

# Plans for MHD control in KSTAR

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On behalf of the **KSTAR** team

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# Outline

## I. In-Vessel Control Coils (IVCC) system

- IVCC system is to be implemented in KSTAR, as an actuator to provide the control of vertical & radial position control, field error correction (FEC), and resistive wall mode (RWM) feedback stabilization.

## II. Physical Requirements

- Vertical and radial position control coil
- FEC coil
- RWM control coil
- Other possible application including ELM control

## III. Neoclassical Tearing Mode control using ECCD

- Active suppression of  $m/n = 3/2$  and  $2/1$  NTMs will be pursued by using a 170GHz (2nd harmonic resonant with KSTAR reference scenario of which toroidal field is 3.5 T at magnetic axis) ECCD system for KSTAR. Results of a preliminary study and a prototype of control system are presented.

## IV. Issues and future works

- KSTAR operation schedule is presented. Remained issues and future works of MHD control on the basis of this schedule is addressed.

## V. Summary

# In-Vessel Control Coils System

# Plasma control capability of the KSTAR IVCC system

- **Main functions:**

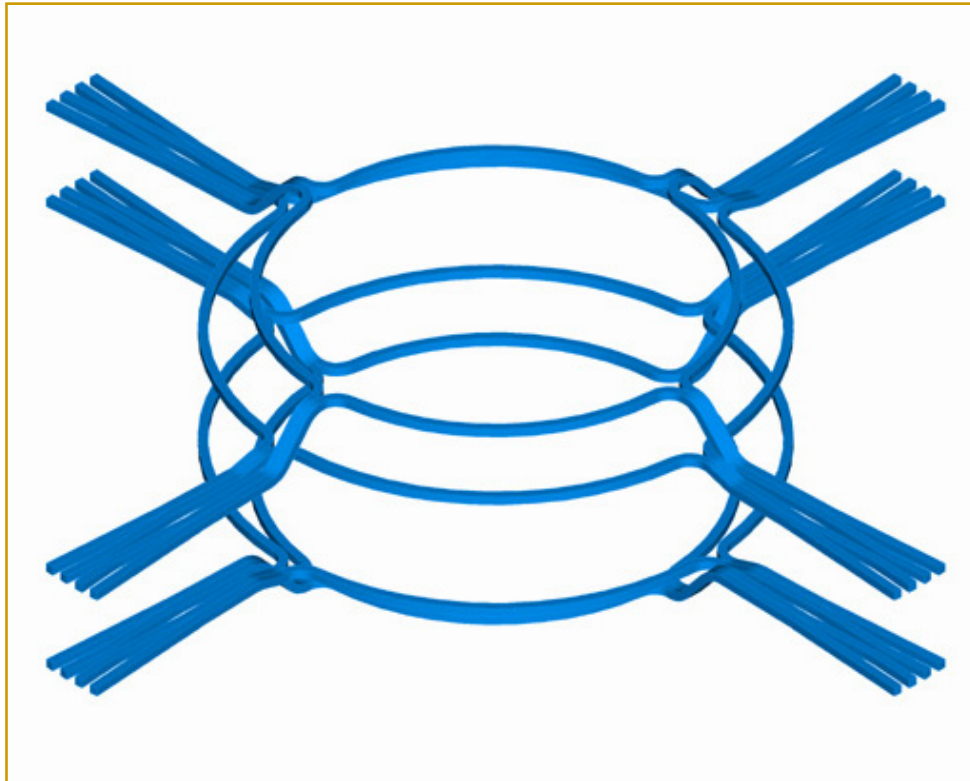
- Vertical position control ( $n = 0$ )
- Radial position control ( $n=0$ )
- Field error correction (FEC) ( $n \geq 1$ )
- Resistive Wall Mode (RWM) feedback stabilization ( $n \geq 1$ )

- **Additional possible control capabilities are under study.**

- Type-I ELM control
- Tearing mode control
- Local plasma rotation control
- Impurity control

# A schematic of KSTAR In-Vessel Control Coils (IVCC) system

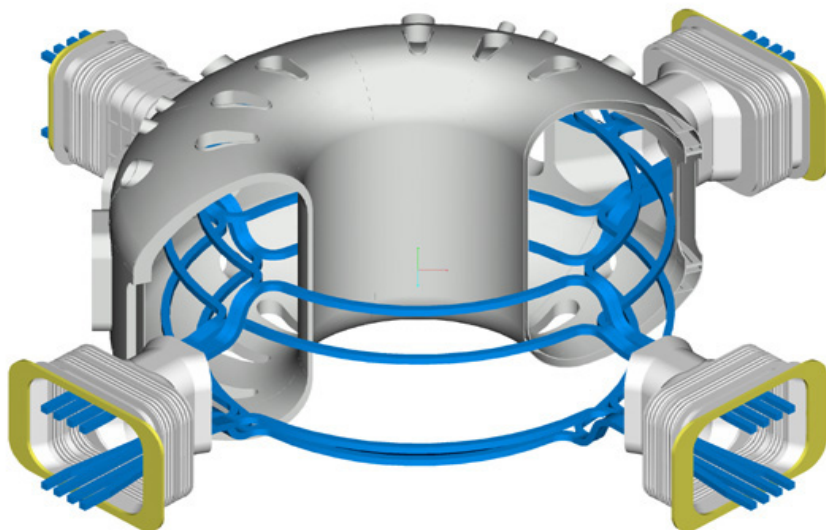
- IVCC is a unified coil system using toroidal segmentation concept



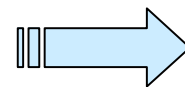
- **Each In-Vessel Control Coil is divided into four toroidal segments (at 4 positions in a poloidal section at p1, p2, p3, and p4, total 16 segments)**
- **Each segment is deformed to have lead parts, of which a proper connection can give a loop for plasma position control, FEC/RWM control.**

# Advantages of the Segmented IVCC design are

- Simplification in the **fabrication and installation**.
- Improvement in the **reliability** of the coil system.
- Easy **maintenance and repair**.
- Saving in in-vessel **space**.
- More improved plasma **control flexibility**.

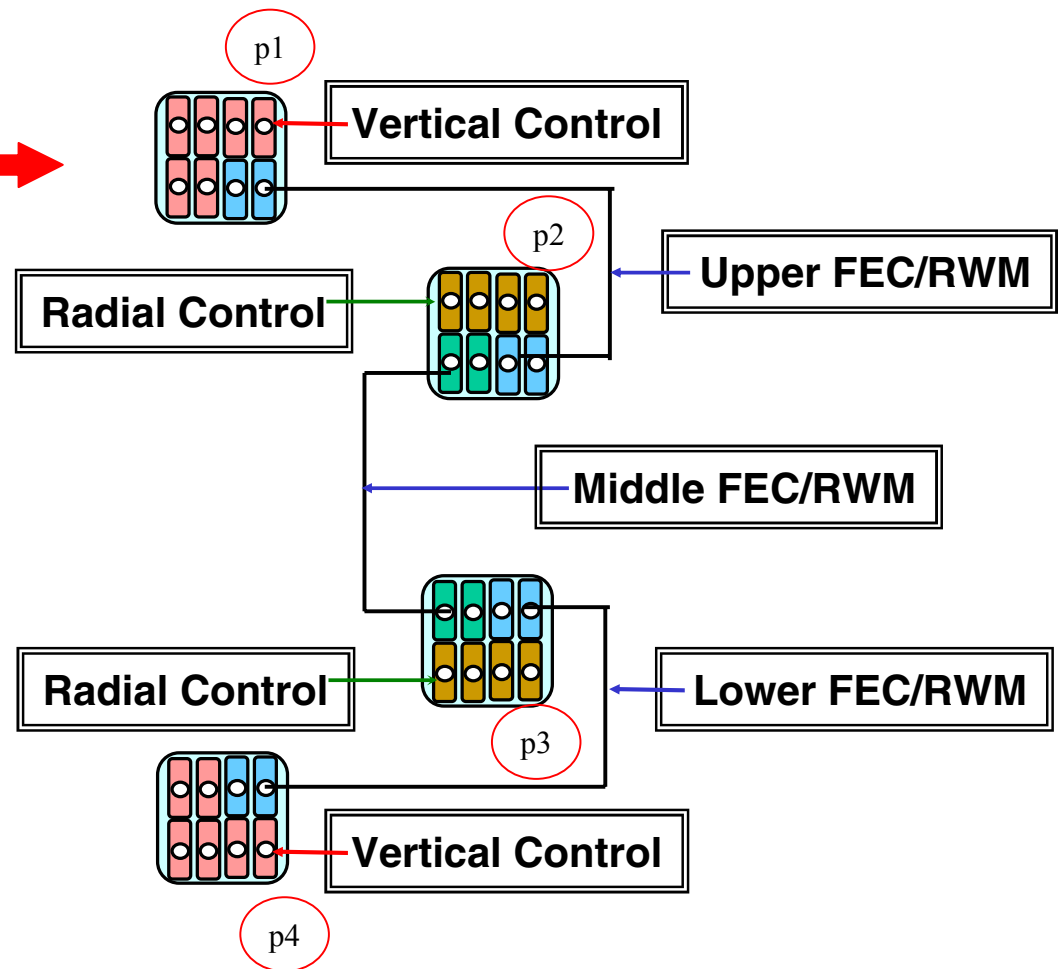


IVCC Installation is performed through three NBI and one RF type ports after main device assembly



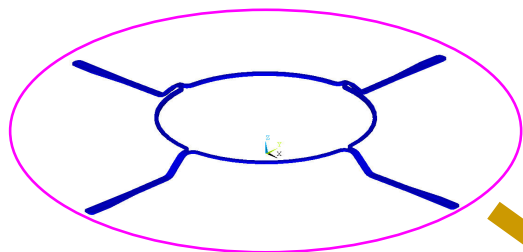
1:10 mock-up of the KSTAR VV & IVCC shows that the installation principle is possible.

