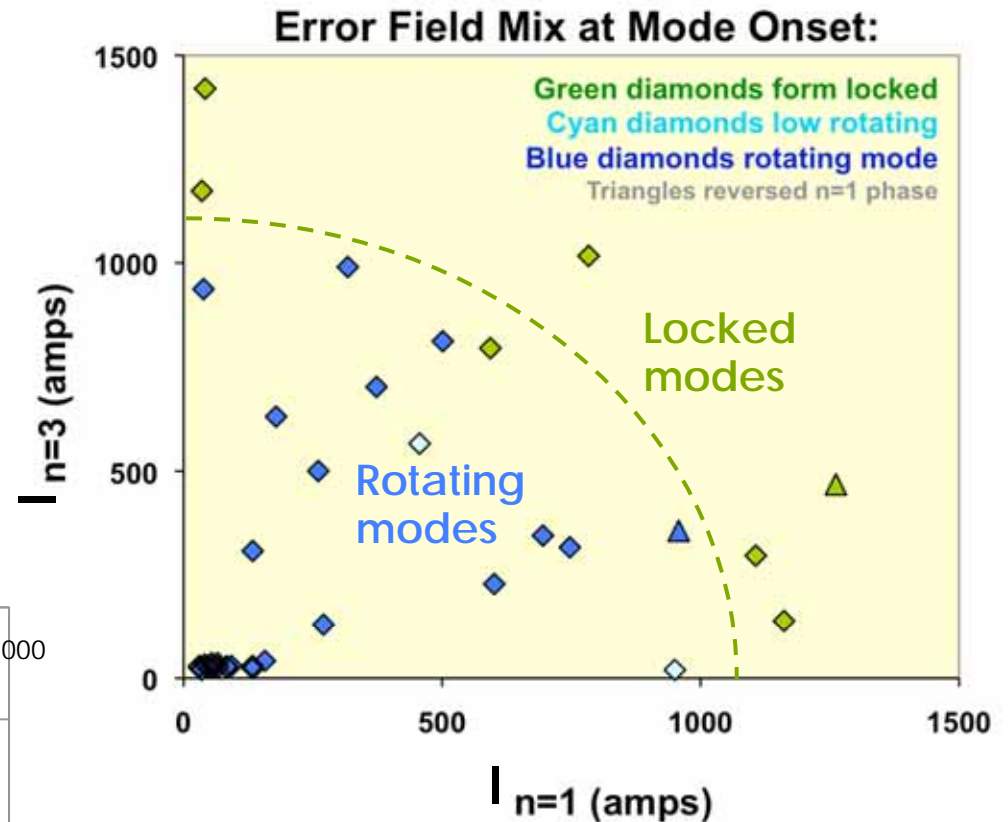
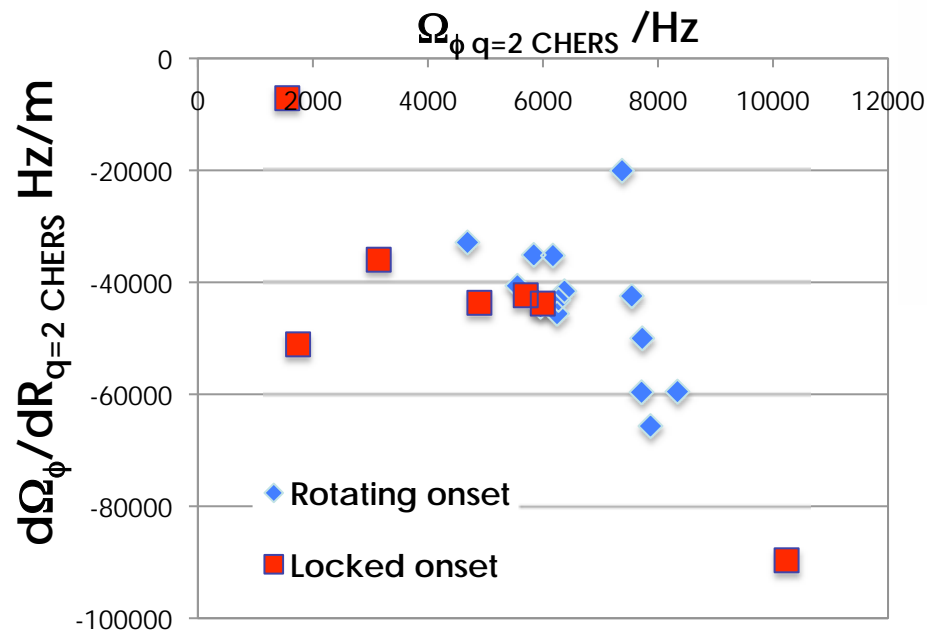


NSTX



# New Experiments Perturbed $\beta$ Limit with Wide Range of Resonant $n=1$ & Non-resonant $n=3$ Fields

- $n=1$  and  $n=3$  fields varied up to locked mode limits (◆)
  - Locked mode threshold with roughly equal levels of  $n=1$  and  $n=3$  field current
  - Wide variation in rotation profile achieved:

