

# Resistive Wall Mode Control in DIII-D

by

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for

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Active MHD control in ITER**

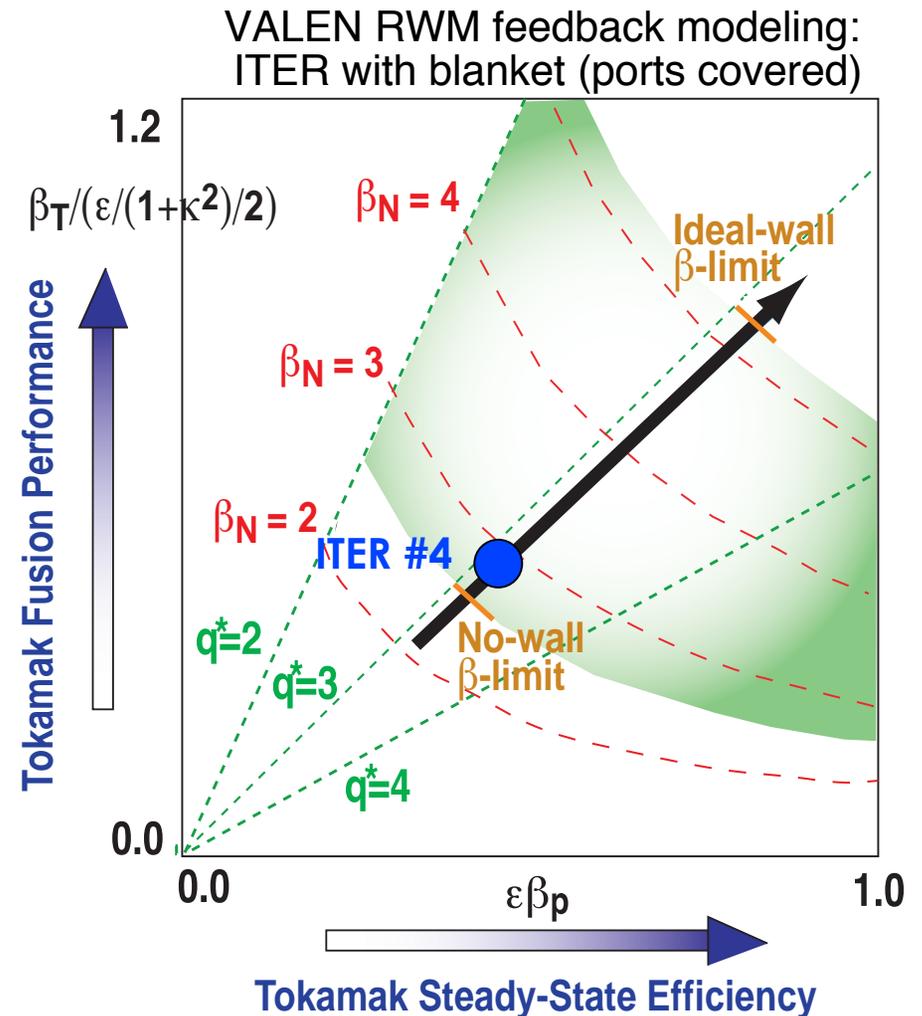
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*Columbia  
University*

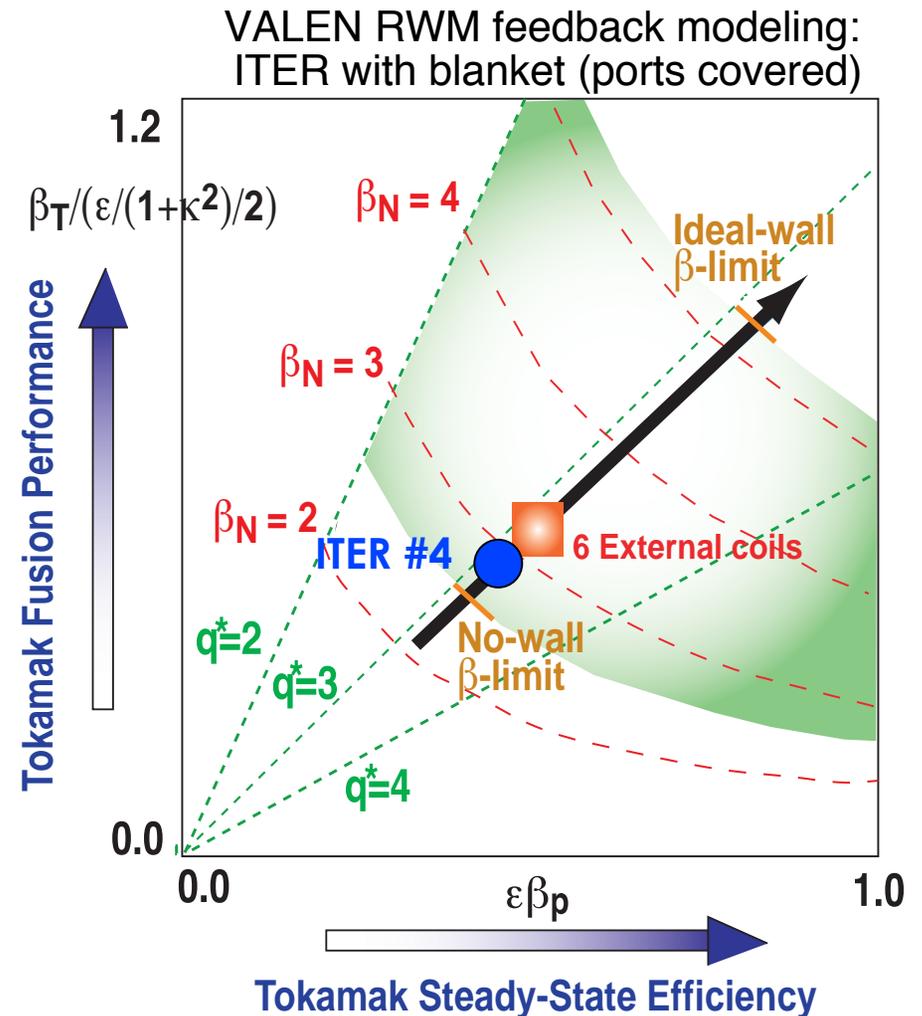
# Resistive Wall Mode Stabilization is Needed for Steady State Tokamak Operation at High Fusion Performance

- ITER Steady-State scenario (#4) requires Resistive Wall Mode stabilization
  - Target:  $\beta_N \sim 3$ , above the no-wall stability limit  $\beta_N^{\text{no-wall}} \sim 2.5$
- Sufficient plasma rotation could stabilize RWM up to ideal-wall  $\beta_N$  limit



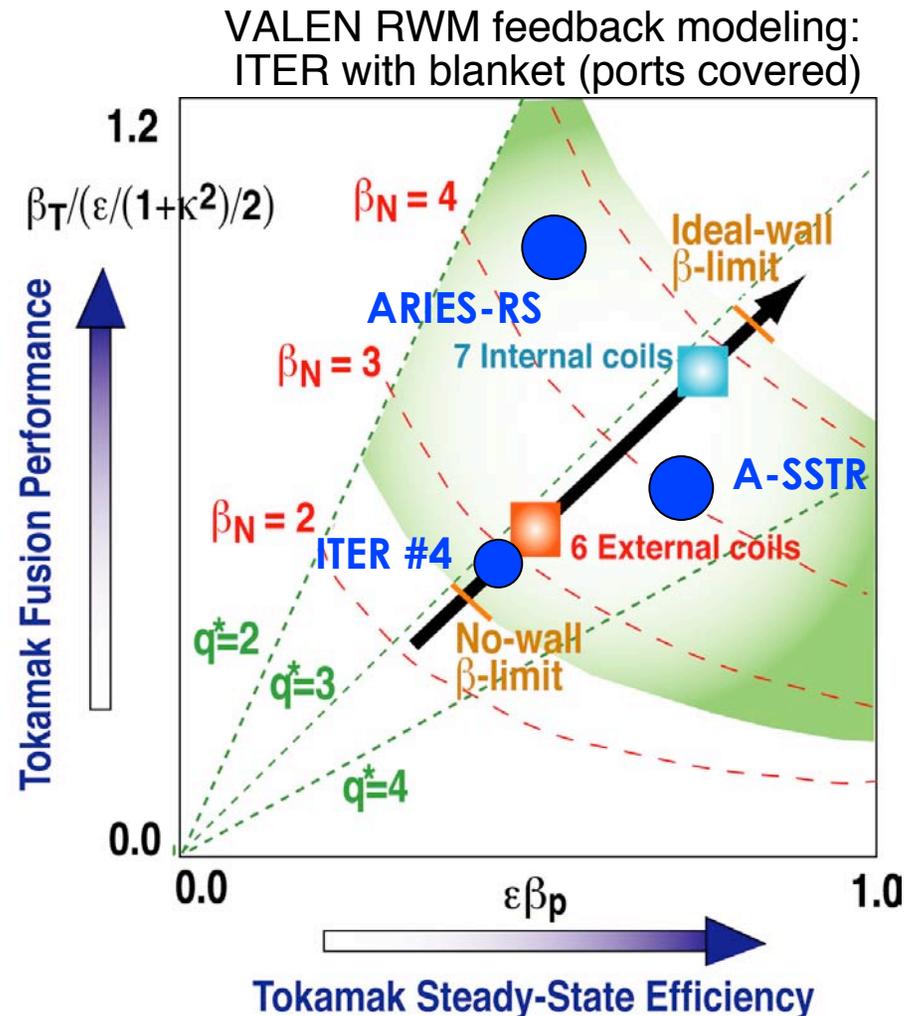
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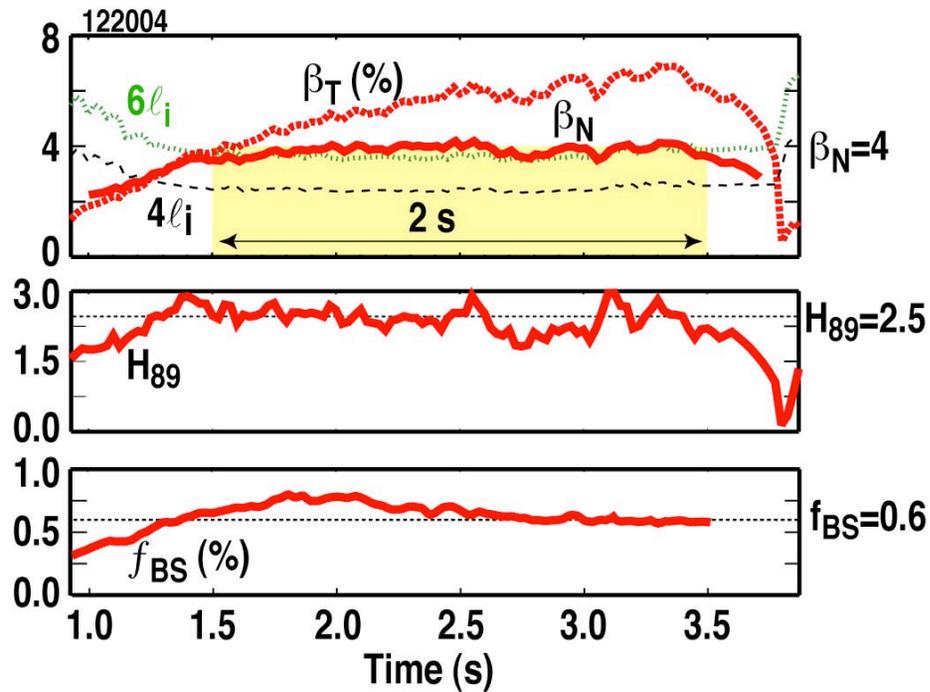