- Each coil segment is composed of 8 copper sub-coils
- Figure shows a poloidal cross sectional view
- Pink sub-coils : connected to be IVC (internal vertical control) coils (2 sets of upper and lower)
- Mud yellow : connected to be radial control coils (upper and lower)
- Green : connected to be middle FEC/RWM control coils
- Blue : connected to be upper and lower FEC/RWM control coils

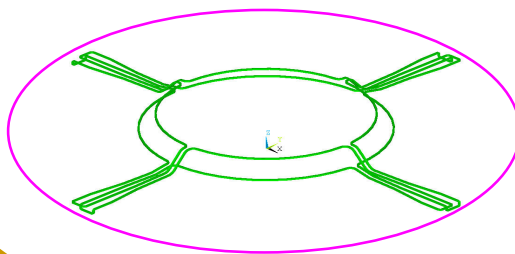


# Connection lines for position control and FEC/RWM coils in 3-D

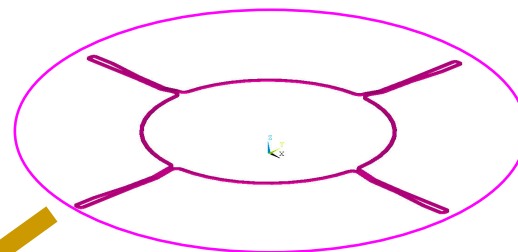
Upper Vertical Control Coil



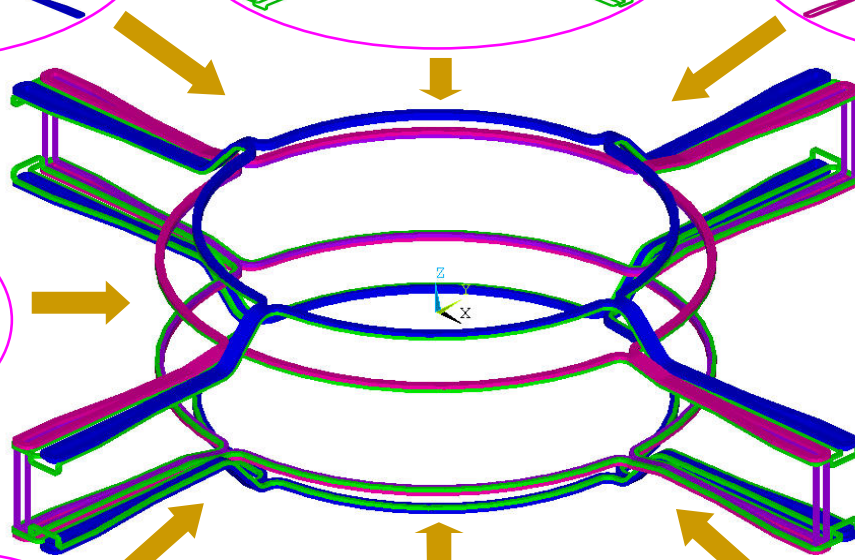
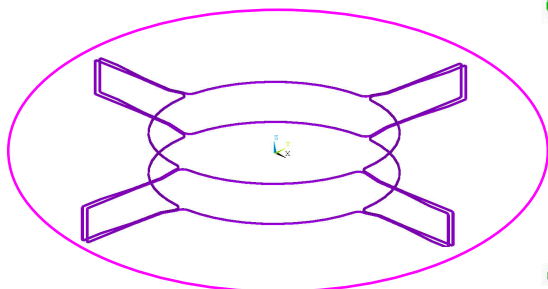
4 Upper FEC/RWM Coils



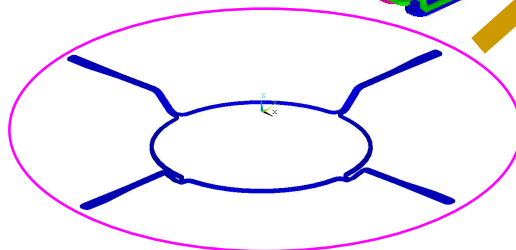
Upper Radial Control Coil



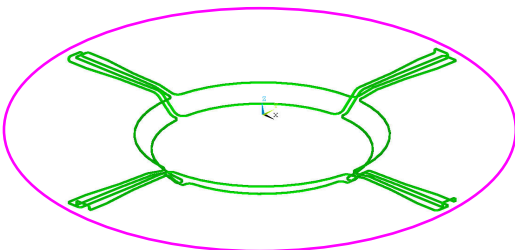
4 Middle FEC/RWM Coils



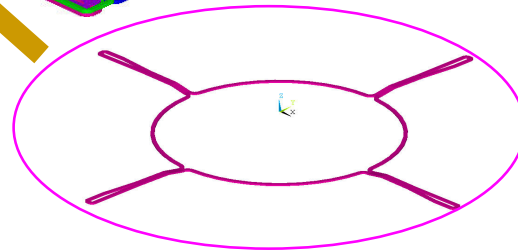
Lower Vertical Control Coil



4 Lower FEC/RWM Coils



Lower Radial Control Coil





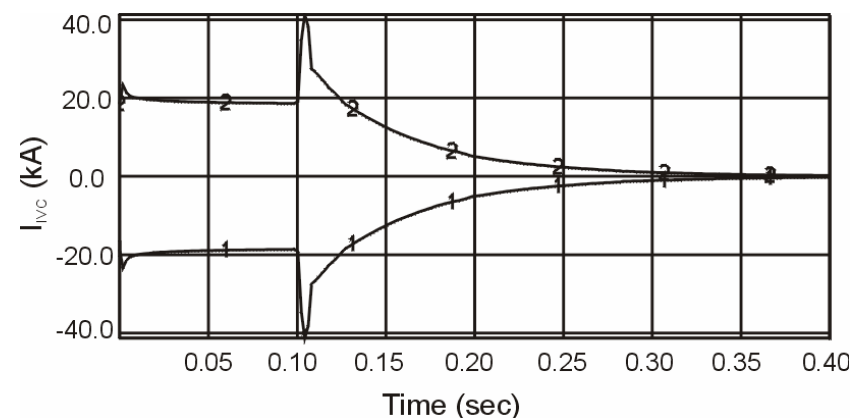
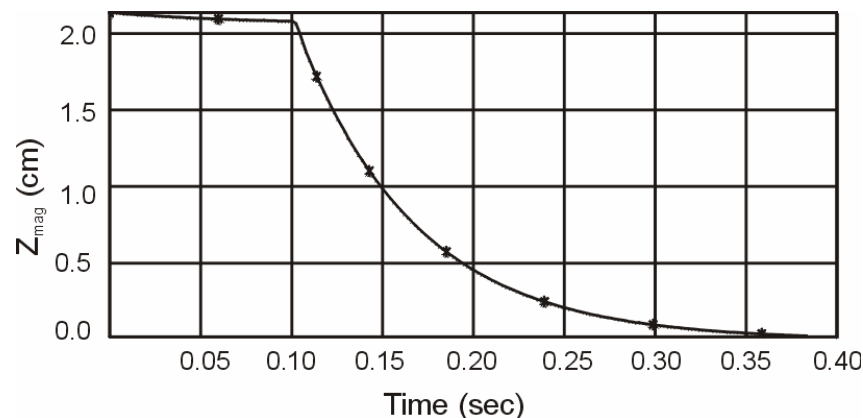
# Physical Requirements for

- Plasma Position Control
- Field Error Correction
- Resistive Wall Mode Control

# Plasma Position Control

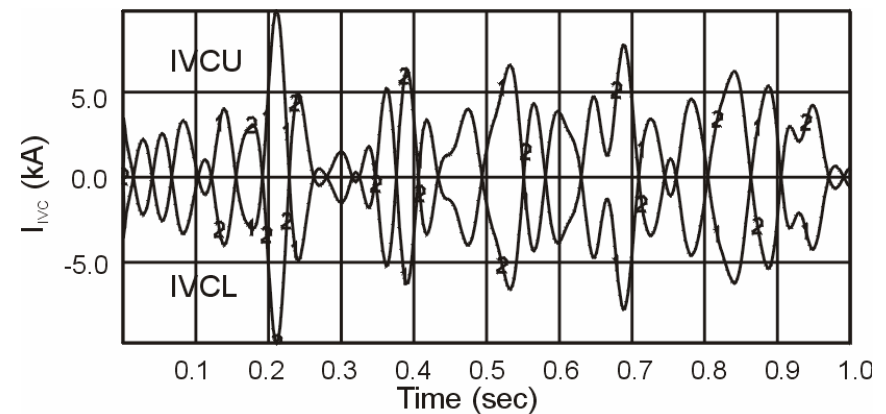
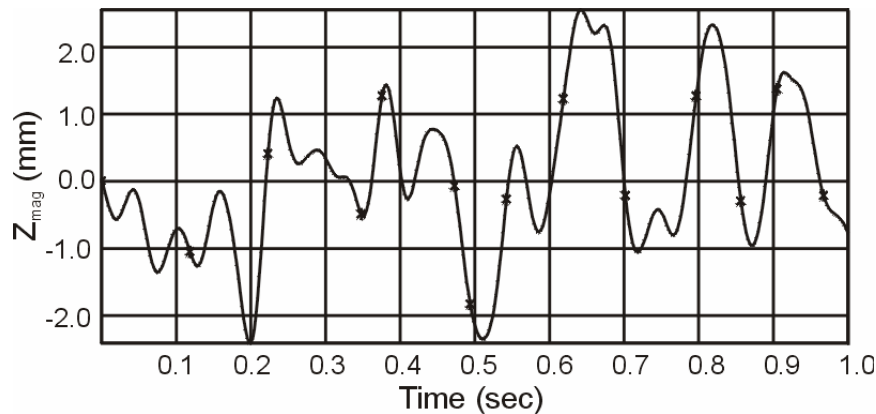
# Plasma vertical position control

- The **fast time-scale ( $\sim 10$  msec) plasma position control** is realized by using two pairs of inner control coils (**IVC** for vertical position control, **IRC** for radial position control).
- A **step response simulation** has been used to calculate the **IVC** current to hold a worst plasma ( $\beta_N=0.3$ ,  $I_i(3)=1.2$ ,  $I_p=2.0$  MA,  $\kappa=2.0$ ) 2 cm above mid-plane, and to bring it back to its original position within 200 msec. The maximum current (voltage) is found to be **42 kA-turns (123 V/turn)**.



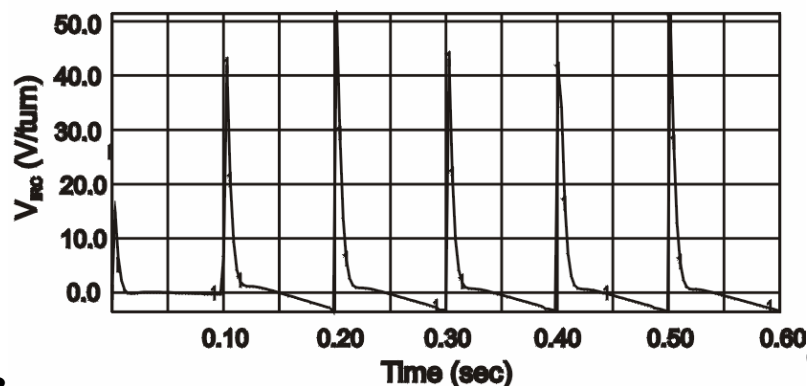
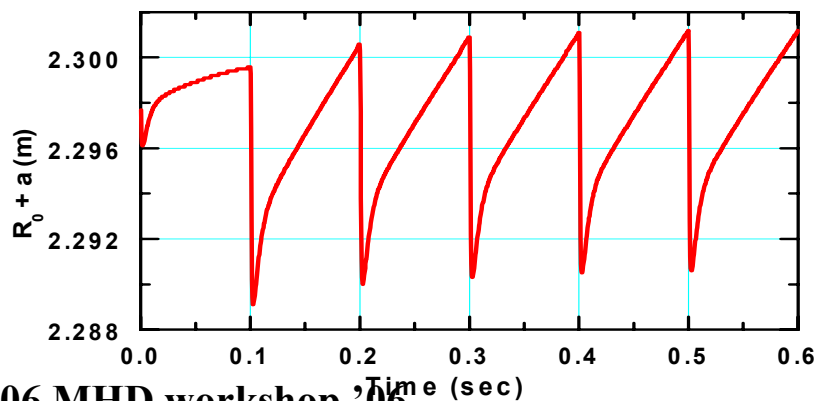
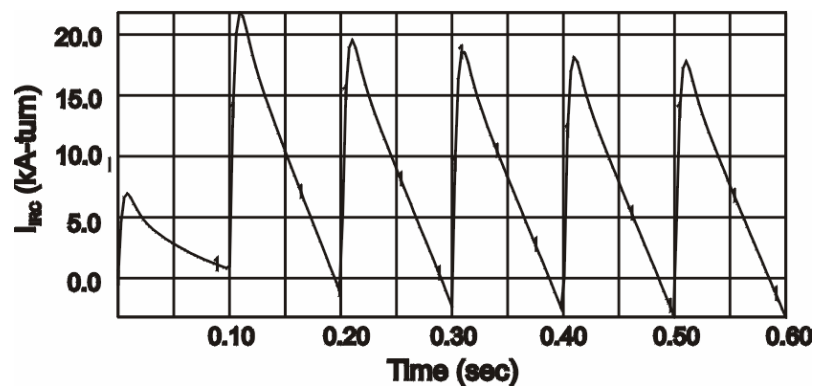
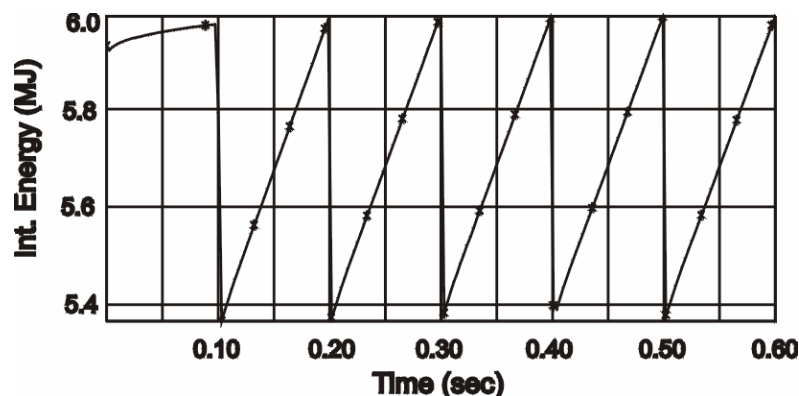
# Plasma vertical position control (cont.)