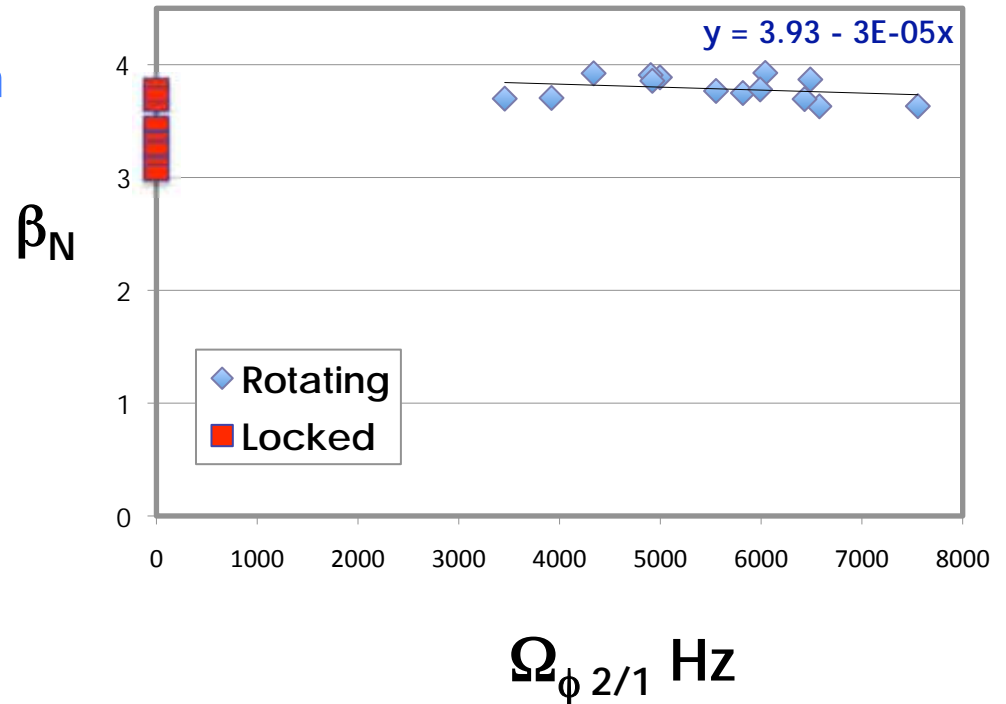
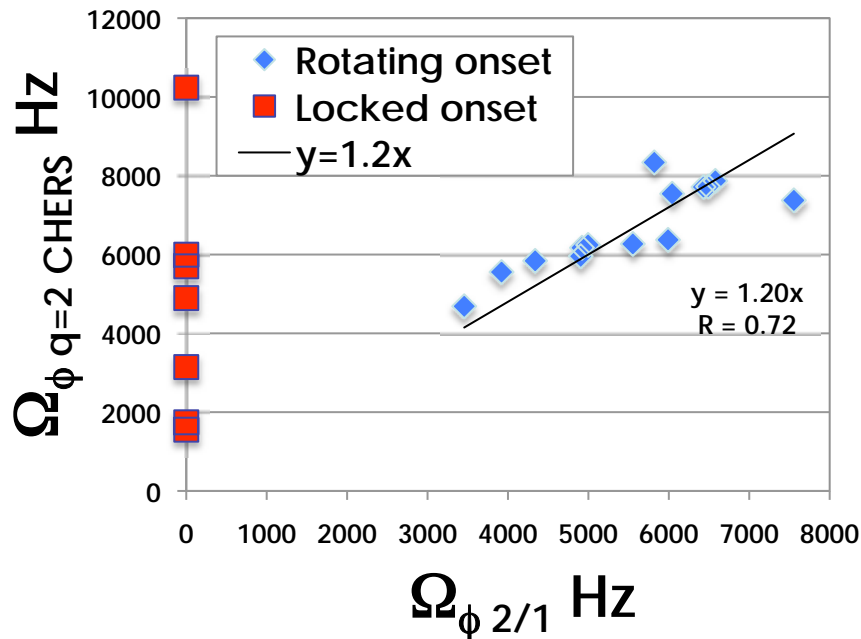


- Locked modes much slower on CER but not at zero rotation



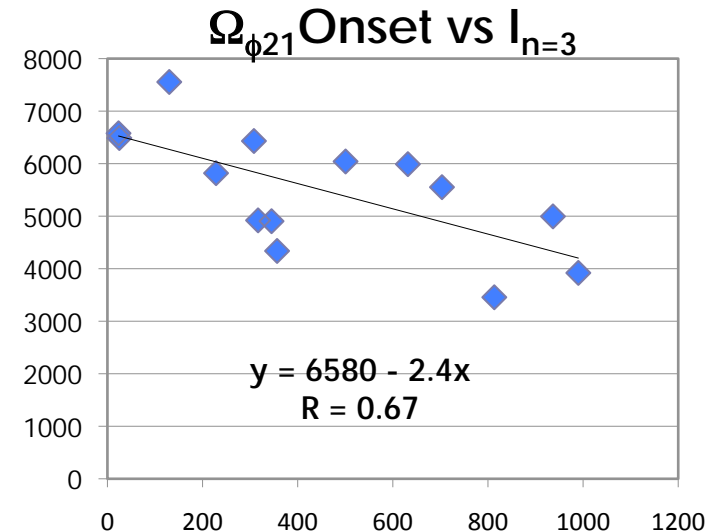
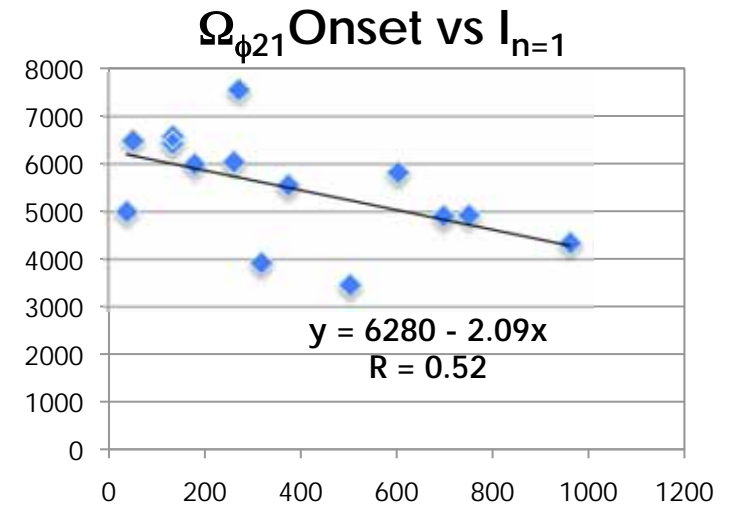
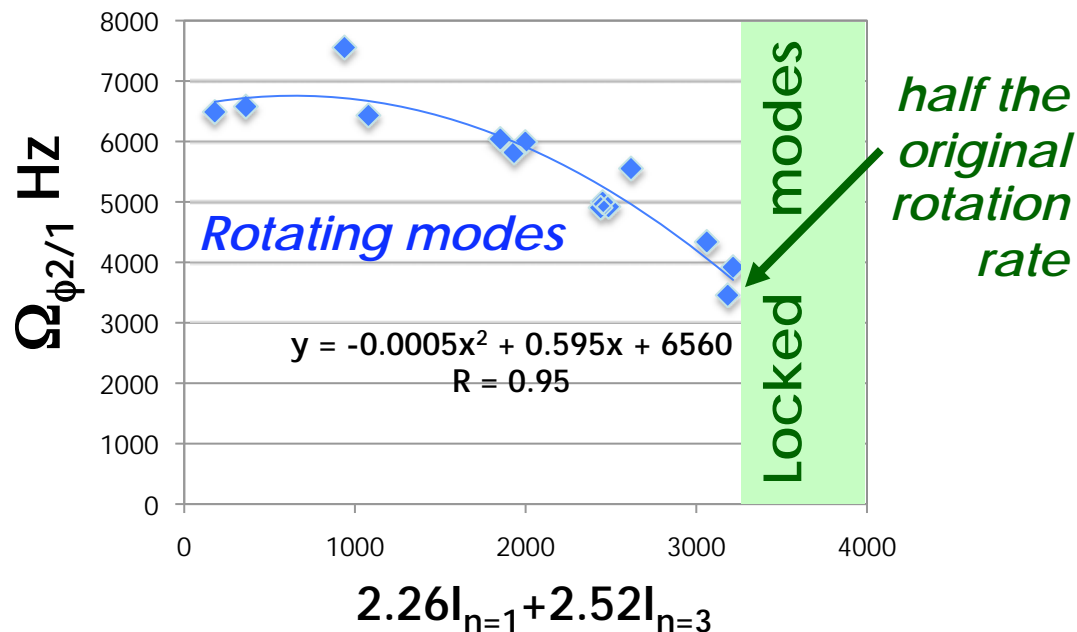
# Differences in CHERS q=2 and 2/1 mode rotation