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- **Present ITER design of external error field correction coils is predicted to allow RWM feedback stabilization if plasma rotation is not sufficient**
- **Improved design for RWM stabilization could allow studies of scenarios approaching advanced tokamak reactor concepts, i.e.  $\beta_N > 4$**

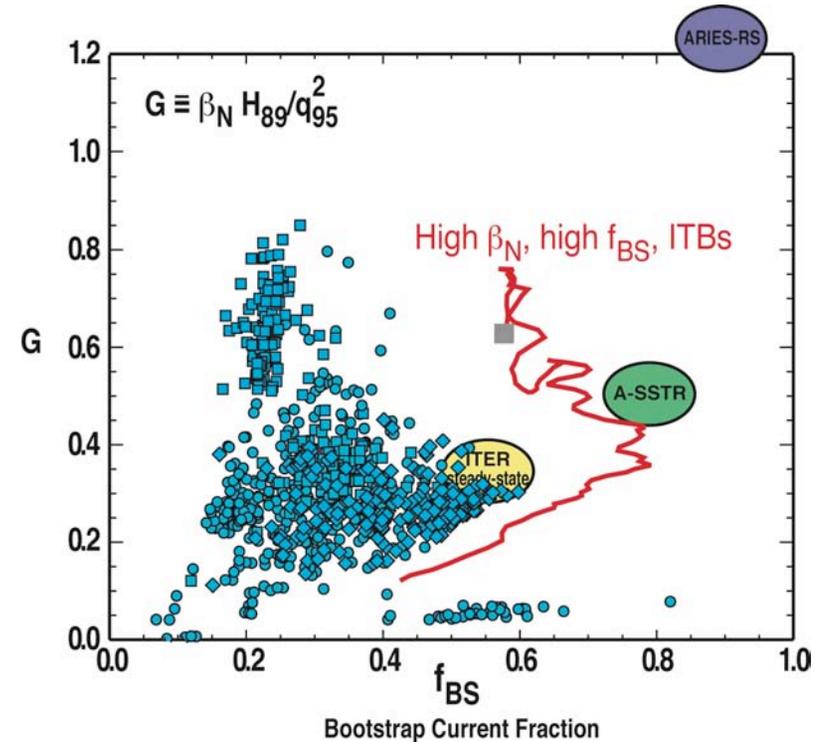
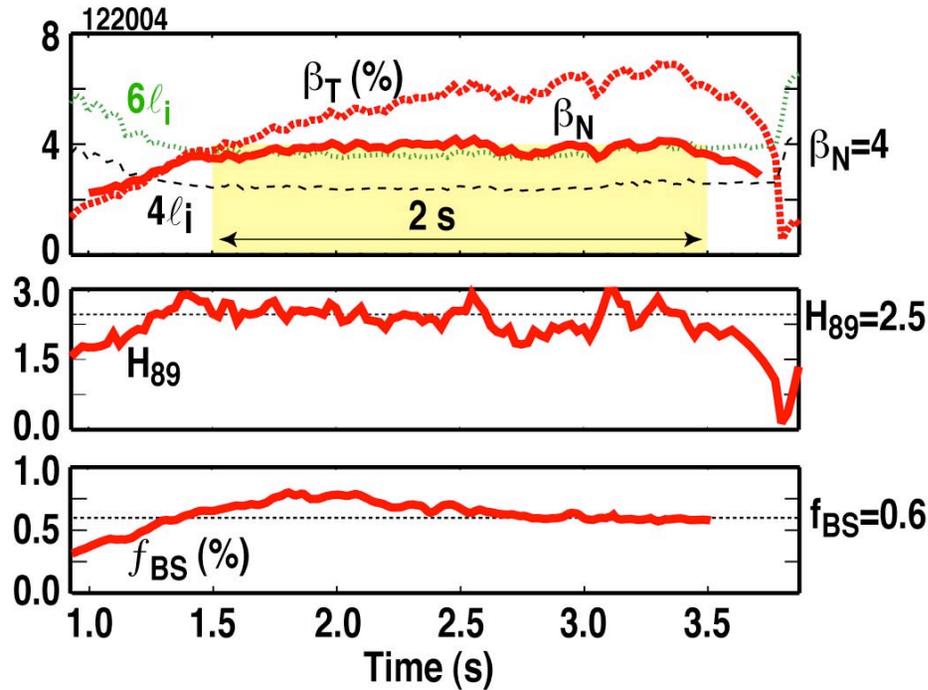