- **Random disturbance simulation** has been performed to evaluate the **IVC** power supply requirements. The random displacements in  $Z_{\text{mag}}$  are characterized by  $\Delta Z_{\text{rms}} = 1 \text{ mm}$ ,  $\Delta\omega = 1/\tau_z$ ;  $\tau_z = 18.0 \text{ msec}$  ( $\beta_N = 0.3$ ,  $I_i = 1.2$ ). The maximum feedback current (voltage) is found to be **9.8 kA-turns (8V/turn)**.



# Plasma radial position control

- Power supply requirements for **IRC** are calculated for a high  $\beta$  plasma ( $\beta_N = 5.0$ ,  $I_i = 0.8$ ,  $I_p = 2$  MA) undergoing **10 % drop in stored energy every 100 msec ( $\sim \tau_E$ ) with recovery**. This 10% drop is assumed to be worst **recoverable** event. The maximum feedback current (voltage) in **IRC** is found to be **22 kA-turns (52 V/turn)**.



# Field Error Correction

# Field error calculation

- Definition of Fourier harmonics  $A_{mn}$  and  $A_{3\text{-mode}}$

$$c_{mn} = \frac{1}{2\pi^2 B_0} \int_0^{2\pi} \int_0^{2\pi} B_r \cos(n\phi - m\theta) d\theta d\phi,$$

$$s_{mn} = \frac{1}{2\pi^2 B_0} \int_0^{2\pi} \int_0^{2\pi} B_r \sin(n\phi - m\theta) d\theta d\phi,$$

$$A_{mn} = \sqrt{c_{mn}^2 + s_{mn}^2},$$

$$A_{3\text{-mode}} = \left[ A_{21}^2 + 0.8 A_{31}^2 + 0.2 A_{11}^2 \right]^{1/2} : \text{based on DIII-D scaling}$$

$B_0$  : magnetic field at the geometrical axis (3.5 T for KSTAR)

- $B_r$  : error field component normal to (2, 1) surface, over which the integration is carried out
- Correction current then calculated to reduce the estimated field error below the following threshold values for locked modes;

$$A_{21} = 1 \times 10^{-4}, A_{m1} = 2 \times 10^{-4} \quad (m = 1, 3, 4),$$

$$A_{42} = 2 \times 10^{-4}, A_{m2} = 4 \times 10^{-4} \quad (m = 3, 5), A_{3\text{-mode}} = 2 \times 10^{-4}$$

## Field error calculation (cont.)

- Field error magnitude calculated, considering possible all sources;
  - PF coil winding irregularities
  - Bus and lead wires
  - Welded joints of V V
  - PF & TF coil misalignments and manufacturing error (shift, tilt)

\* total 232 sources considered



# Calculated field error from PF winding

PF No	$A_{11}$	$A_{21}$	$A_{31}$	$A_{41}$	$A_{3-mode}$
1	2.10	2.74	0.22	0.89	2.91
2	0.11	0.01	0.09	0.05	0.09
3	0.34	0.05	0.18	0.05	0.23
4	0.35	0.11	0.18	0.02	0.25
5	1.16	1.04	0.35	0.28	1.20
6	0.89	0.24	0.32	0.07	0.55
7	0.13	0.64	0.22	0.07	0.67

(\* 10<sup>-5</sup>)

- ✓ Considered PF coil currents are at Start Of Flattop (SOF), when plasma density and rotation allow lower field error, of reference discharge condition as

PF No.	1	2	3	4	5	6	7
coil current (MA)	-3.546	0.126	0.194	0.358	1.426	-0.561	-0.845

- ✓ ~ 10 % of the threshold value

## Field error from PF and TF bus-lines

(\* 10<sup>-6</sup>)

coil	A <sub>11</sub>	A <sub>21</sub>	A <sub>31</sub>	A <sub>41</sub>	A <sub>3-mode</sub>	A <sub>32</sub>	A <sub>42</sub>	A <sub>52</sub>
CS1	7.37	2.82	0.56	0.38	4.37	0.25	0.12	0.04
CS2	4.95	1.13	0.61	0.24	2.54	0.27	0.18	0.05
CS3	10.42	2.06	1.36	0.49	5.24	0.53	0.26	0.11
CS3	3.03	1.39	0.72	0.32	2.05	0.30	0.14	0.07
CS4	5.91	0.71	0.83	0.16	2.83	0.31	0.08	0.08
CS4	1.69	0.79	0.42	0.18	1.16	0.17	0.08	0.04
PF5	1.24	0.59	0.30	0.10	0.85	0.18	0.06	0.04
PF5	0.56	0.25	0.13	0.04	0.37	0.05	0.02	0.01
PF6	0.11	0.05	0.03	0.02	0.07	0.05	0.01	0.01
PF6	0.28	0.20	0.09	0.03	0.25	0.06	0.02	0.01
PF7	0.51	0.50	0.29	0.09	0.61	0.25	0.08	0.04
TF	1.69	0.81	0.34	0.13	1.15	0.30	0.10	0.03

- This is calculated on the basis of 1MA coil currents
- The results show ~ 1 % of threshold values : minor field error source
  - Field error from PF bus-line is proportional to PF coil current.

## Field error from vacuum vessel weld joints ( $\mu_r > 1$ )

- For SOF (Start of Flattop) coil current :

(\*  $10^{-5}$ )

$\mu_r$	$A_{11}$	$A_{21}$	$A_{31}$	$A_{41}$	$A_{3-mode}$	$A_{32}$	$A_{42}$	$A_{52}$
1.05	0.30	0.20	0.16	0.09	0.28	0.08	0.04	0.02
1.10	0.57	0.42	0.32	0.15	0.56	0.17	0.10	0.03
1.15	0.87	0.62	0.44	0.24	0.83	0.20	0.14	0.10
1.20	1.17	0.82	0.59	0.33	1.11	0.28	0.17	0.14
1.25	1.47	1.07	0.71	0.37	1.41	0.37	0.21	0.13
1.30	1.72	1.25	0.85	0.46	1.65	0.44	0.25	0.17

- It makes field error ~ 10 % of the threshold value.
- Field error is proportional to the deviation of relative permeability from unity.

## 3-Mode Harmonics for 2mm installation errors

(1.0E-6)

PF	Shift	Tilt	Elongation
1	13.12	9.17	0.0017
2	10.02	6.85	0.0018
3	7.71	4.74	0.0010
4	5.73	3.31	0.0008
5	4.28	1.49	0.0009
6	8.43	4.33	0.0010
7	8.19	5.93	0.0014

- Gives max. ~10% of field error threshold

- Using the random number simulation (1000000 ~ 1500000 sampling) to reduce the calculation size

- Normal distribution

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$

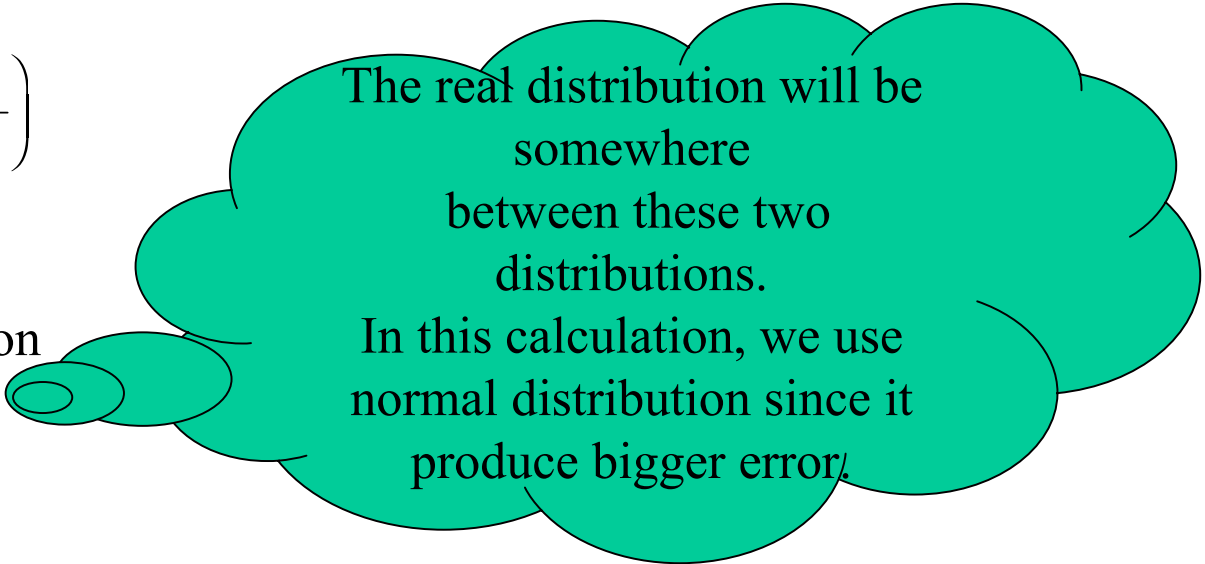
$$\int_{-\sigma}^{\sigma} f(x)dx = 0.6827$$

$\sigma$  : standard deviation

- Unit distribution

$$f(x) = \begin{cases} \frac{1}{2\Delta}, & -\Delta < x < \Delta \\ 0, & \text{otherwise} \end{cases}$$