- Mode forms locked while CHERS shows plasma rotating
  - Actual mode onset rotation is lower than CHERS
    - Coupling to ELMs?
  - Locked mode stops MHD fluid while plasma still flows



# Braking Effect: n=1 & n=3 Contribute Similarly to Braking

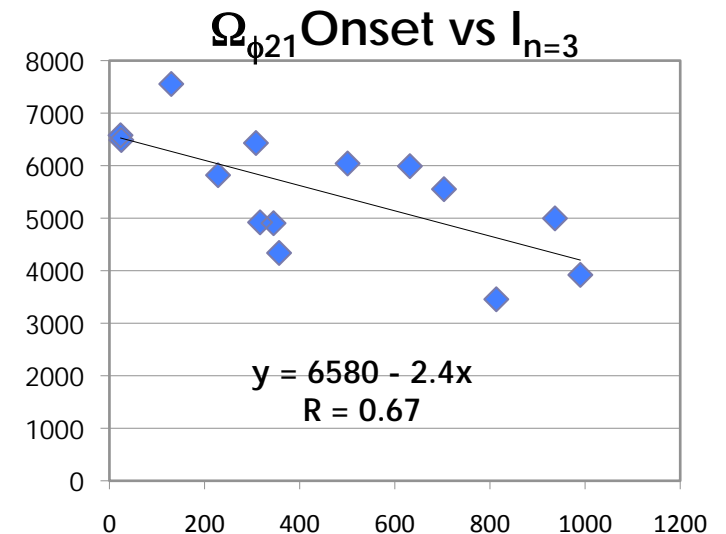
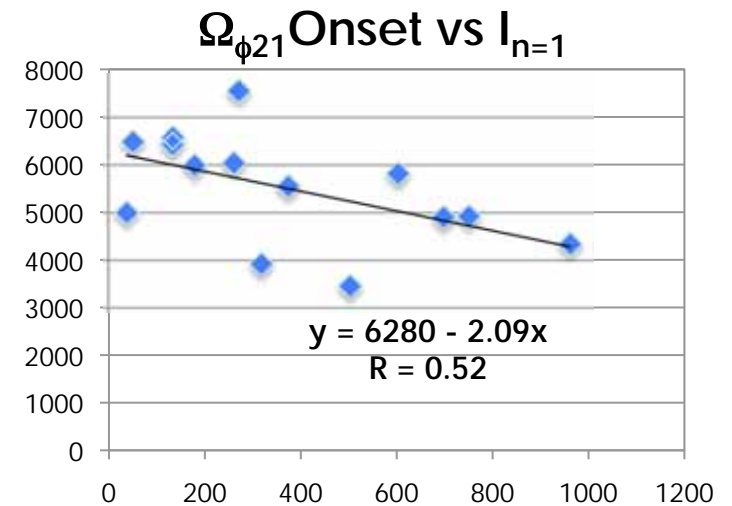
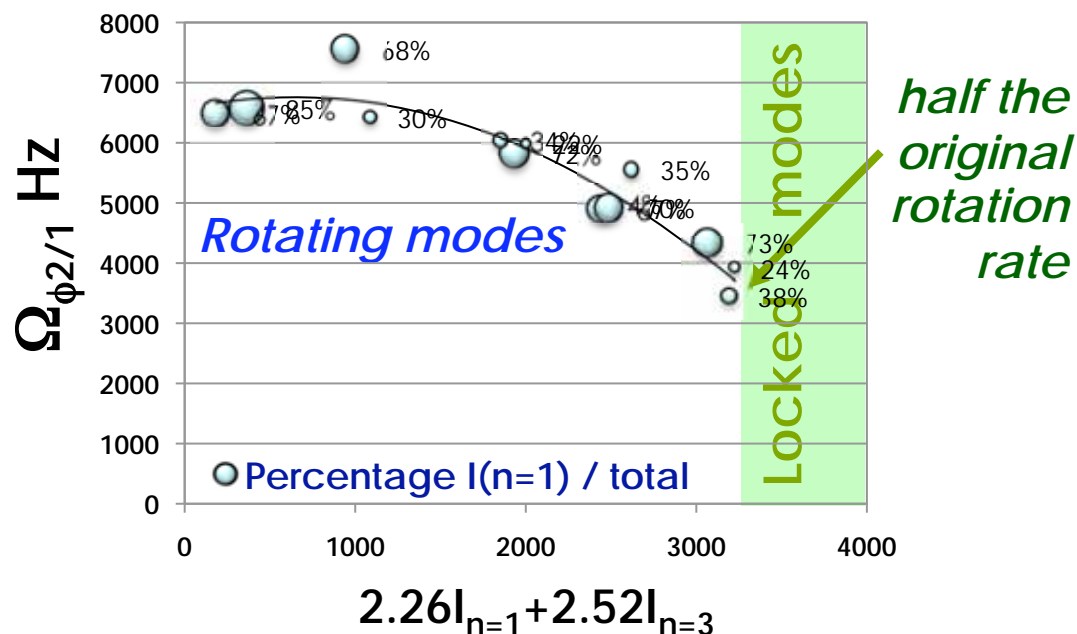
- Both n=1 and n=3 brake plasma
- Best fit is combination of similar levels of n=1 and n=3 currents:
  - $\Omega_{\phi 21} = 7500 - (2.26I_{n=1} + 2.52I_{n=3})$
  - *Good correlation for braking:*