# RWM Stabilization by Rotation Allows Demonstration of High Performance Tokamak Regimes



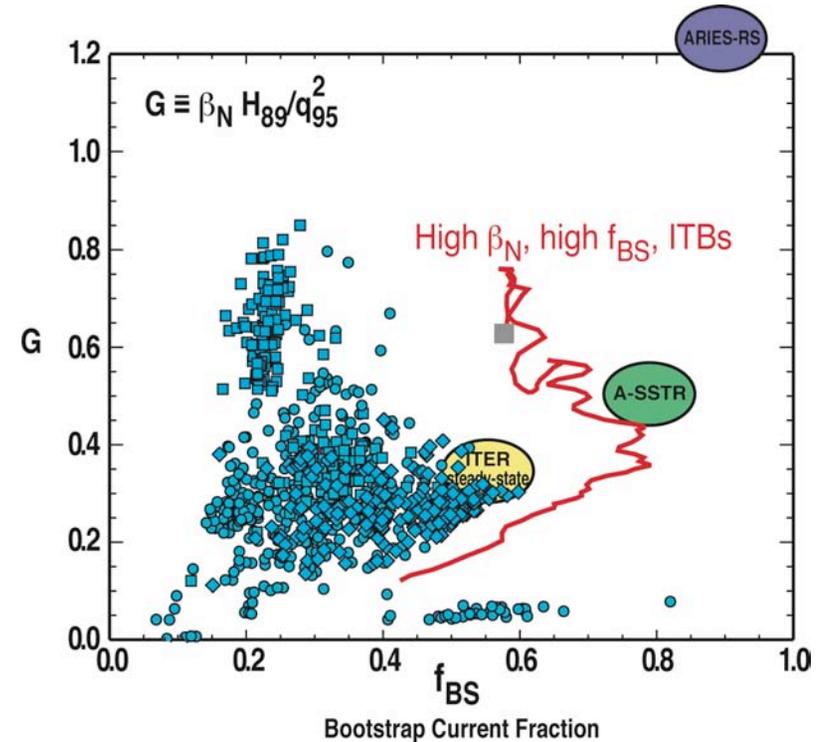
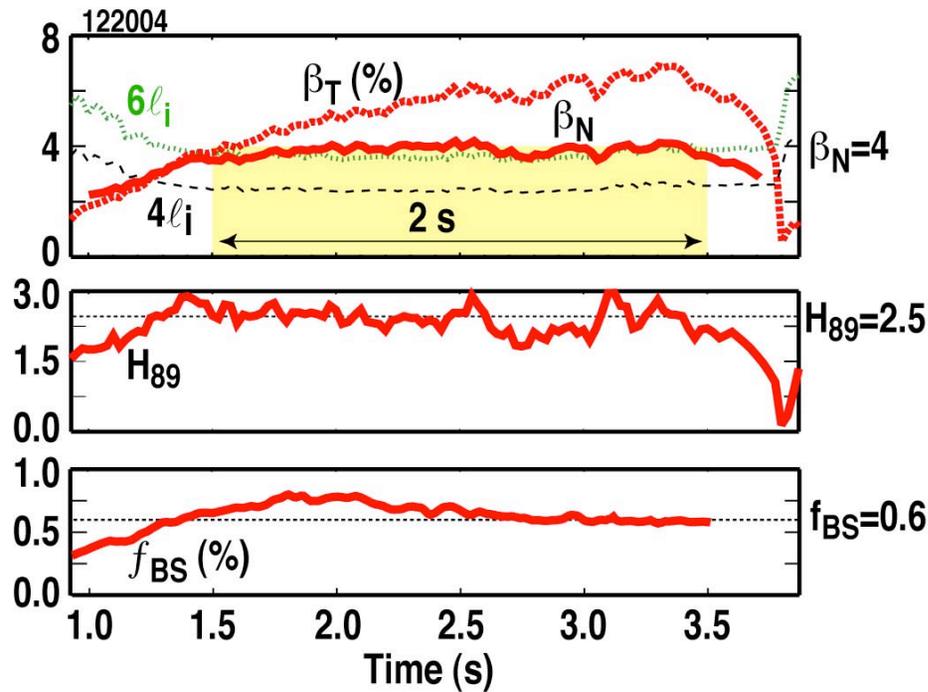
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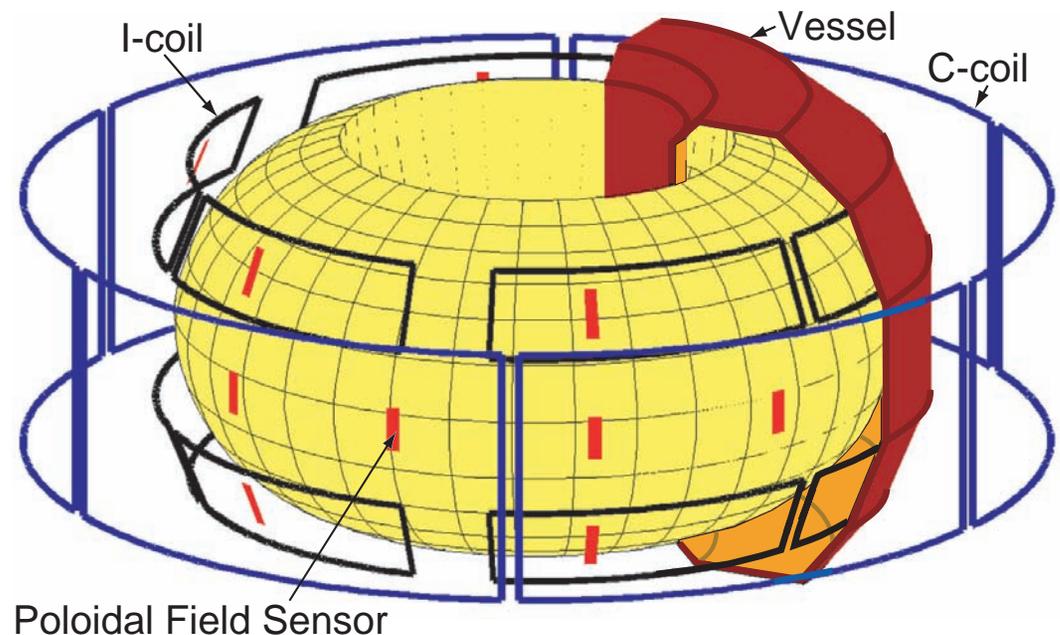
# RWM Stabilization by Rotation Allows Demonstration of High Performance Tokamak Regimes



- High  $\beta$ ,  $\beta_N$ , high bootstrap current fraction, high energy confinement sustained simultaneously for 2 s in DIII-D
- Multiple control tools needed, including
  - Simultaneous ramping of plasma current and toroidal field
  - Simultaneous feedback control of error fields and RWM

# Plasma Rotation Control is Needed to Explore Regime of High Beta and Low Rotation

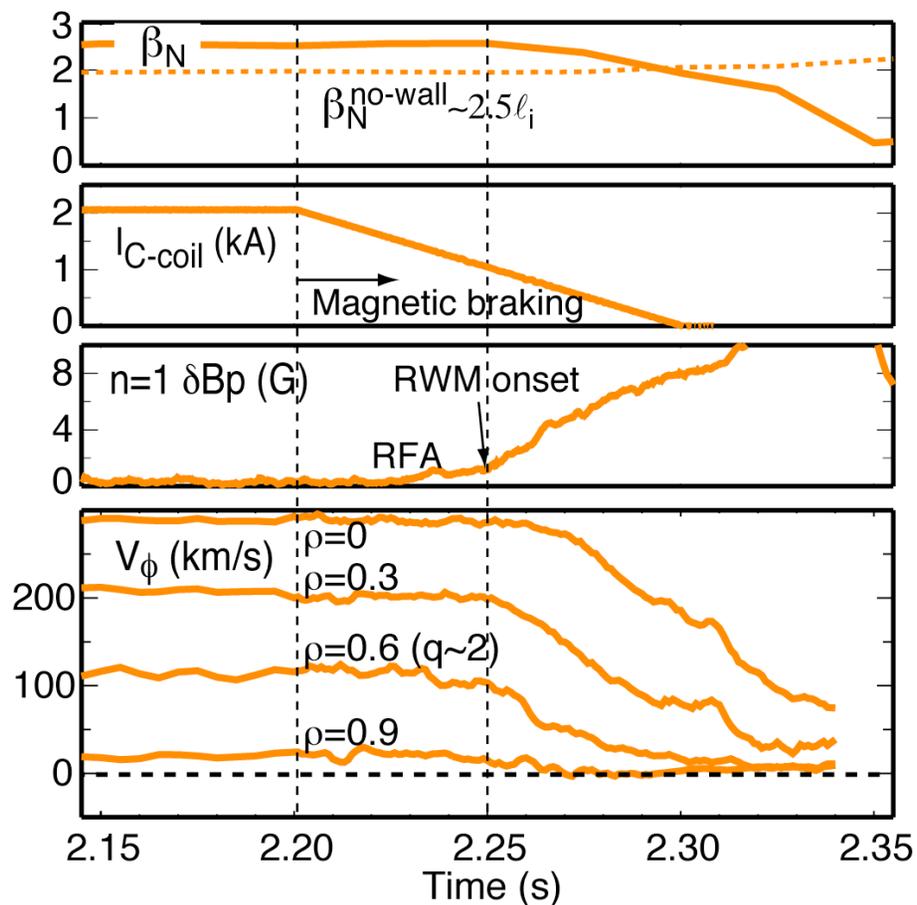
- **Plasma rotation is sufficient to stabilize RWMs in most DIII-D scenarios with all co-injected neutral beams (same direction as  $I_p$ )**
  - Unidirectional NB heating in high beta plasmas applies strong torque
  - Difficult to test RWM feedback control under realistic reactor conditions
- **Resonant and non-resonant magnetic braking to reduce the rotation have disadvantages**
  - Feedback system tends to respond to applied resonant braking field
  - Fine control is difficult: rotation tends to lock
  - Once locked, braking field may excite islands in the plasma



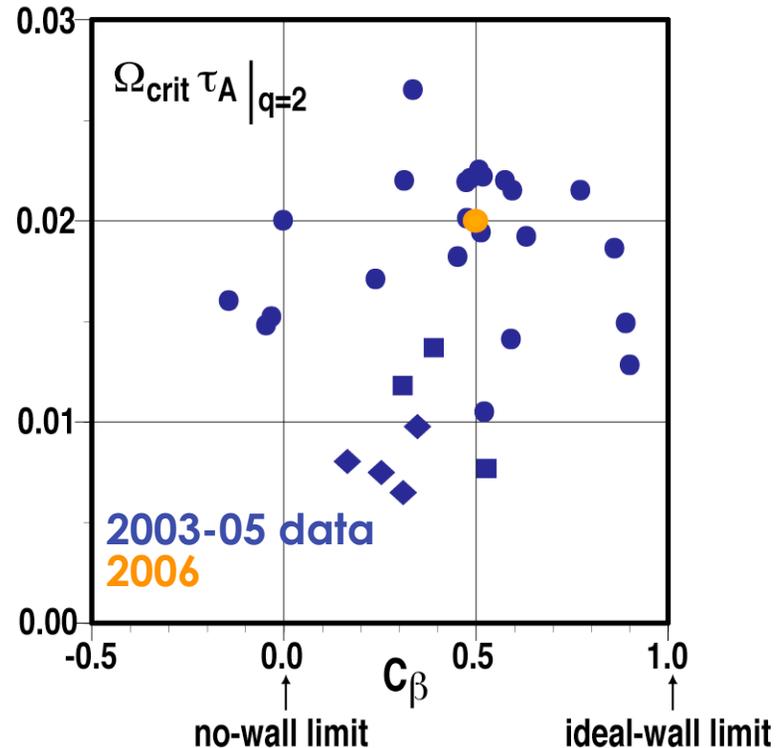
# Magnetic Braking Using $n=1$ External or Intrinsic Fields Yields RWM Rotation Thresholds $\sim O(1\%)$ of $\Omega_A$ ( $q=2$ or $3$ )

- **DIII-D using only uni-directional NBI:**

- Magnetic braking is applied by removing the empirical correction of the intrinsic  $n=1$  error field