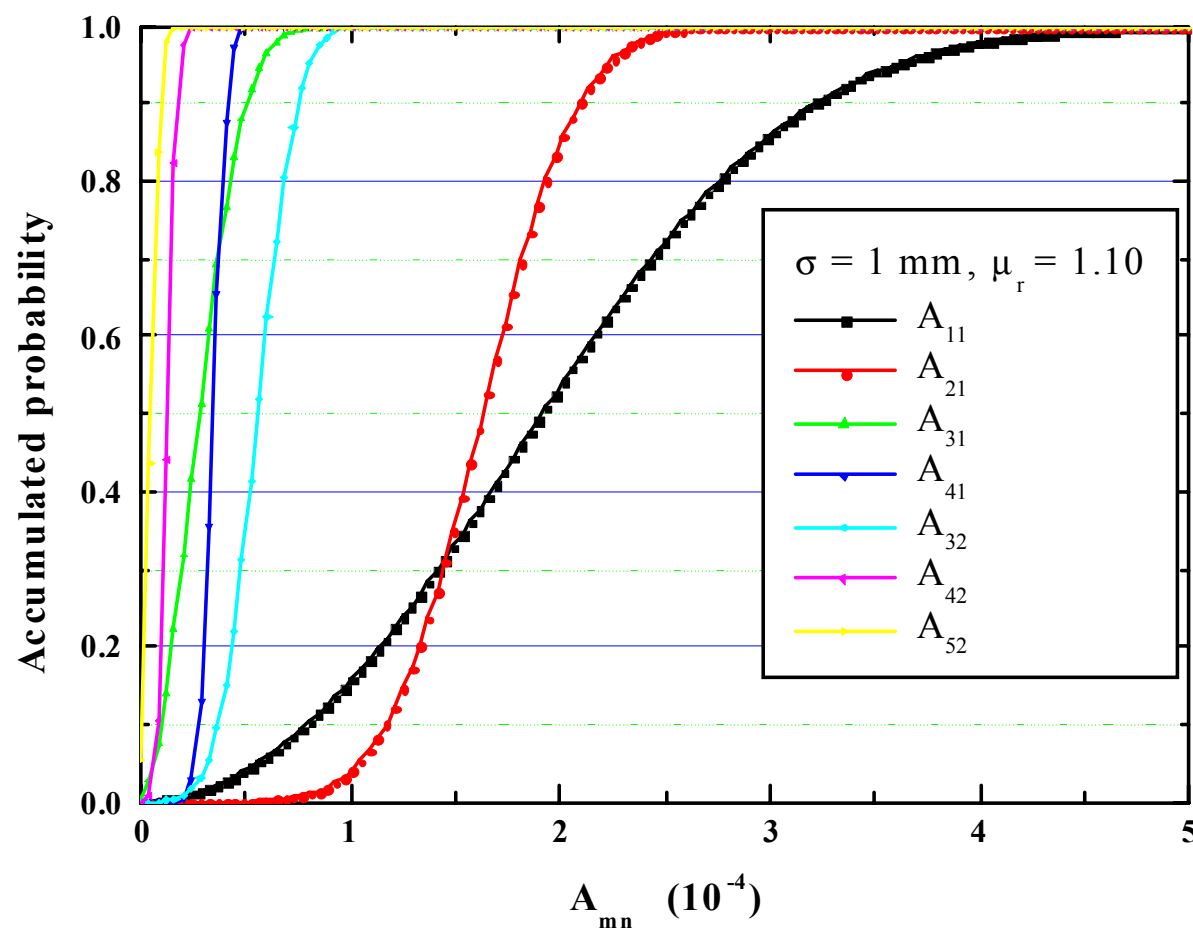
$\Delta$  : the accuracy of alignment



The real distribution will be somewhere between these two distributions.

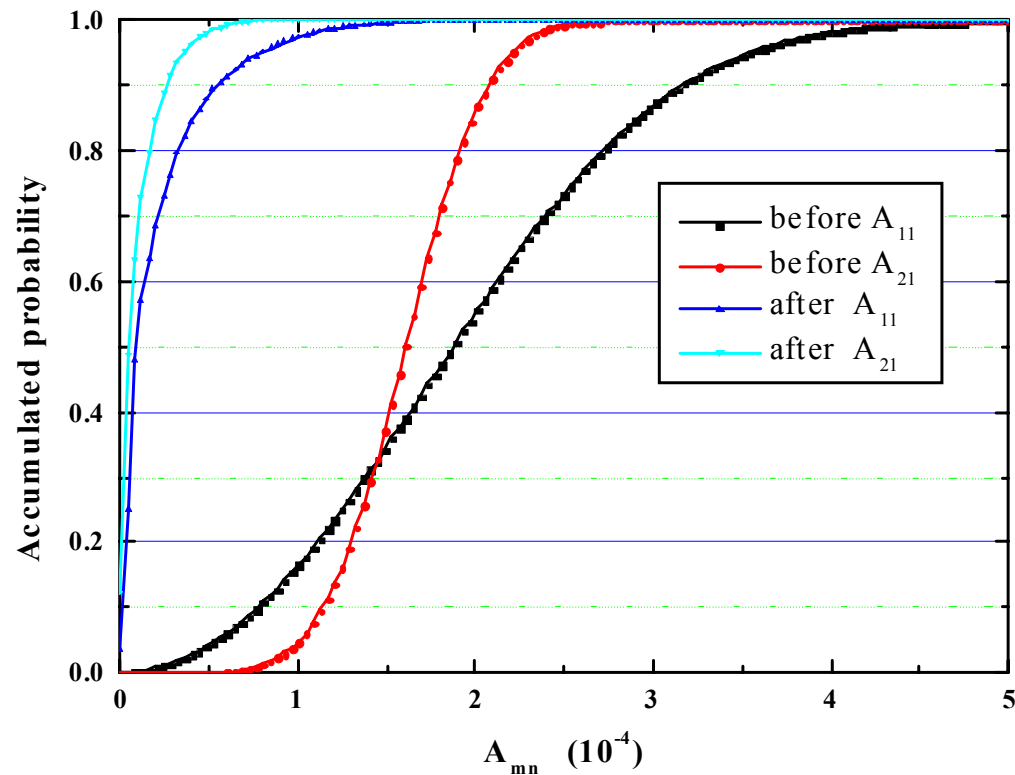
In this calculation, we use normal distribution since it produce bigger error.

# Calculated field error considering all the sources



- 1/1 and 2/1 modes are expected to be biggest.

# Field error correction current requirement is calculated



Before and after error correction with the correction current limit **6.5 kA** when  $\sigma=1$  mm,  $\mu_r=1.10$

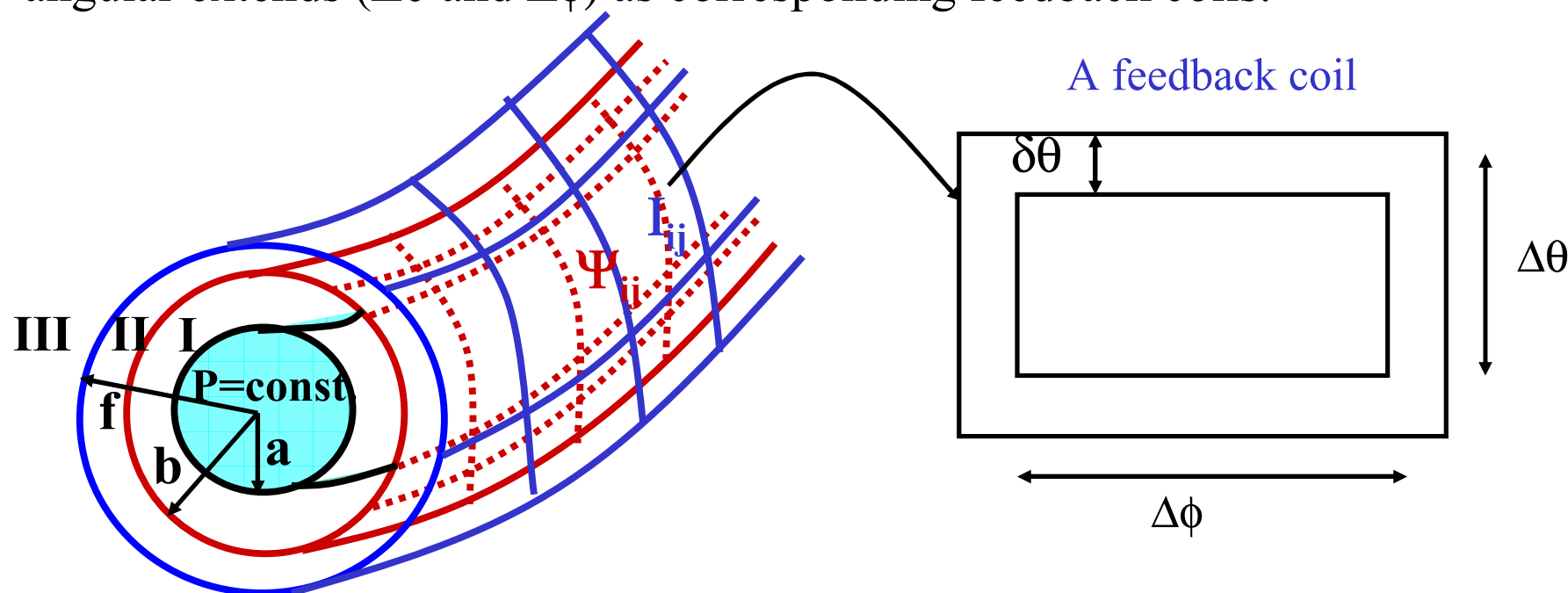
- Maximum **13 kA** of correction current is necessary to correct field error up to  **$n = 2$  mode** with **99.8 % confidence** when standard deviation  $\sigma = 1.5$  mm, magnetic permeability of the welded joint  $\mu_r = 1.10$