✓ *Matches Fitzpatrick theory: Penetration at half natural rotation rate.*

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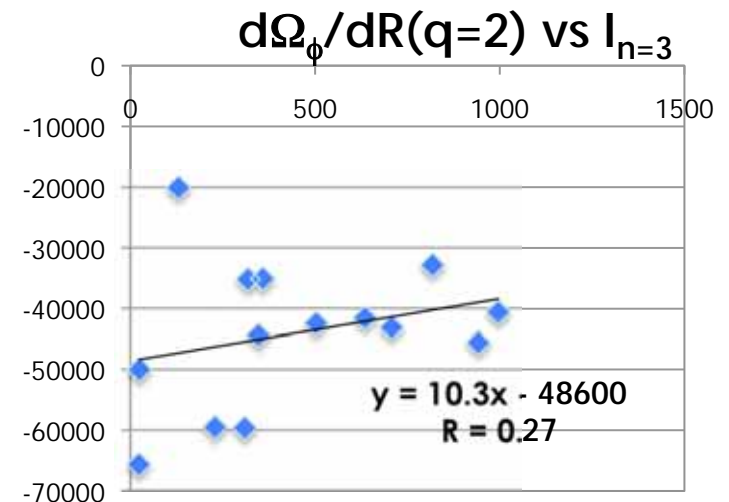
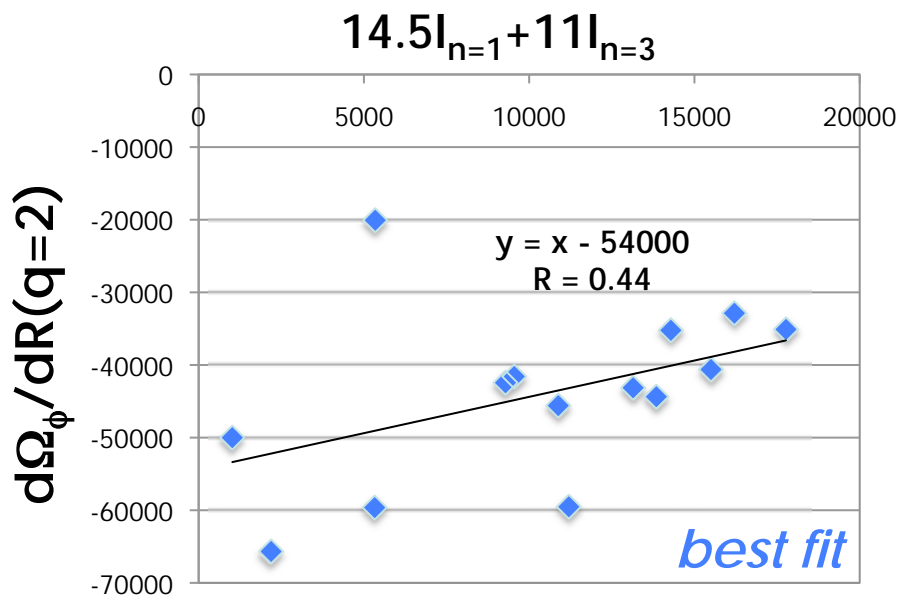
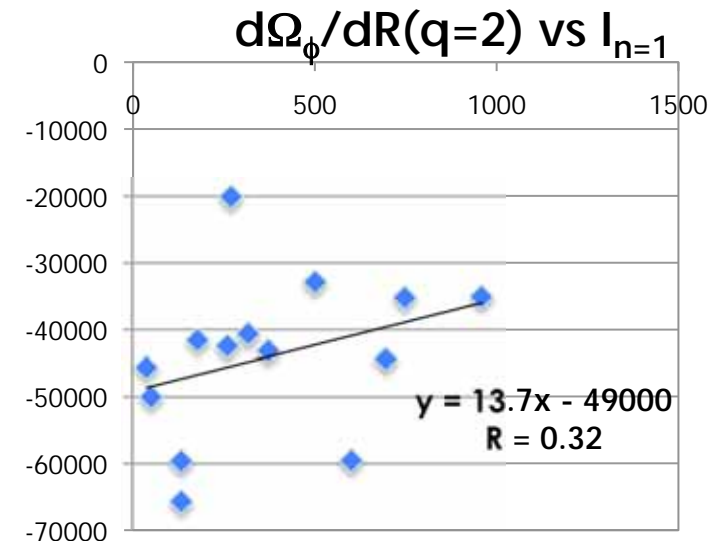