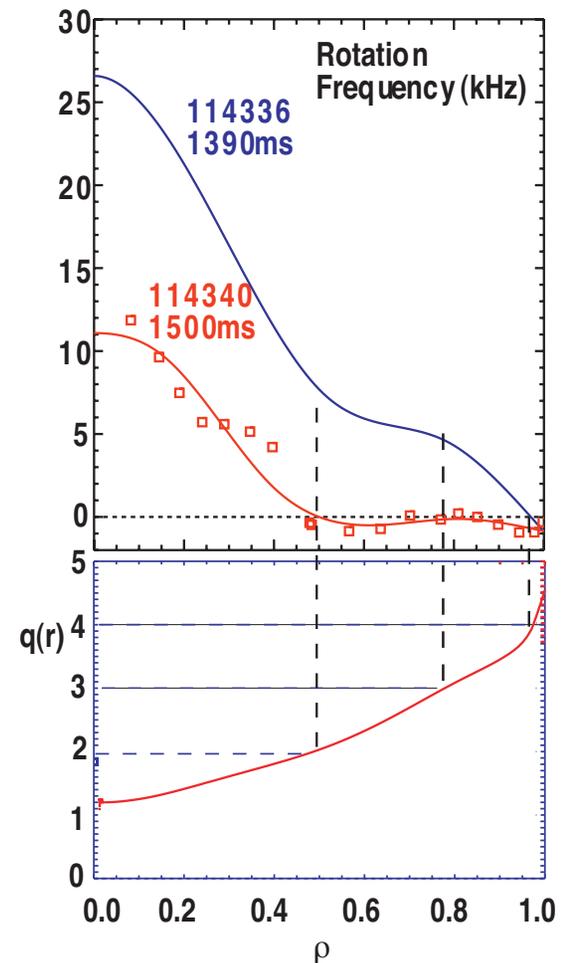
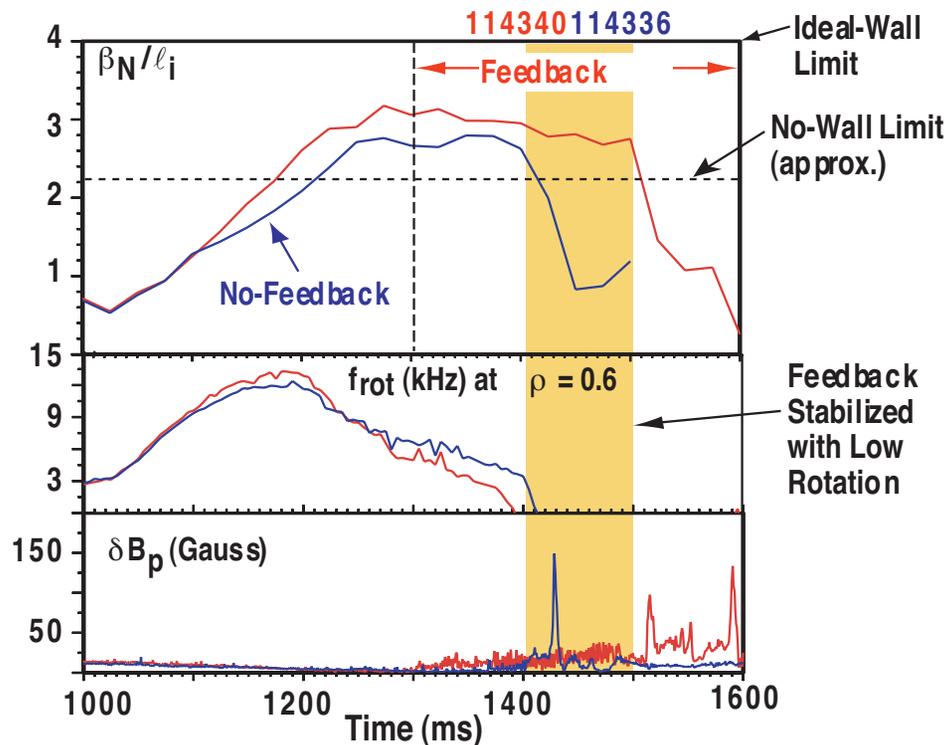


- Critical rotation frequency  $\Omega_{\text{crit}}$  at  $q = 2$  surface ranges from 0.7 to 2.5% of local  $\Omega_A$



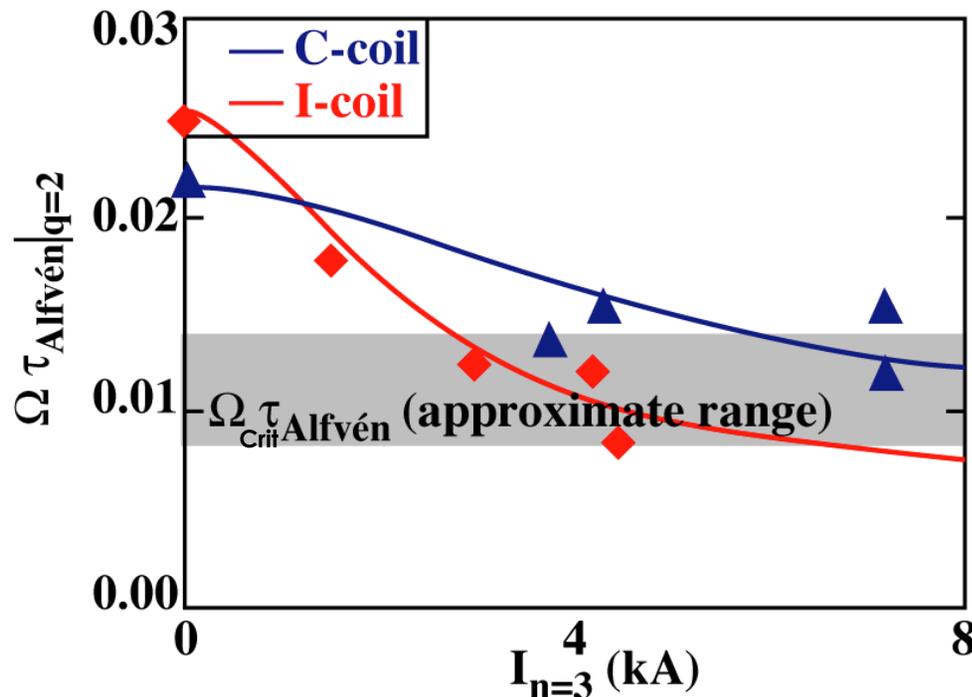
# Resonant Braking Provides Demonstration of Transient Feedback Stabilization at Low Rotation

- I-coil feedback sustains beta (for  $\sim 30\tau_w$ ) in discharge with near-zero rotation at all  $n=1$  rational surfaces
- Comparison case without feedback is unstable even with lower beta and faster rotation



# Non-Resonant n=3 Braking Did Not Give Access to the Low-rotation Regime

- n=3 magnetic braking can create large drag torque
- RWM remains stable when correction of n=1 error field is optimal (DEFC)



- Braking effect saturates as braking field is increased
- Saturated rotation agrees with neoclassical toroidal viscosity model

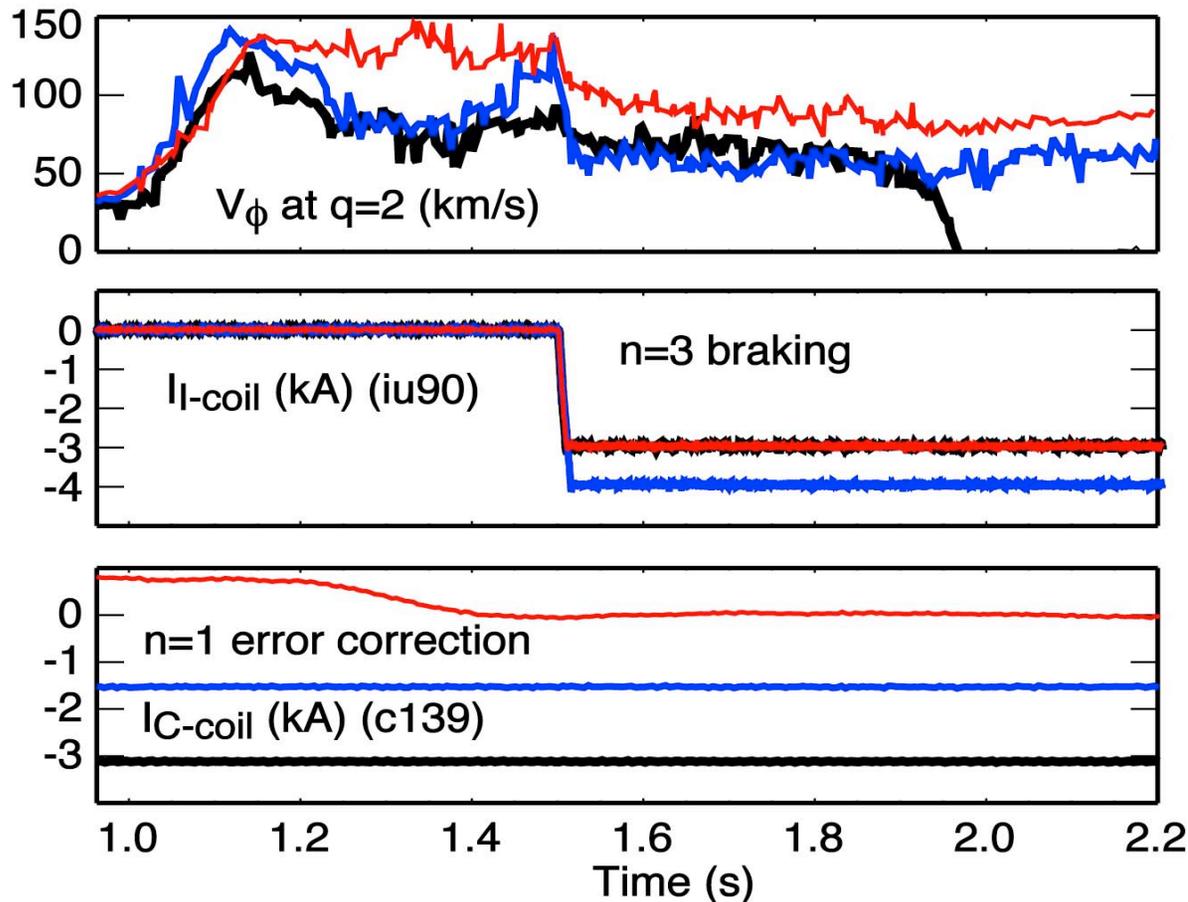
$$\Omega_D \sim 2/3 \nabla T_i / (Z_i e B_\theta R)$$