# Resistive Wall Mode Control

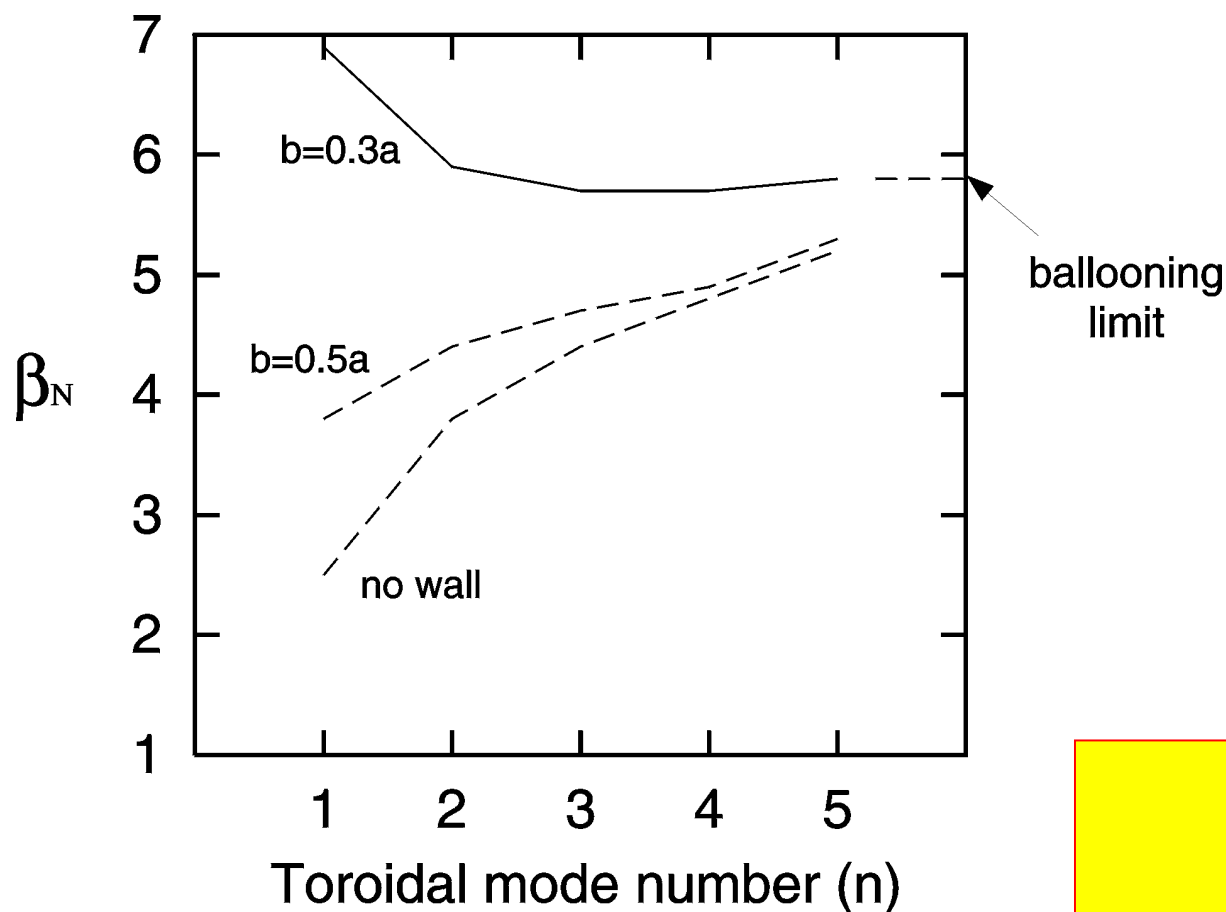


# RWM control – model for calculation

- A **toroidal, circular, surface plasma model ( $r=a$ )** with **resistive wall** at  $r=b$  and **feedback coils** at  $r=f$  is considered. Feedback coils and resistive wall are modeled by **surface current distributions** at  $r=b$  and  $r=f$ , respectively.
- **Sensors** are assumed to be located at  $r=b$  with same poloidal and toroidal angular extends ( $\Delta\theta$  and  $\Delta\phi$ ) as corresponding feedback coils.



# Idel MHD stability for the reversed-shear mode



- Ballooning stable up to  $\beta_N = 5.8$
- Continuous conformal wall with plasma-wall separation  $b < 0.3a$  can make kink limit to exceed ballooning limit

for KSTAR  $b \sim 0.15a$

✓ RWM control is important to get a high-beta plasma

# Passive stabilization by toroidal plasma rotation

## ◆ Toroidal rotation frequency in KSTAR

calculated by balancing momentum input by NBI & momentum loss by anomalous transport and assuming  $\tau_M \sim \tau_E$  with  $\tau_E$  by ITER-89 scaling

$$\begin{aligned} \omega_f / \omega_A &= (V_B P_B q \cos \psi_B \tau_M) / (V_A V_P \langle n \rangle e V_B) \\ &\sim 0.015 H_{\text{factor}} P_B^{1/2} (\text{MW}) / \langle n \rangle^{1/2} (10^{20} \text{ m}^{-3}) \\ &\sim 0.069 \end{aligned}$$

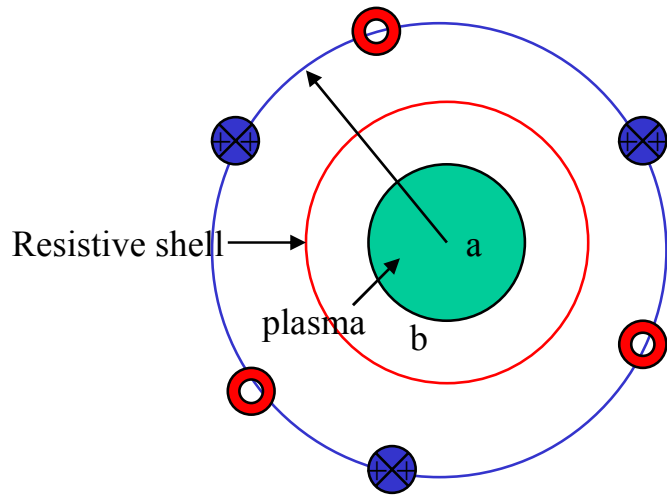
where  $\omega_A = V_A / 2\pi R q$ , Alfvén frequency, and we assumed the KSTAR parameter values,  $V_B = 120 \text{ keV}$ ,  $\psi_B \sim 30^\circ$ ,  $V_P = 16 \text{ m}^3$ ,  $P_B = 2.7 \text{ MW}$  (baseline NBI power),  $\langle n \rangle = 0.5 \times 10^{20} \text{ m}^{-3}$ , and  $H = 2$ .

## ◆ Rotational stabilization might be possible

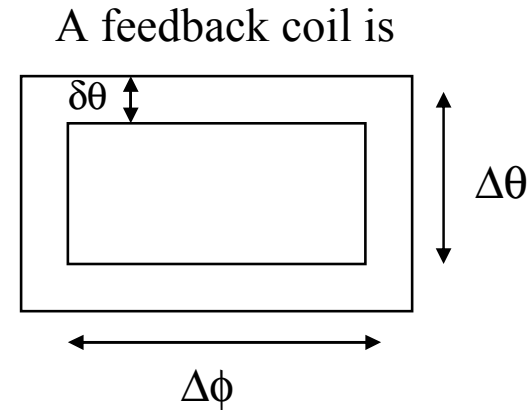
$(\omega_f / \omega_A)_{\text{threshold}} \sim 0.033$  for TPX passive plate, similar to KSTAR  
(cf. D.J. Ward, Phys. Plasmas **3** 3653 (1996))

\* **FEC is important**, to avoid the rotation damping by field error amplification  
above no-wall beta limit

# Active control of resistive wall mode : I. cylinder model



Feedback coils (current density distribution)



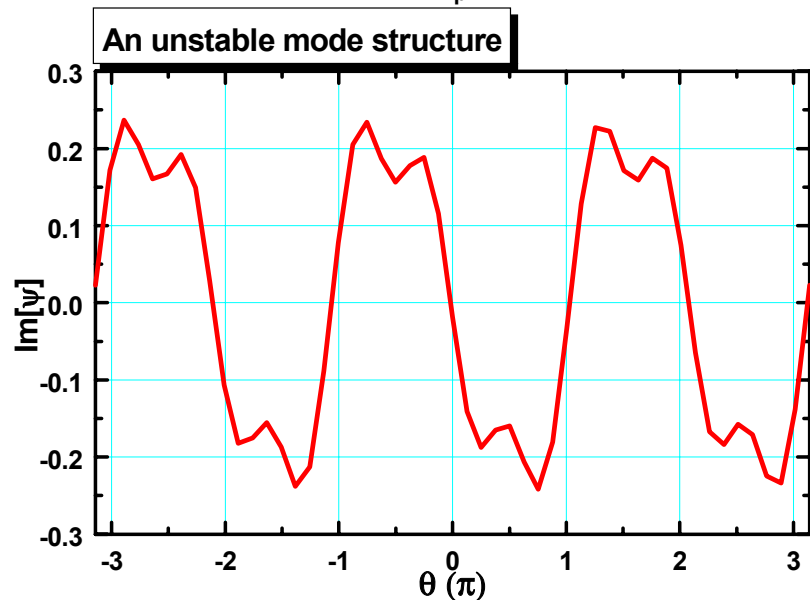
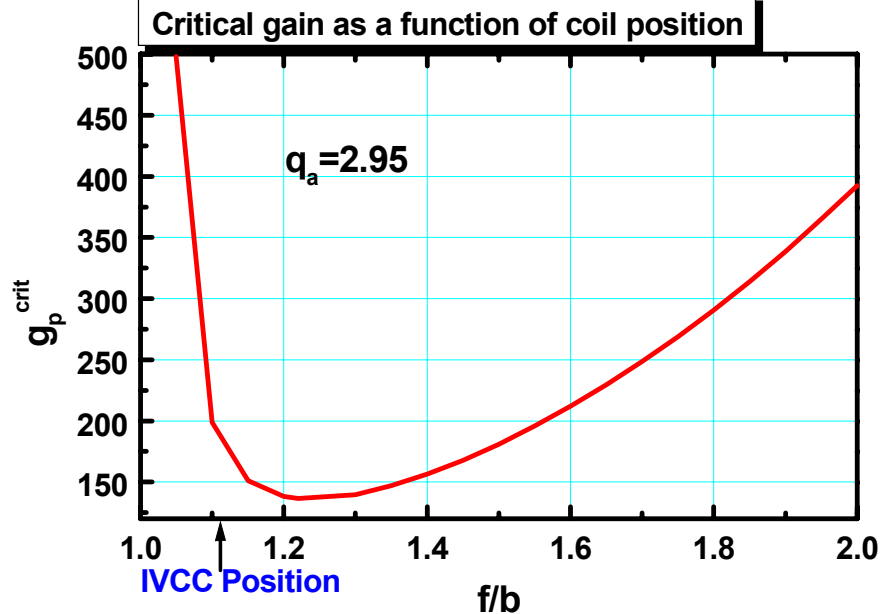
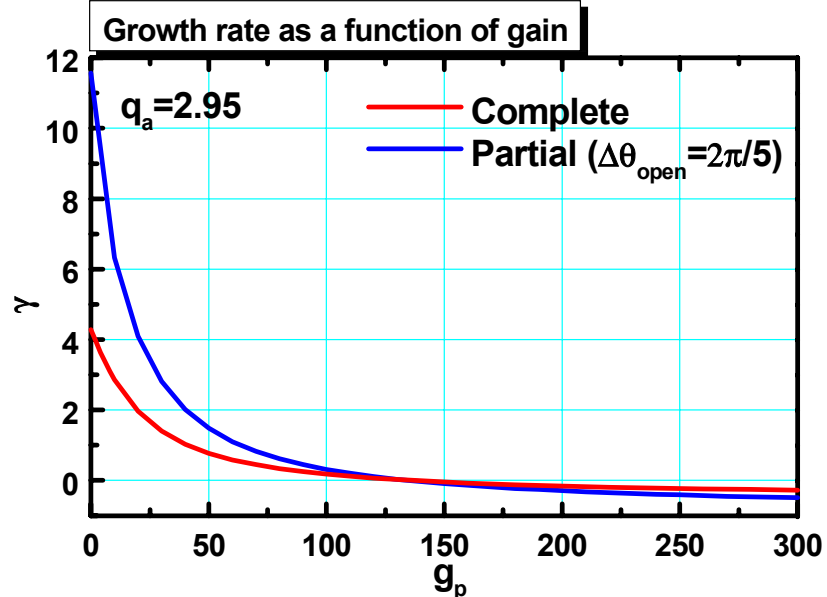
*An eigenvalue equation set of RWM growth rate including feedback coil effect is*

$$(\vec{A} - \vec{B}\gamma - \vec{C}\gamma^2) \cdot \vec{\zeta} = \vec{0} \text{ where}$$

$$C_{lm}\zeta_m = (1/f)U_{lk}^T g_d^{kn} \Phi_{ni} \delta_{ij} [\psi_{jm}]_{r=b} \zeta_m$$

$$B_{lm}\zeta_m = (\mu_0 \sigma_{lk} \delta_{kj} + 1/f [U_{lk}^T g_p^{kn} \Phi_{ni} \delta_{ij}][\psi_{jm}]_{r=b} + i\delta_{lk} [\frac{\partial \psi_{km}}{\partial r}]_{r=f-\epsilon}^{r=f+\epsilon}) \zeta_m$$

$$A_{lm}\zeta_m = (1/f) [U_{lk}^T g_l^{kn} \Phi_{ni} \delta_{ij}][\psi_{jm}]_{r=b} \zeta_m$$