✓ *Fitzpatrick theory: Kind'a odd this works for n=3 – shouldn't?*

# Rotation Shear Much More Variable Over The Scan

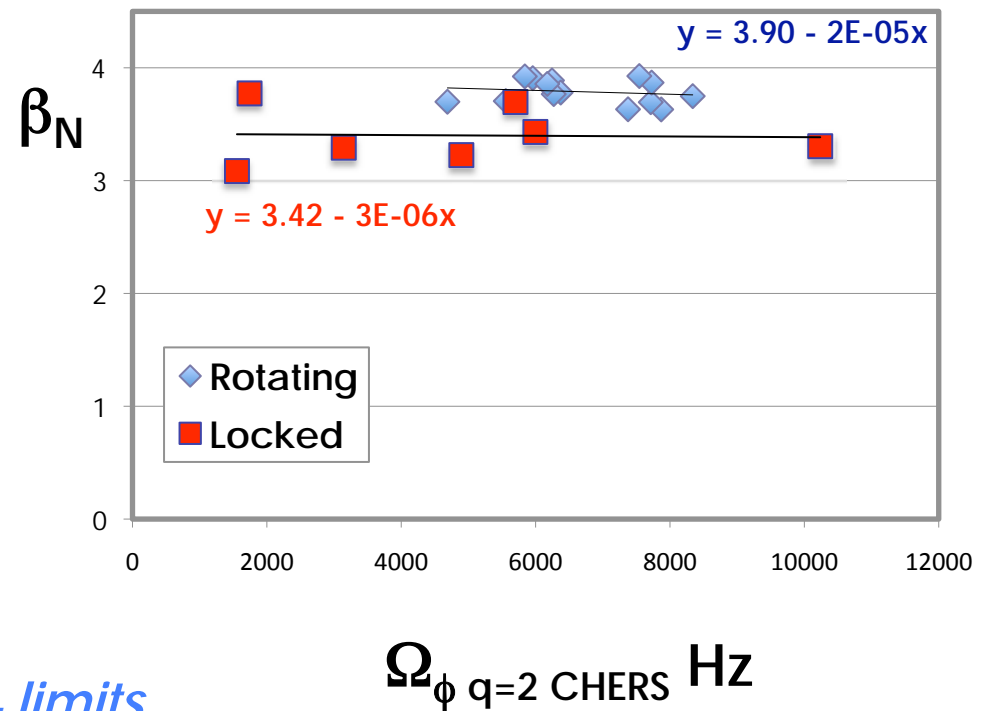
– *provides opportunity to decouple from rotation trend*

- Rotation shear more scattered than simple dependence on  $n=1$  &  $n=3$ 
  - Although both forms of braking reduce rotation shear – *best fit*:
    - $d\Omega_{\phi 21}/dR = -54000 - (14.5I_{n=1} + 11I_{n=3})$
  - Can decouple rotation shear from rotation effects – *which governs NTM?*



# Mode Forms at Lower $\beta_N$ when Locked

- Locked mode threshold is 0.5 lower in  $\beta_N$ 
  - May be partly confinement reduction
  - stripped out for rest of this analysis (J-KP analyzing locked mode physics<sup>1</sup>)

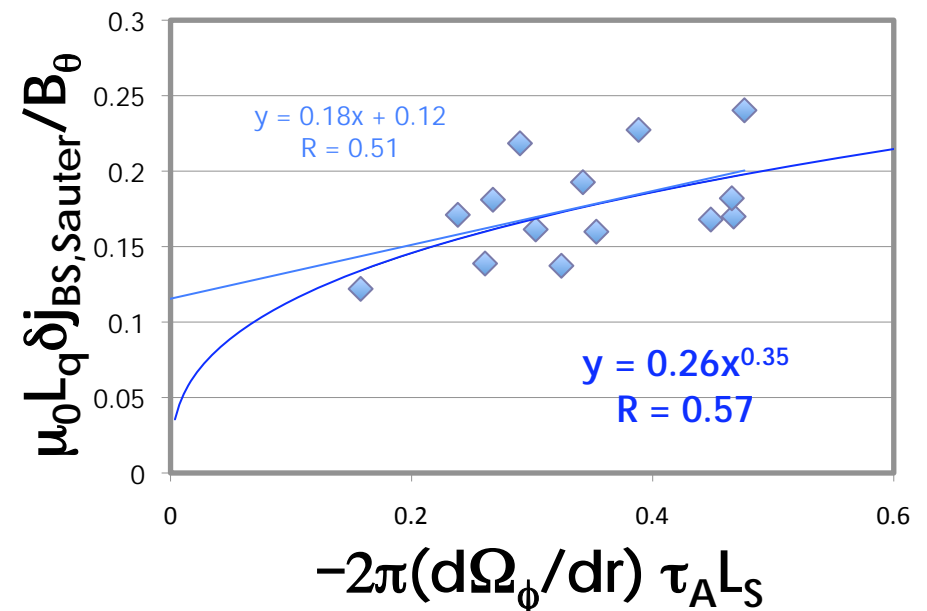
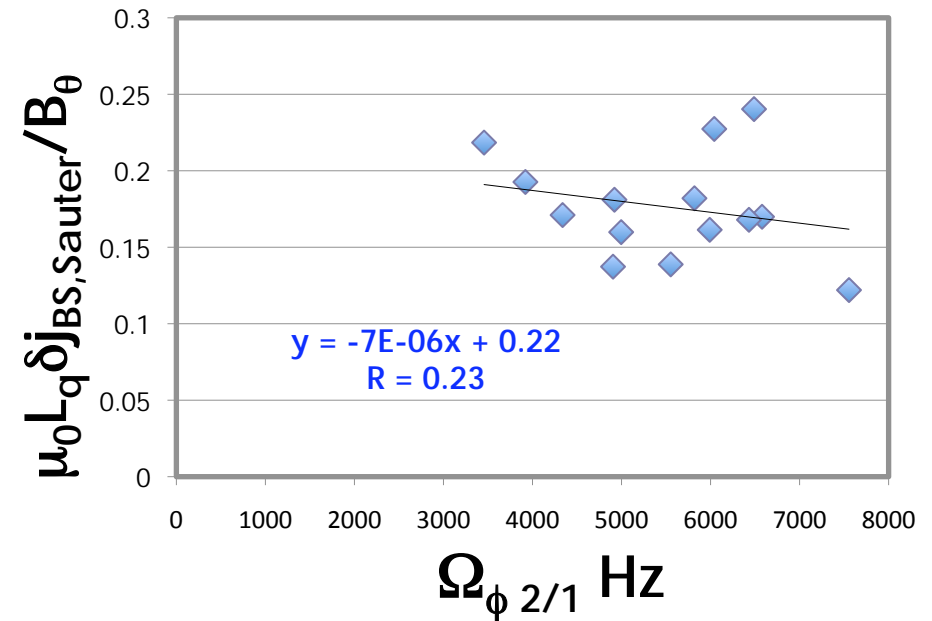