- K.C. Shaing, S.P. Hirshman and J.D. Callen, Phys. Fluids **29**, 521 (1986)

$$dL/dt = T_{NB} - L/\tau_M - k(\Omega - \Omega_D) I_{n=3}^2$$

# Non-Resonant $n=3$ Braking Can Give Access to Unstable RWM, If $n=1$ Error Correction Is Non-optimal

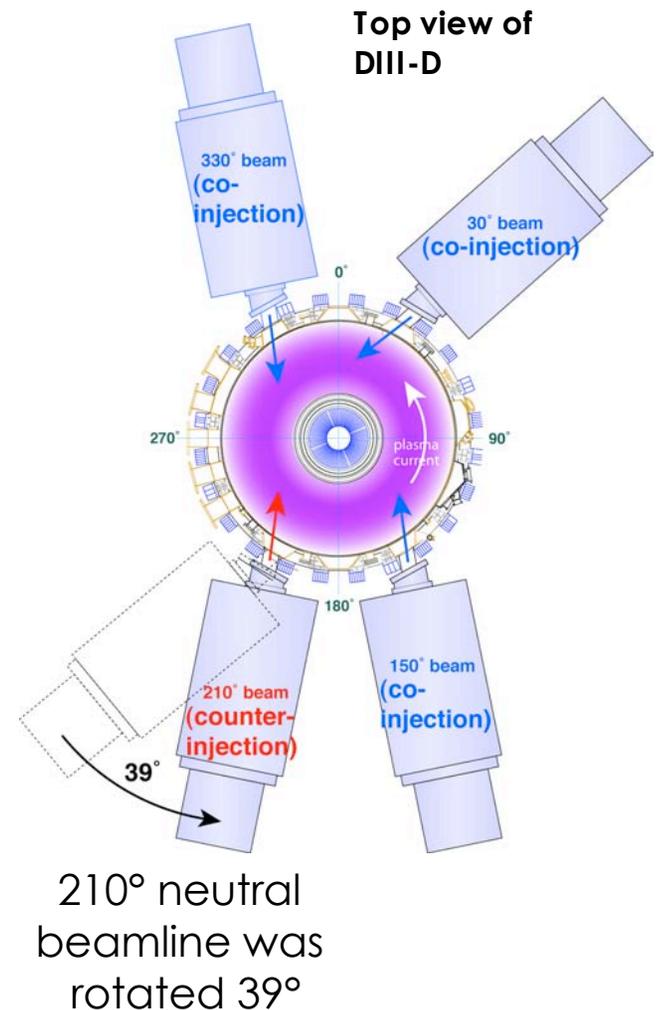
- C-coil used for  $n=1$  error field correction (red=optimal)
- I-coil used for  $n=3$  magnetic braking



- Small  $n=1$  error field introduced accidentally (one C-coil pair)
- RWM onset observed for sufficiently large  $n=3$  and  $n=1$  error field

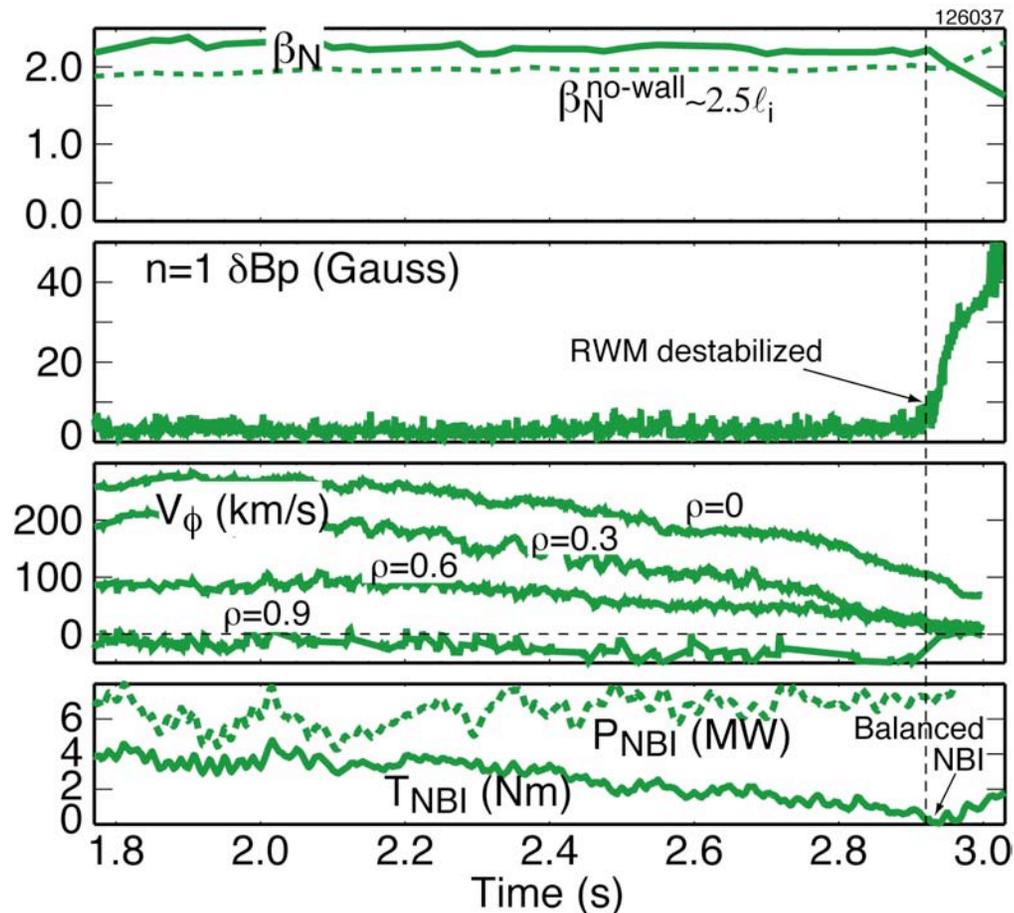
# Balanced injection provides effective rotation control without magnetic perturbations

- **Magnetic braking experiments suggested that RWM stabilization requires mid-radius plasma rotation  $\sim O(1\%)$  of the Alfvén frequency,  $\Omega_A$** 
  - This level of rotation may not be realized in ITER
- **Recent experiments using balanced NBI in DIII-D (and JT-60U) show that the plasma rotation needed for RWM stabilization is much slower than previously thought**
  - $\sim O(0.1\%)$  of  $\Omega_A$
  - Such a low rotation should be achievable in ITER
- **Even with sufficient rotation, active feedback may still be needed, but the system requirements could be reduced**