The required feedback current is estimated to be **2.4 kA-turns**.

$$\begin{aligned}
 I_k &= \frac{\delta\theta}{2R_0\Delta\phi\mu_0} g_p \Phi_k \\
 &\approx -200 \times (\pi/30) \times (\pi/6) \times 0.53 \times B_r / \mu_0 \\
 &\approx 2.4 \text{ kA}
 \end{aligned}$$

Other possible applications of KSTAR IVCC for advanced physics studies are 

- **Edge Localized Mode control**

- ELM suppression by  $n=1$  or 2 (due to the geometry of the IVCC system) resonant magnetic perturbation with currents up to 6 kA (ref. DIII-D case : 4 kA)

- **Tearing mode control**

- Suppression/generation of tearing modes by resonant or non-resonant helical magnetic perturbations

- **Plasma rotation and transport control**

- Local & temporal reduction of plasma rotation by magnetic islands generated using helical perturbation
- Fluctuation suppression by local flow shear
- Need to check the possibility of the enhancement of electron transport or the destabilization of tearing or NTM modes.

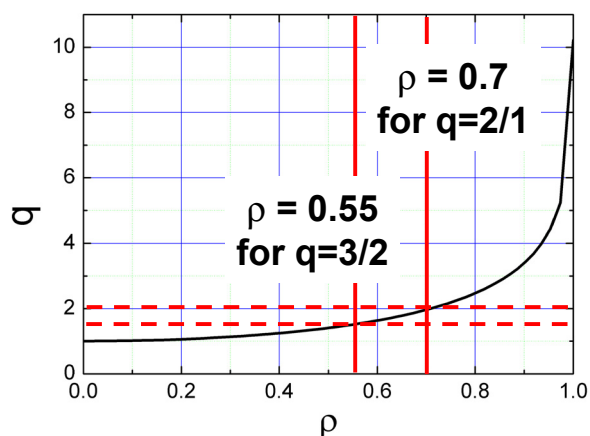
- **Impurity transport control**

- Static island generation near plasma edge

# Neoclassical Tearing Mode Control : a preliminary work

# NTM control- EFIT equilibrium profiles used in TORAY-GA code

- Reference Plasma: The reference Double Null (DN) plasma parameters are presented in Table 1 (column 2). The EFIT model developed at GA was used to produce an equilibrium close to these parameters.



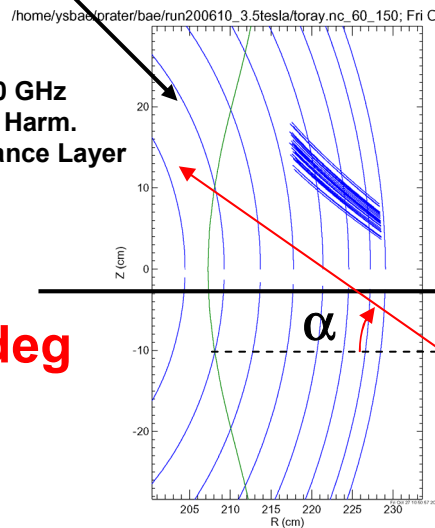
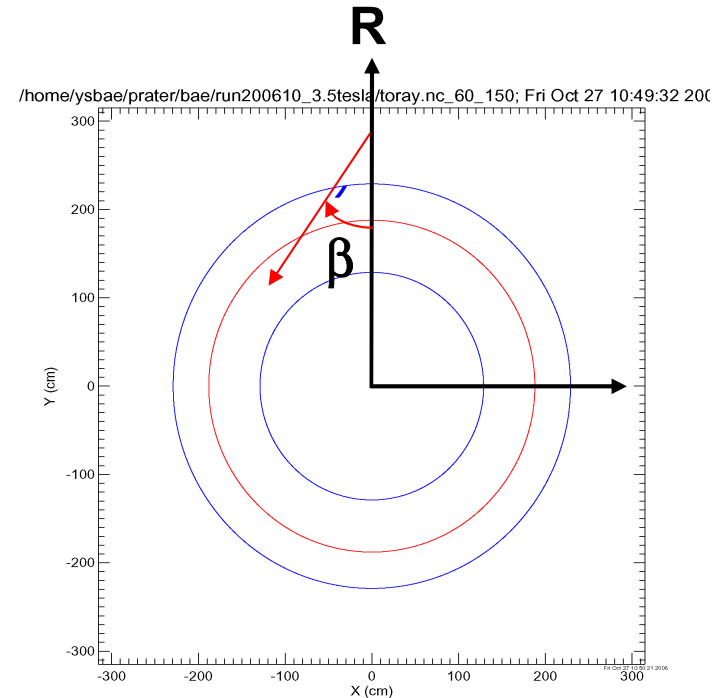
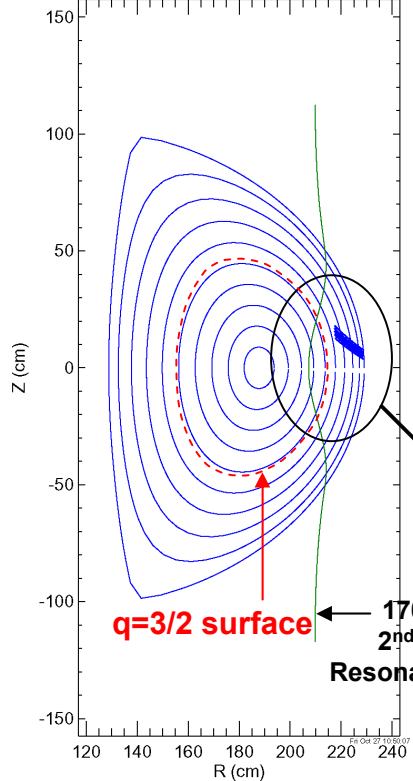
Plasma Parameters	KSTAR Reference DN Equilibrium	Reference EFIT	High <i>li</i> EFIT
Eqdsk File	--	g010004.01020	g010004.01000
$B_\phi$	3.5 T	3.5 T	3.5 T
$I_p$	2.0 MA	2.0 MA	2.0 MA
$R_o$	1.8 m	1.79 m	1.79 m
$a$	0.5 m	0.501 m	0.499 m
$\kappa_x$	2.0	2.00	2.01
$\delta_x$	0.8	0.80	0.80
$\beta_\phi$	4%	4%	4%
$\beta_n$	3.5	3.53	3.51
$l_i(1)$	--	1.01	1.14
$l_i(3)$	0.8	~ 0.8*	~ 0.9*
$q_{95}$	--	3.9	3.83
* EFIT calculates $li(1)$ ; $li(3) \sim 0.8 * li(1)$ ; (--) Information not available			

From J. Leuer, GA Engineering Physics Memo (July 30, 2004).