- Rotating mode shows no rotation dependence!
  - Generally below no-wall  $\beta_N$  limits
  - But need to look at drives in local parameters & understand what we really varied
    - How does braking impact rotation and mode drives?



# Bootstrap Drive Measure of NTM Threshold Suggests Dependence Through Rotation Shear

- No measurable trend with rotation!
  - Weak positive correlation with normalized rotation shear
    - Lowest thresholds at low rotation shear
    - Highest thresholds at high rotation shear
    - Best 'fit' is power law
- This correlation in the 'most noisy' parameters suggest physics is right:*
- *Rotation impact is through shear changing  $\Delta'$*
- No correlation if fit  $\beta_N$  instead
  - Fit vs rotation & rotation shear offers little improvement



# Conclusions on Rotation & Error Fields

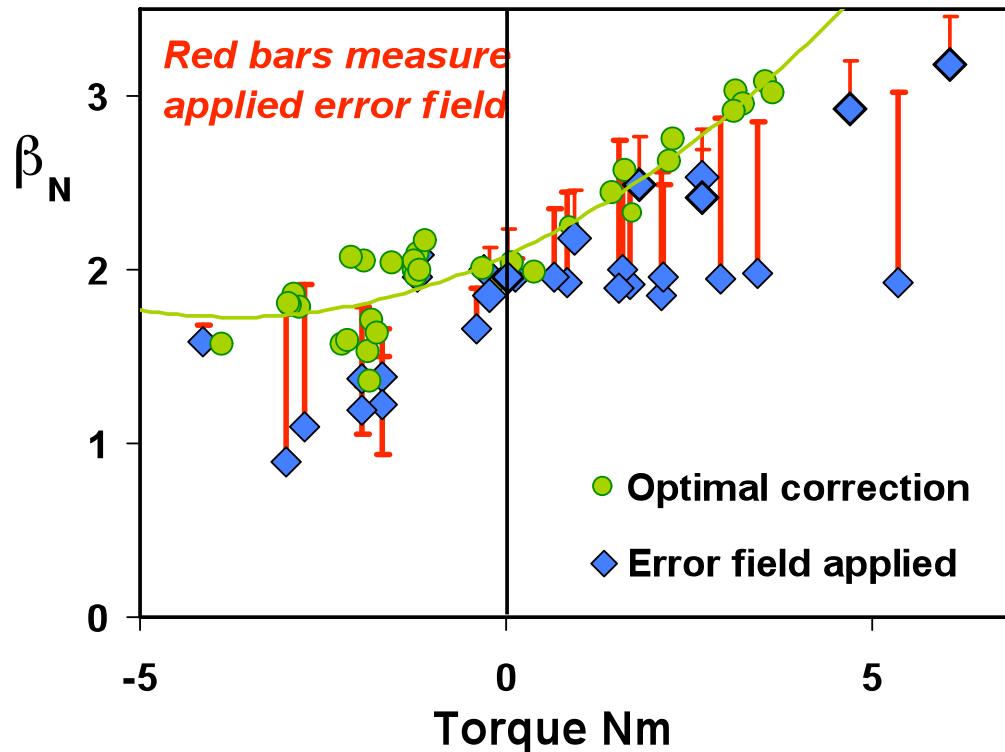
- NTM threshold dependence on rotation comes through **flow shear** impact at the rational surface
  - Confirms previous database study in controlled conditions
  - Correlations with rotation completely stripped out!
    - *Suggests changes to inherent plasma stability at the tearing resonant surface play an important role in determining mode onset*
- Threshold between rotating & locked mode regime at half natural plasma rotation – *for  $n=1$  &  $n=3$  fields!*
  - Locked modes above this (à la Fitzpatrick)
- Locked mode cases exhibit confinement degradation *before* mode onset, and have a lower  $\beta_N$  limit
- Both  $n=1$  resonant braking and  $n=3$  non-resonant braking have similar effects on plasma and mode