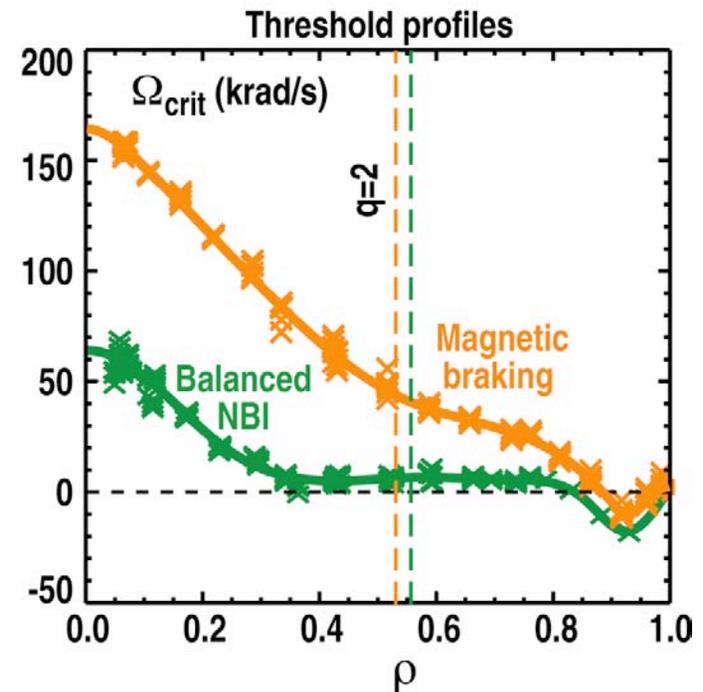


# Much Slower Rotation Before RWM Onset is Observed by Reducing the Injected Torque With Minimized Error Fields

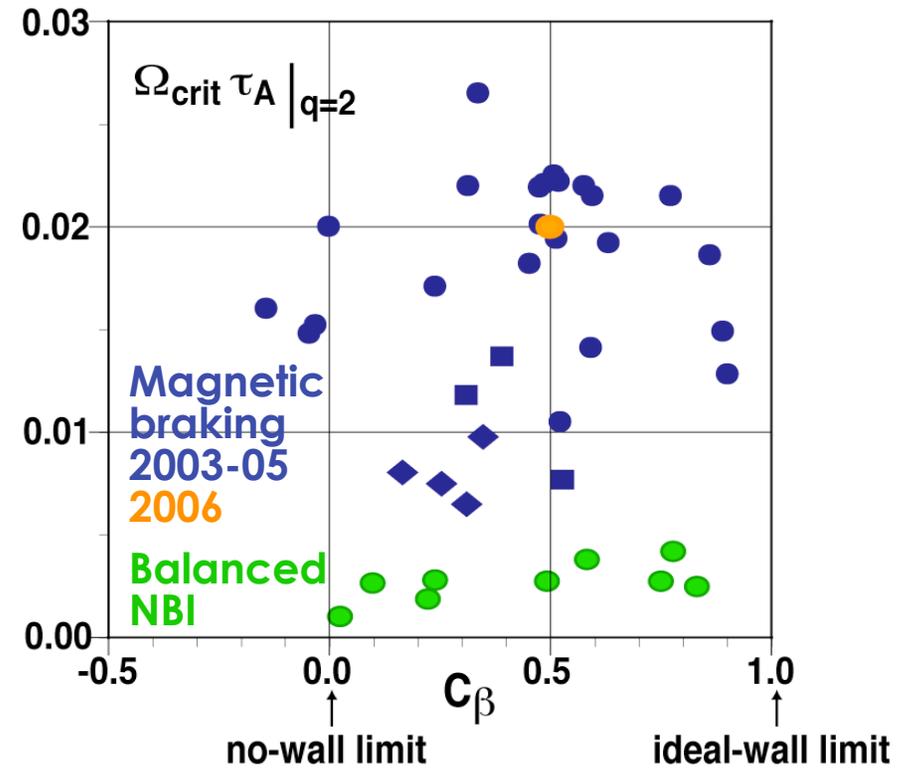
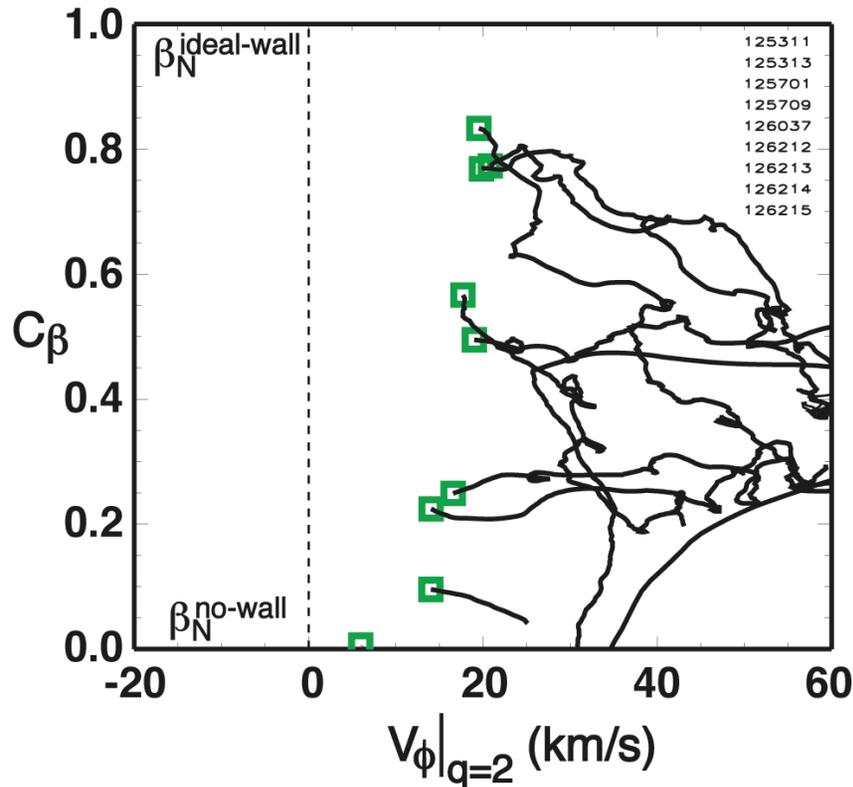
- DIII-D using a varying mix of co and counter NBI:



- Plasma rotation is reduced uniformly for  $\rho < 0.9$
- $\Omega_{\text{crit}}$  at  $q = 2$  is  $\sim 7x$  slower than measured with magnetic braking



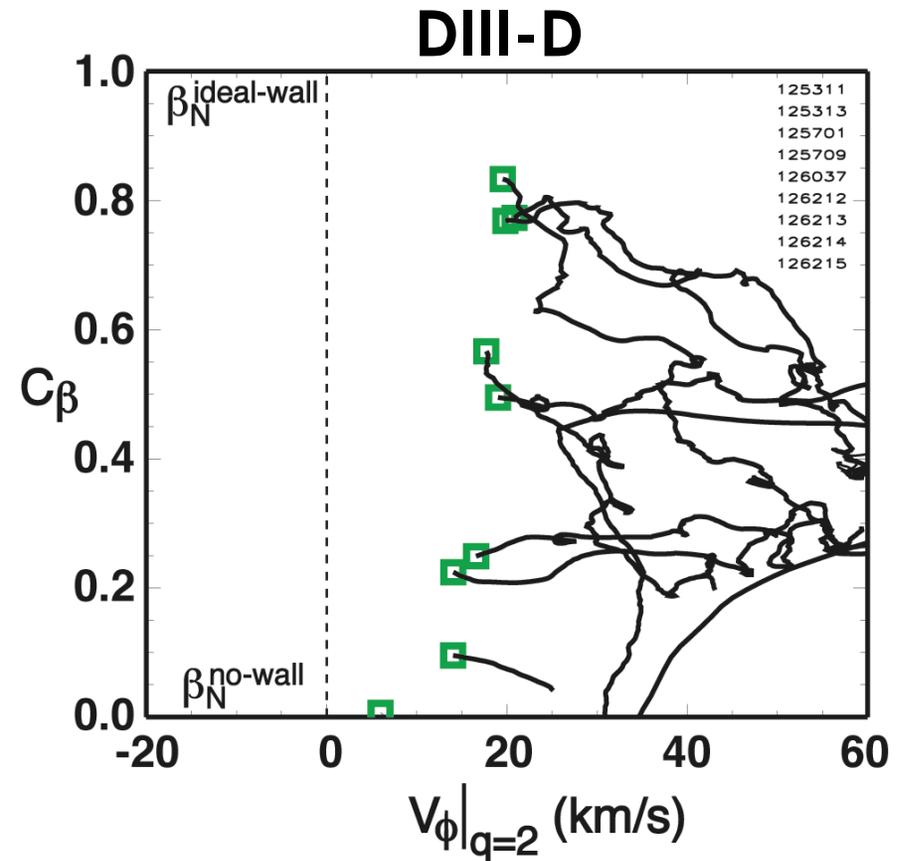
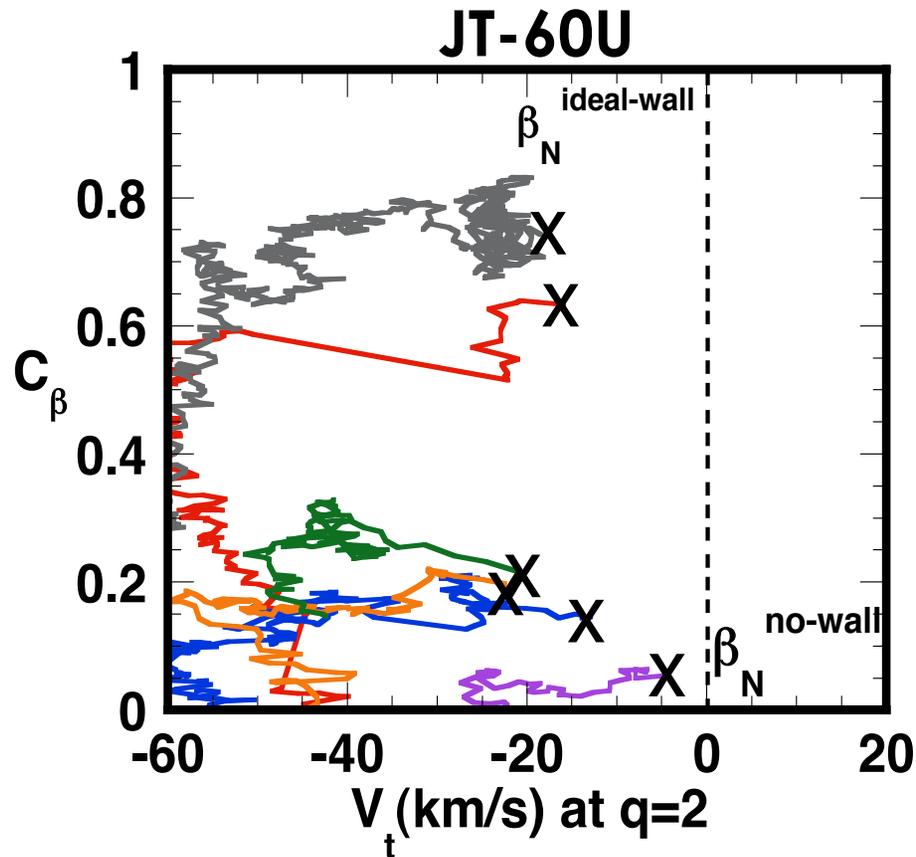
# Weak $\beta$ -Dependence is Observed for Rotation Thresholds Measured With Minimized Error Fields



- RWM onset ( $\square$ ) observed when  $V_\phi$  at  $q=2$  is  $\sim 10$ - $20$  km/s, or  $\sim 0.3\%$  of local  $V_A$