# Geometry for 170 GHz ray tracing and EC-wave injection angles

/home/ysbae/prater/bae/run200610\_3.5tesla/toray.nc\_60\_150

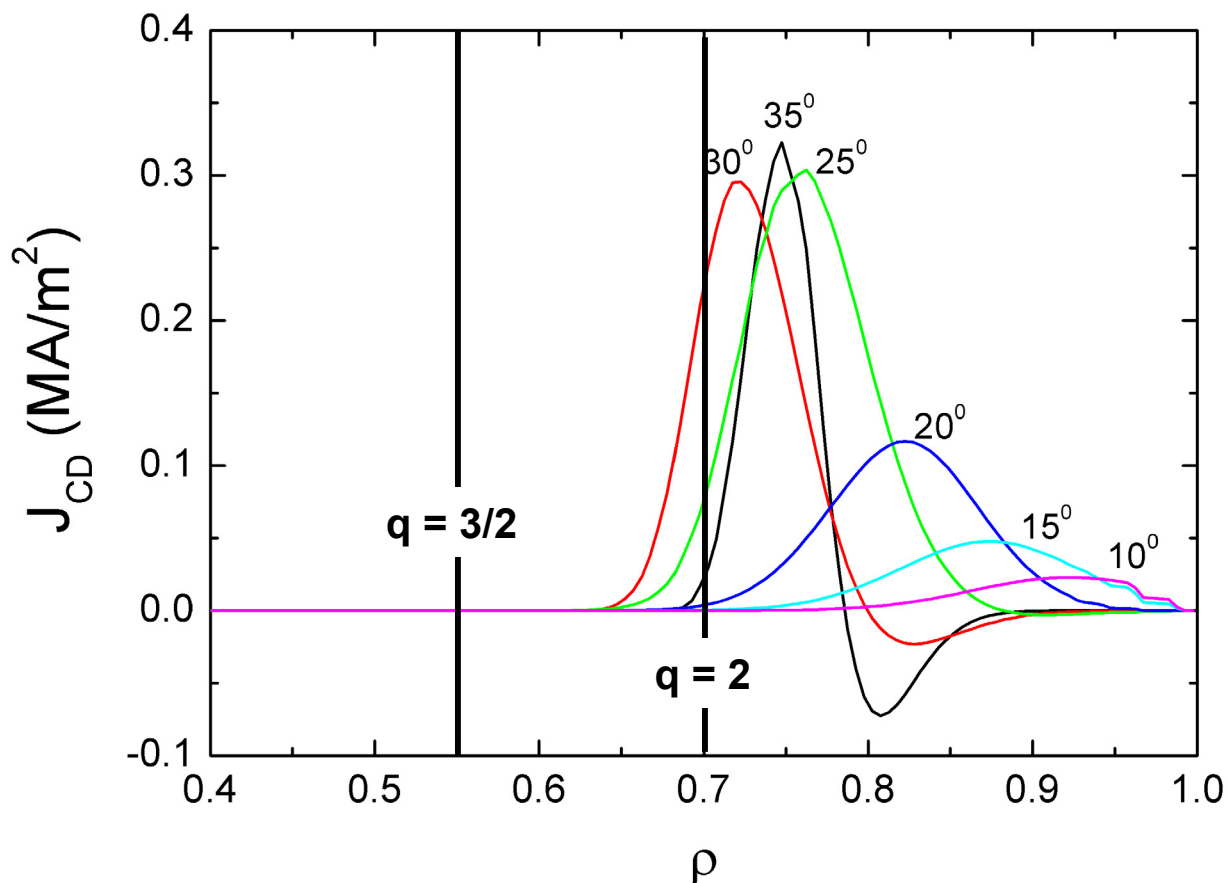


$\alpha$ : poloidal angle  
 $\beta$ : toroidal angle

e.g.  $\alpha = 30$  deg,  $\beta = 30$  deg

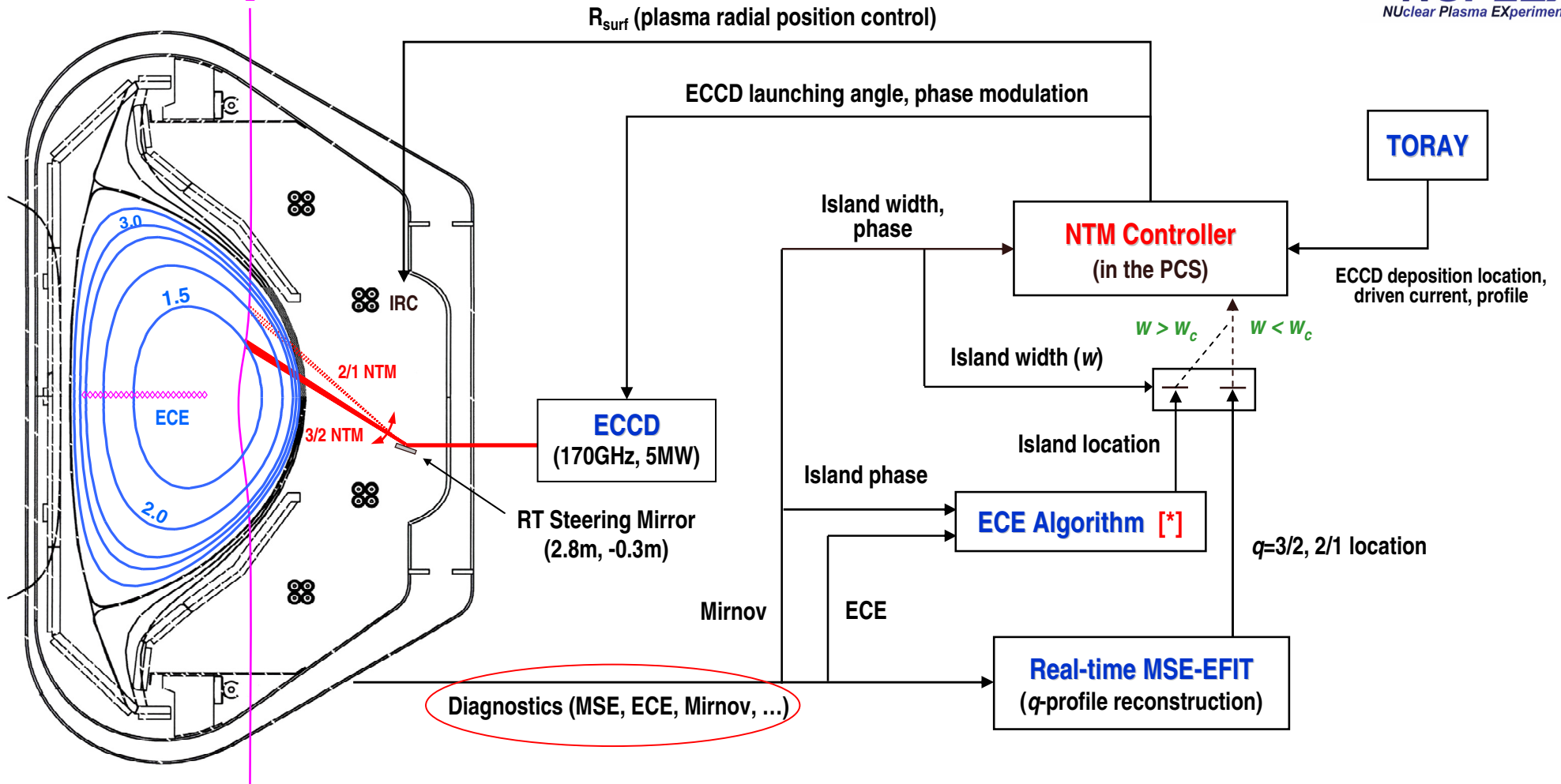
Mirror pivot position  
 (R = 2.8 m, Z = -0.3 m)  
 → Lower row in Equatorial Port

# Driven current density profiles ( $\beta = 30$ deg)



Profiles of the driven current density for poloidal launched angles and for 5 MW of EC power injected as X2-mode with  $\beta = 30$  deg. When  $\alpha$  is around 30 deg, the current induced on the  $q = 2$  surface is highest.

# Conceptual Design of KSTAR NTM Control System



2<sup>nd</sup> Harmonic resonance of 170GHz EC wave ( $R \approx 2.1m$ )

[\*] : Y. S. Park et al 2006 *Plasma Phys. Control. Fusion*

# Calculation of MRE Under KSTAR Ref. DN Equilibrium

## • Modified Rutherford Equation :

$$\frac{\tau_R}{r} \frac{dw}{dt} = \underbrace{\Delta' r}_{(1)} + \epsilon^{1/2} \underbrace{\left( \frac{L_q}{L_p} \right)}_{(2)} \beta_p \frac{r}{w} \left[ \underbrace{\frac{w^2}{w^2 + w_d^2}}_{(3)} - \underbrace{\frac{w_{pol}^2}{w^2}}_{(4)} - \underbrace{\frac{8q\delta_{EC}}{\pi^2 w} \left( \eta \frac{j_{EC}}{j_{BS}} \right)}_{(5)} \right]$$

Where each term is related to (1) Conventional tearing mode stability, (2) Profile scale lengths, (3) Transport threshold,  $w_d$  (4) Polarization threshold,  $w_{pol}$

- Finally, the term of (5) is our concerned and a function of the **ratio of external current and bootstrap current**. Others are functions of equilibrium quantities.

$$\Gamma_{EC} \propto -K_1 \left( \frac{w}{\delta_{EC}}, \frac{\Delta R}{\delta_{EC}} \right) \frac{j_{EC}}{j_{BS}}$$

where  $\eta$  is current efficiency,  $\eta = \eta_0 (1 + 2\delta_{EC}^2 / w^2)^{-1} \exp[-(5\Delta R / 3\delta_{EC})^2]$

$\delta_{EC}$  : FWHM of Gaussian RF current density profile

$\Delta R$  : offset between center of current drive and center of island

By numerical estimation of  $K_1$  by F.W. Perkins [\*],

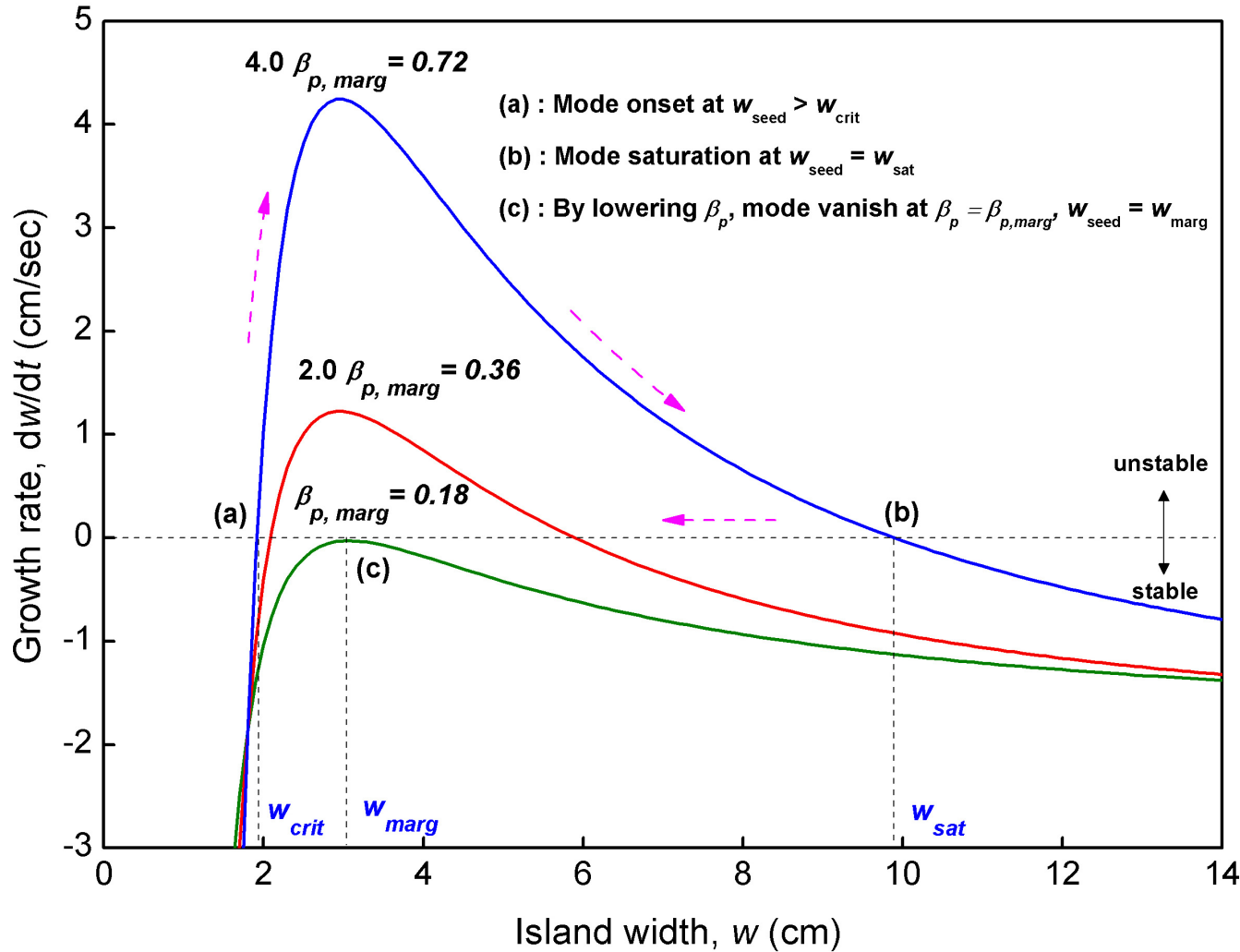
[\*] : F.W. Perkins et al 2000 *Bull. of APS*

$$K_1 \left( \frac{w}{\delta_{EC}}, \frac{\Delta R}{\delta_{EC}} \right) \approx \left( \frac{8q\delta_{EC}}{\pi^2 w} \eta \right) \frac{j_{EC}}{j_{BS}} \quad \text{in case of un-modulated ECCD}$$

$\delta_{EC} = 0.03 \text{ m}$ ,  $\eta_0 = 0.4$  are assumed in ideal alignment case ( $\Delta R = 0$ )