*Work in progress – some points to think about...*

**New DIII-D  
experiments to look  
at  $\Delta'$  role**

# Error field interact with tearing $\beta$ limit. How?

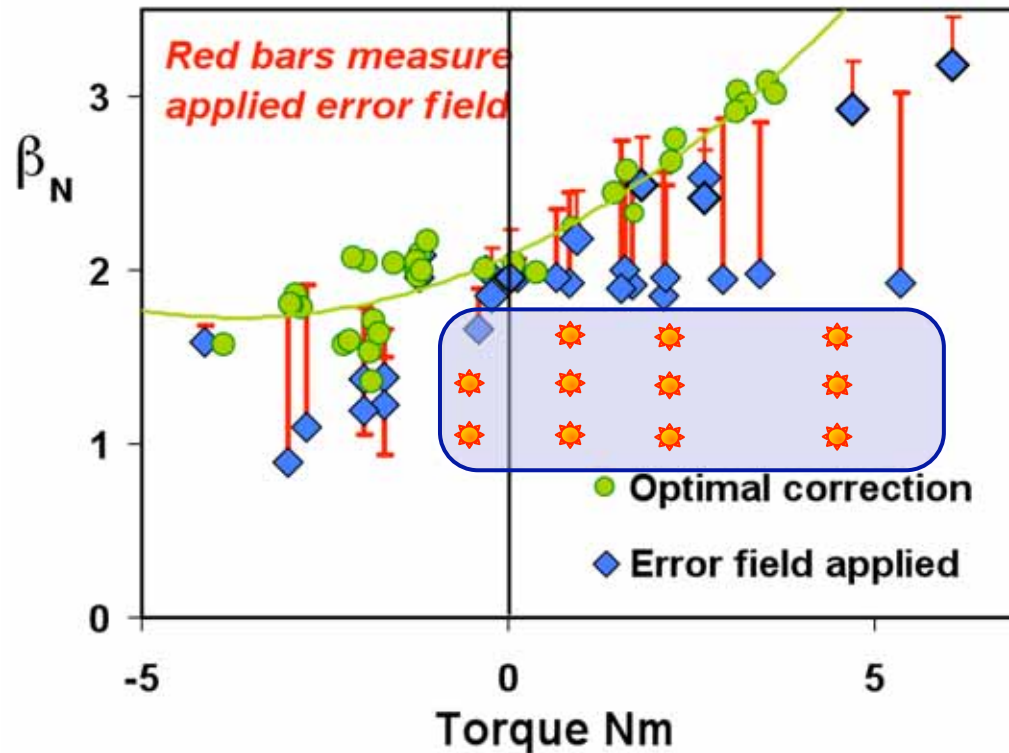
*Compare TM  $\beta$  limits with EF cases:*



- Error field required scales as ~ proximity in  $\beta$  to TM limit
- But effect through:
  - EF response changes?
    - With proximity to ideal or tearing limit?
  - Changes in underlying NTM stability?
  - Simple torque balance physics?

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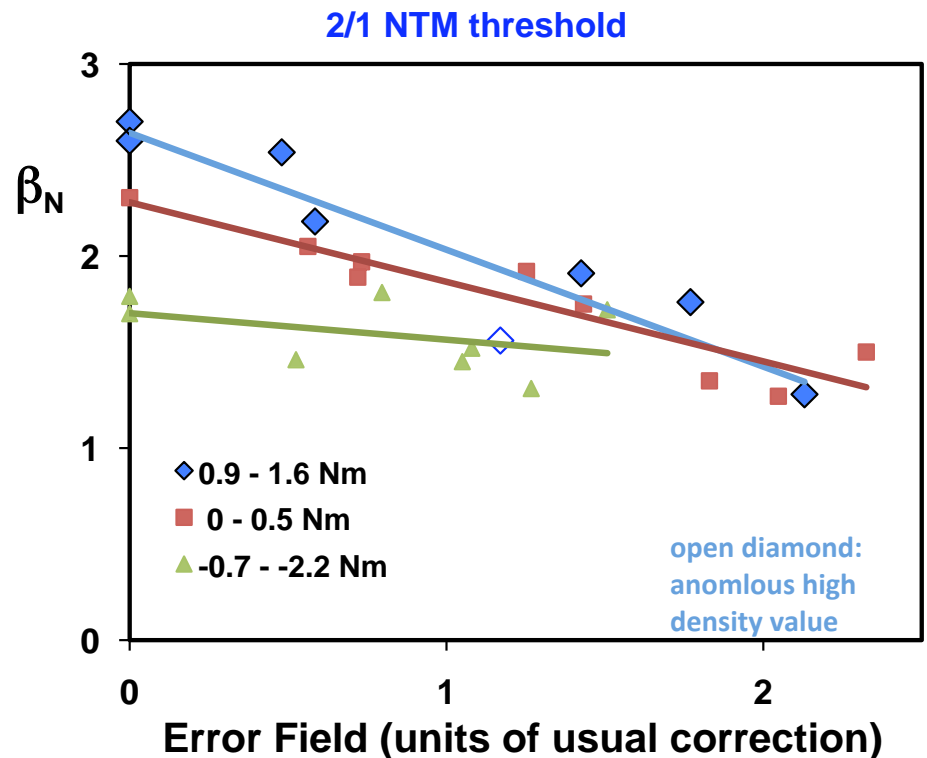
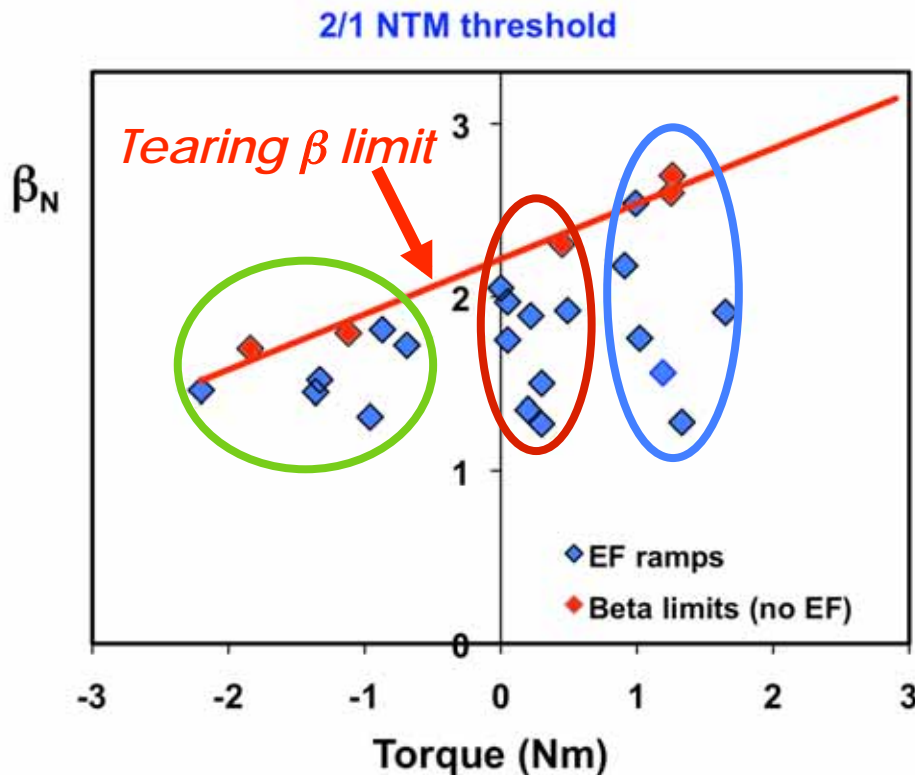
*New scans to probe this...*