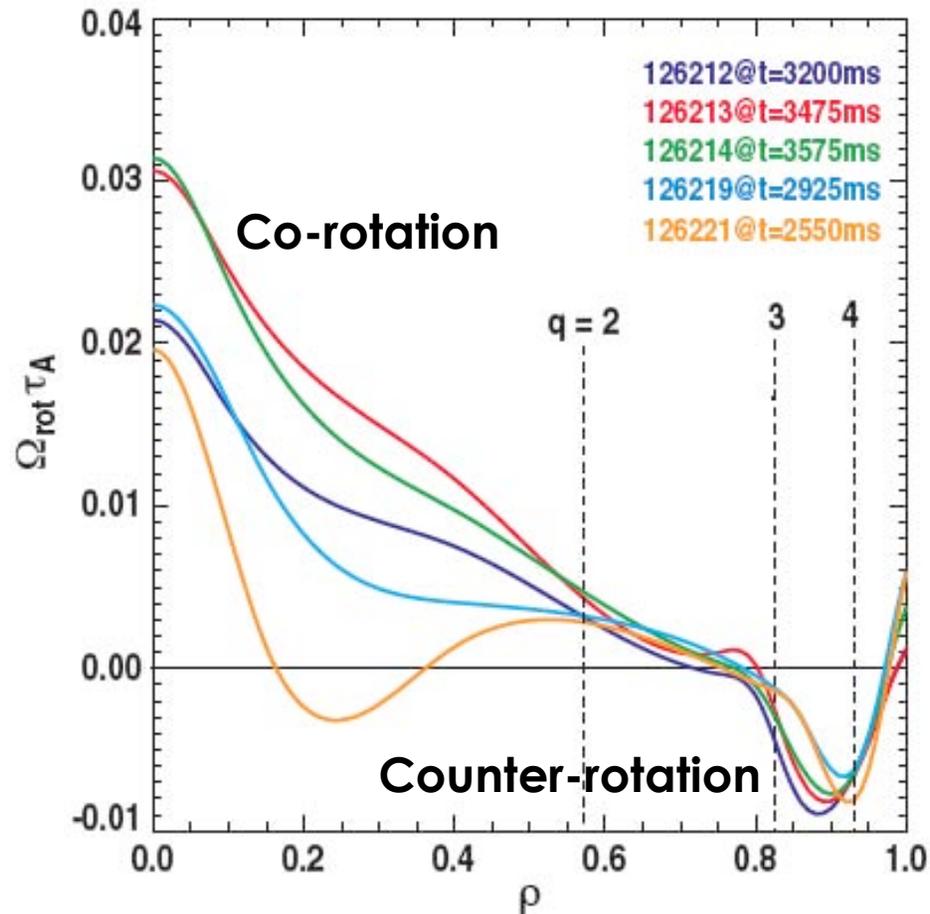
# Independent, Simultaneous Discovery of Low RWM Rotation Thresholds in DIII-D and JT-60U

[Takechi, IAEA FEC 2006]

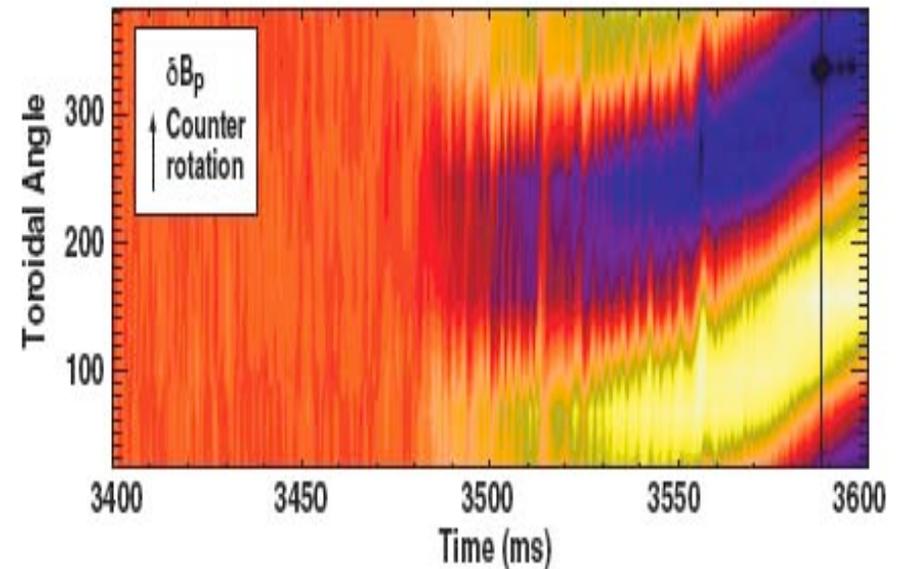


# Profiles at RWM Onset Suggest Rotation in the Outer Region of the Plasma Is Important

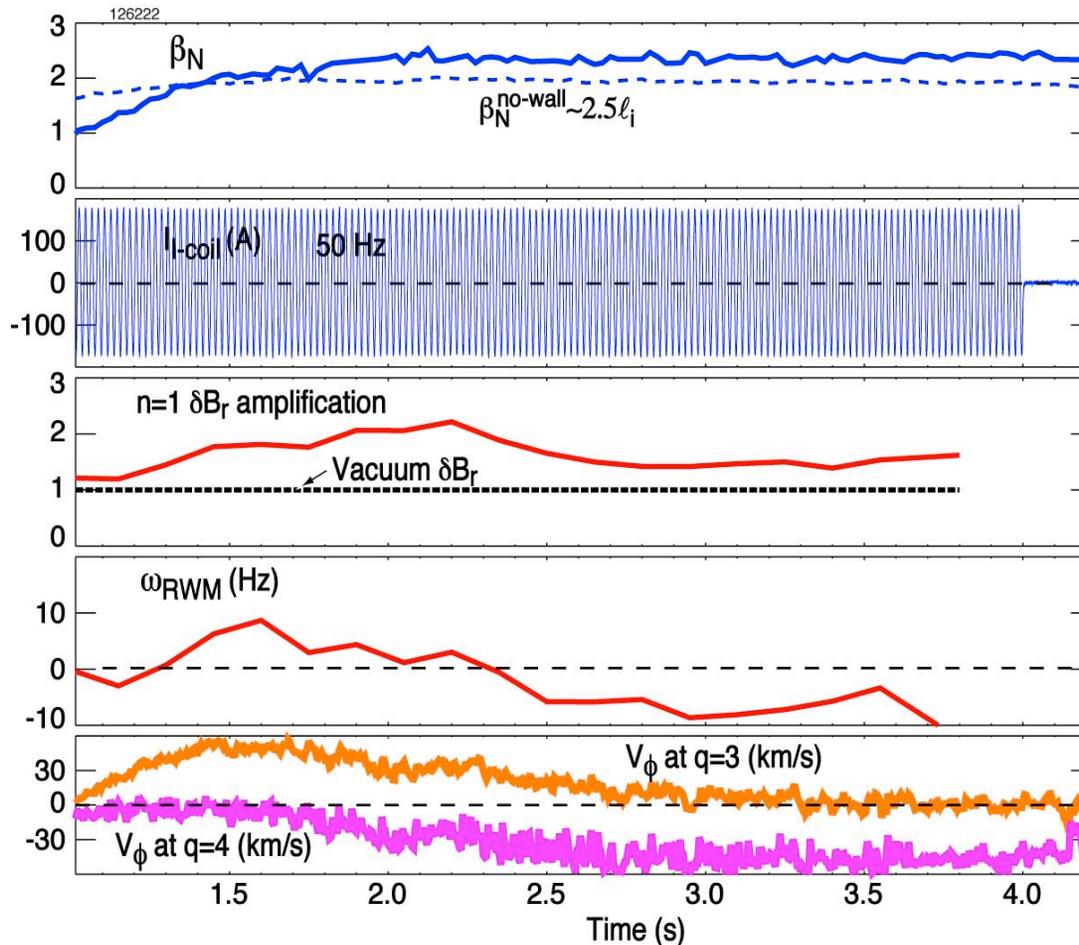
- Central rotation seems uncorrelated with RWM onset