# Marginal Stability Limit of 3/2 NTM in KSTAR DN plasma of reference

scenario :  $\beta_{p, \text{marg}} = 0.18$



$$m/n = 3/2$$

$$\Delta' r_s = -3$$

$$\varepsilon = 0.217$$

$$r_s = 0.39 \text{ m}$$

$$L_q/L_p = 4.46, 4.35, 4.30$$

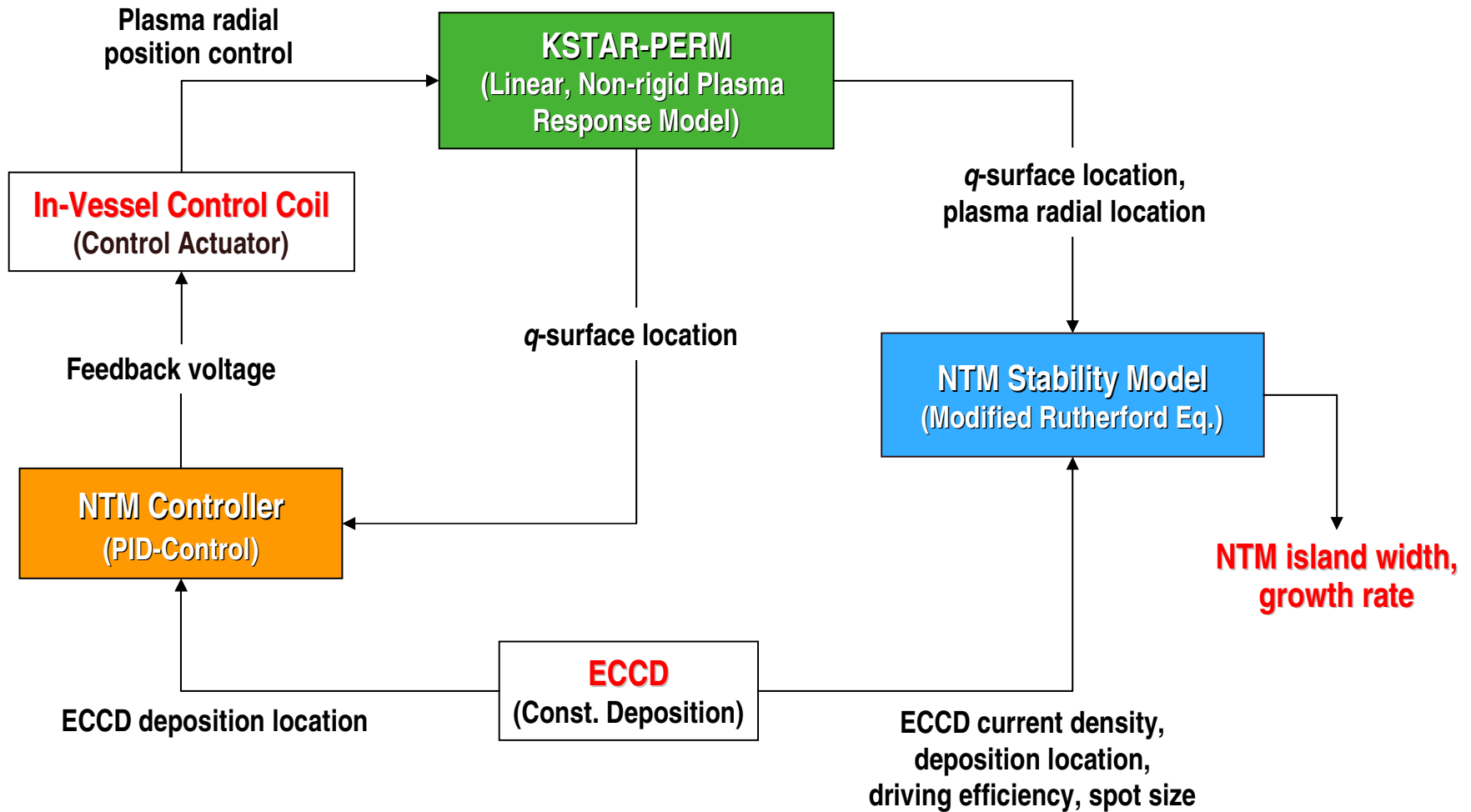
$$w_{\text{pol}} = 1.8 \text{ cm}$$

$$\tau_R = 62 \text{ sec}$$

$\beta_p$  is assumed to be decreased with increasing island size ( $\beta_p$  is ~25% decreased at saturated island)

$L_p$  is assumed to be increased as increasing island size ( $L_p$  is ~80% increased at saturated island because the pressure profile is broaden by increasing island size)

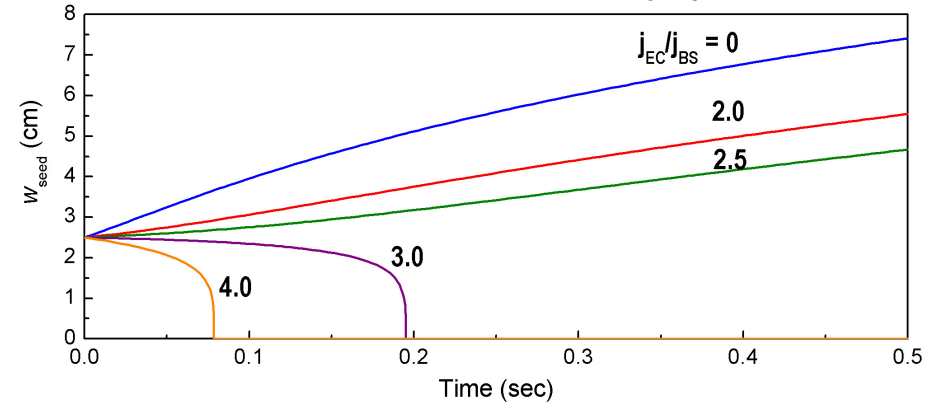
# Diagram of Prototype KSTAR NTM Control Simulator



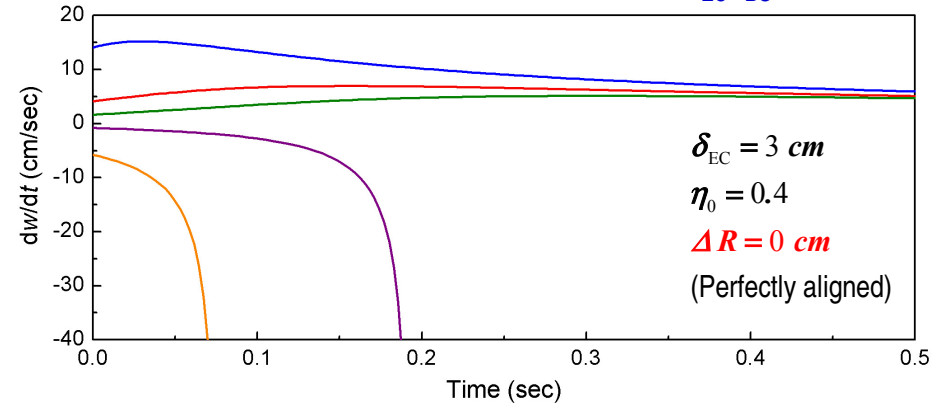
# Calculation results

- Calculation with a prototype control simulator shows that the ratio of ECCD and Bootstrap current  $j_{EC}/j_{BS} \sim 3$  can stabilize the 3/2 NTM at reference KSTAR DN discharge

## • Growths of seed islands under different $j_{EC}/j_{BS}$



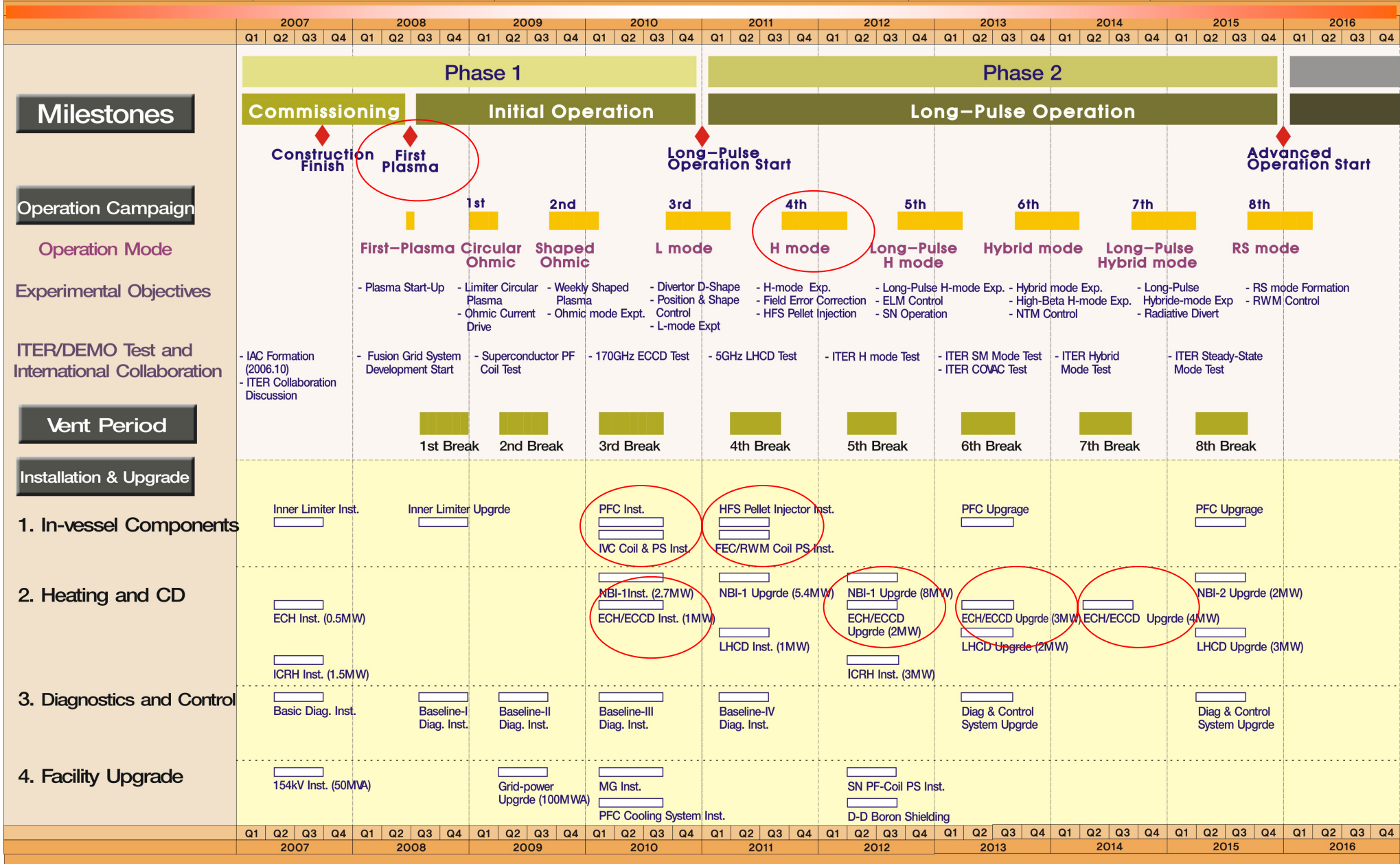
## • Growth rates of seed islands under different $j_{EC}/j_{BS}$



# Issues and future works



# KSTAR OPERATION SCHEDULE [Initial 10years]



# Issues and future works

- Before year of 2010, we should establish/install the control algorithm for IVCC and NTM control since IVCC and Power Supply (PS) for position control and ECCD (baseline) will be installed during year of 2010 and PS for FEC/RWM control will be installed in year of 2011.
- Studies on field error measurement and correction algorithm are underway.
- Suppression of type-I ELM using a sub-coil of IVCC system is under search.
- More calculation, especially bootstrap current, is needed to know required power for NTM control.
- Control of another MHD activity, such as Sawtooth and disruption, will be required.

# Summary

- IVCC are to be implemented in KSTAR, as an actuator to provide the control of vertical & radial position, FEC, and RWM feedback stabilization.
- Physical requirements for plasma position control, FEC, and RWM control are calculated and the results are already adopted in IVCC and PS design value. Applications of IVCC for another MHD activities control are considered.
- A preliminary work for NTM suppression using 170 GHz ECCD is done. More calculation is needed to know required power for NTM control.