# New Studies on DIII-D Just Executed

*– should get at question of EF response vs  $\Delta'$*

- Achieved broad scan of torque and  $\beta_N$ 
  - Measured EF response close to and far from **tearing  $\beta$  limit (red)**
  - Clear responses and variations observed

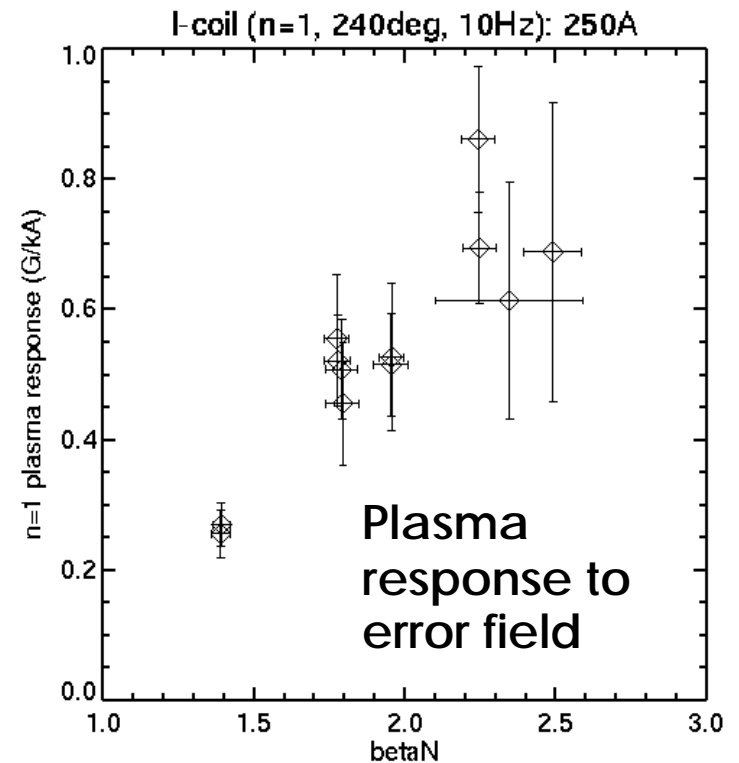


- Less error field needed to access mode with counter torque
  - Is this a rotation or a proximity to  $\Delta'$  effect - see in EF response... (tba)

# Clear variation in EF response with $\beta_N$

*...still analysing out torque dependence*

- Clearly error fields elicit strong response
  - Magnetic response increases
  - Not looked at all data yet! (just high co torque scan)



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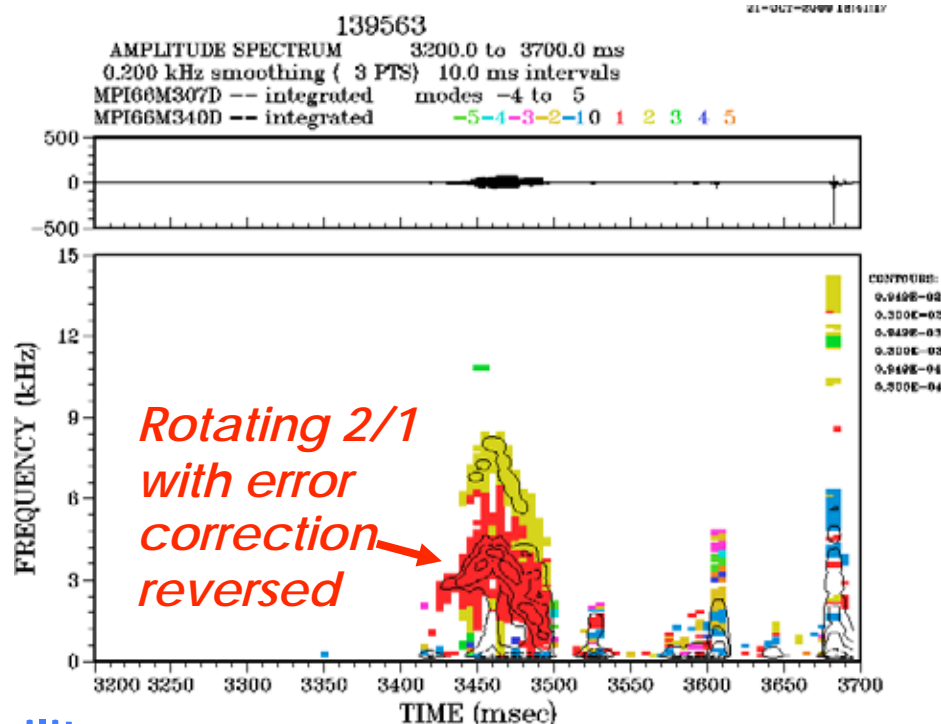
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- In all cases error field lead to rotating mode! →

- Even with lots of error field
- Error fields perturbing NTM stability

- Presumably through rotation shear
- Is there an increased magnetic response as tearing  $\beta$  limit neared?



# We still don't know H Mode Scalings for Error Field Thresholds

## *Still outstanding:*

Need to move on to extrapolation implications & physics tests

- Density scan
  - Lower  $q_{95}$
  - TF scan
- Torque balance of H mode beam driven plasma will be fundamentally different from Ohmic plasma:
    - Ohmic plasmas will have some natural rotation which scales with  $B_t$  and  $n_e$  – built into Ohmic scalings
    - Rotation scales differently with  $B_t$  and  $n_e$  in H mode?
      - *If so (likely!) then EF threshold will scale differently!*