- Negative mode rotation at onset suggests strong interaction near plasma edge



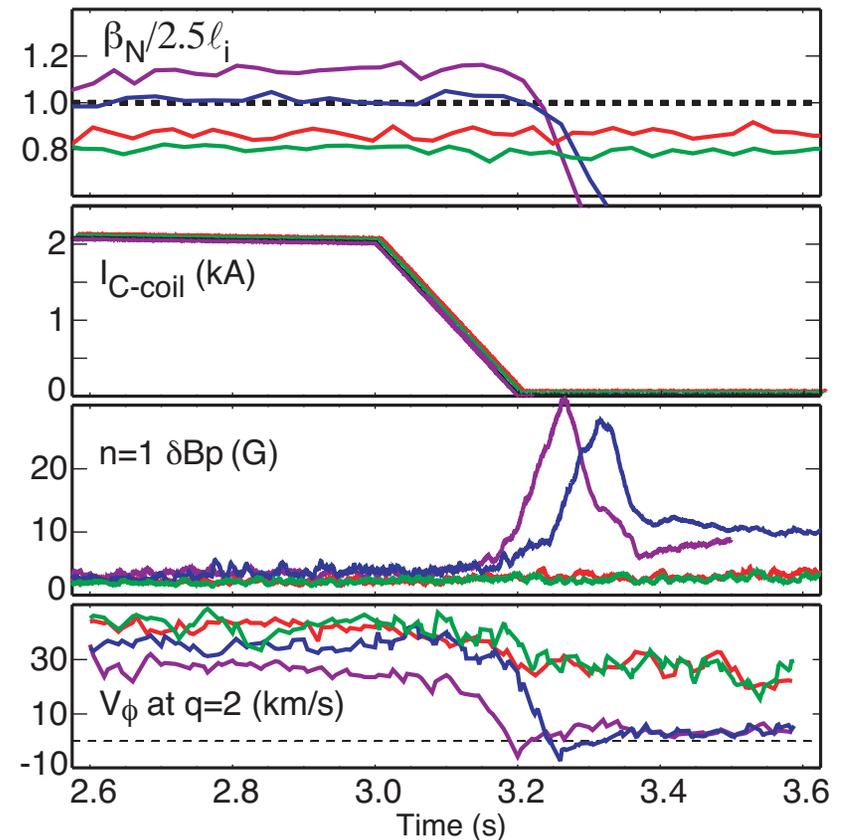
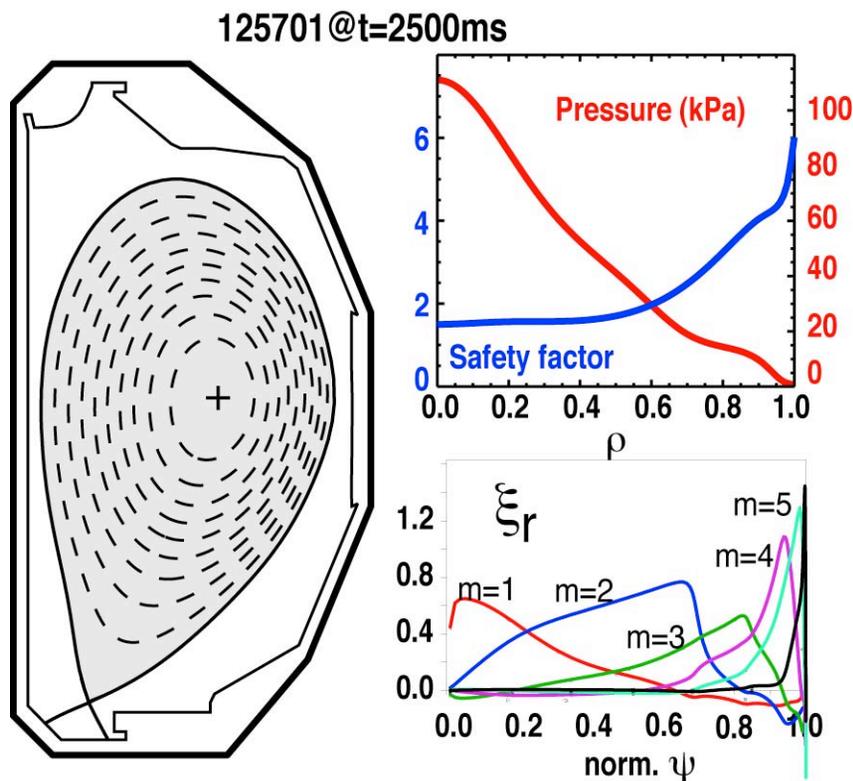
# MHD Spectroscopic Measurements With Varying Plasma Rotation Shows Importance of Edge Rotation



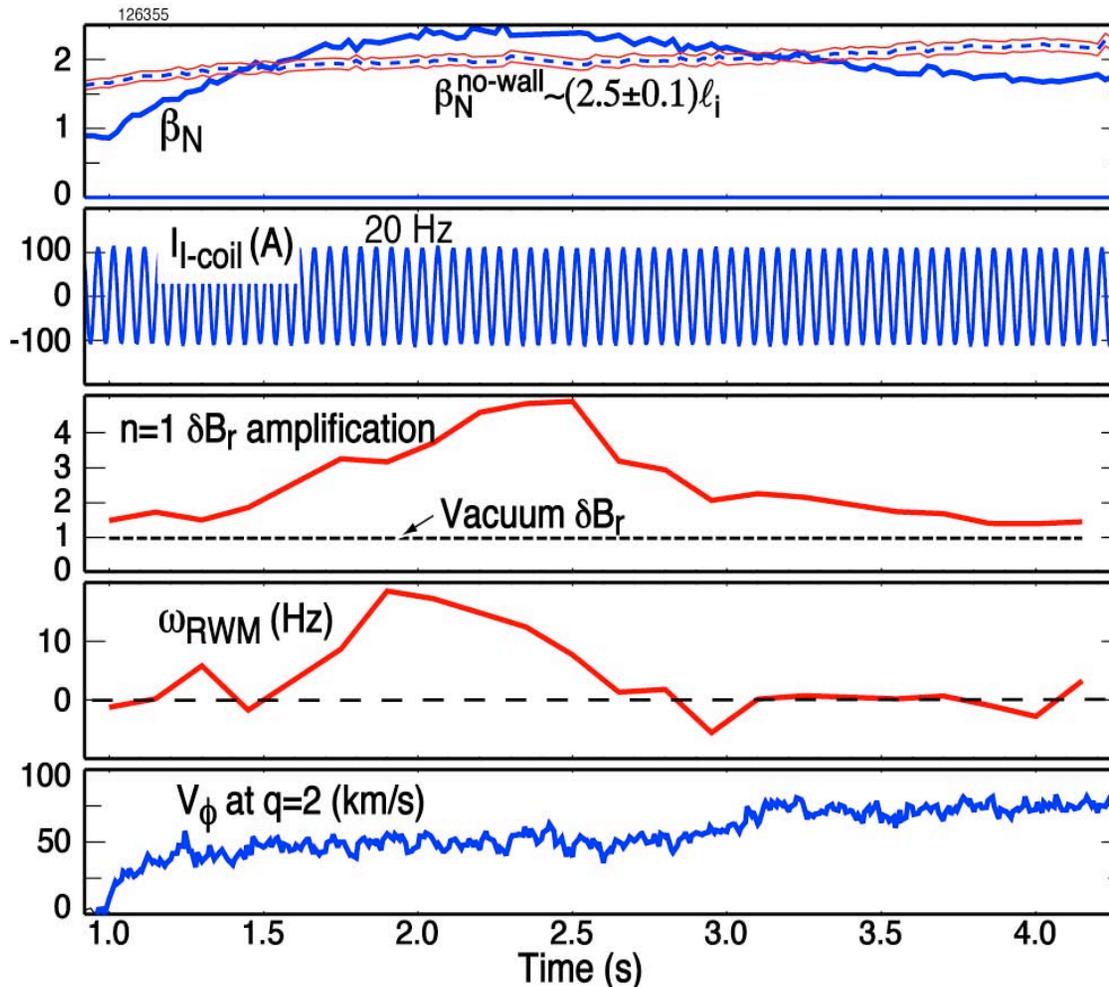
- Natural rotation frequency of stable RWM,  $\omega_{\text{RWM}}$ , obtained from measurements of plasma response at single frequency
- Plasma rotation varied with nearly constant  $\beta_N$
- $\omega_{\text{RWM}}$  crosses zero when rotation between  $q=3$  and  $q=4$  crosses zero

# Sensitivity to Error Fields Confirms $\beta_N$ Is Above No-Wall Limit

- Ideal MHD stability calculations (DCON code and GATO code) predict  $\beta_N^{\text{no-wall}} \approx (2.5 \pm 0.1)l_i$
- Sensitivity to field asymmetries brackets  $\beta_N^{\text{no-wall}}$  between  $2.3l_i$  and  $2.5l_i$ , consistent with stability calculations



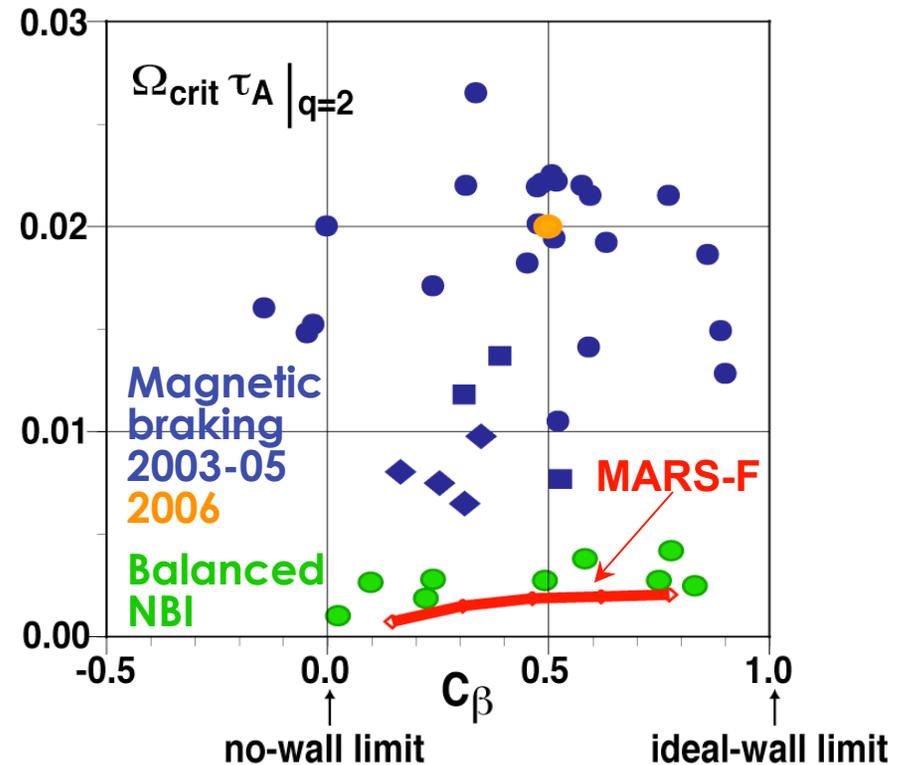
# MHD Spectroscopic Measurements With Varying $\beta_N$ Explain Sharp Threshold of Sensitivity to Error Fields



- Natural rotation frequency of stable RWM,  $\omega_{RWM}$ , obtained from measurements of plasma response at single frequency
  - $\beta_N$  varied with nearly constant high plasma rotation
- $\omega_{RWM} \sim 0$  when  $\beta_N \leq \beta_N^{\text{no-wall}}$
- No momentum exchange between mode and static non-axisymmetric field when natural rotation frequency of RWM is zero

# Ideal MHD With Kinetic Damping Model of Dissipation Is Consistent With New Low Threshold Rotation

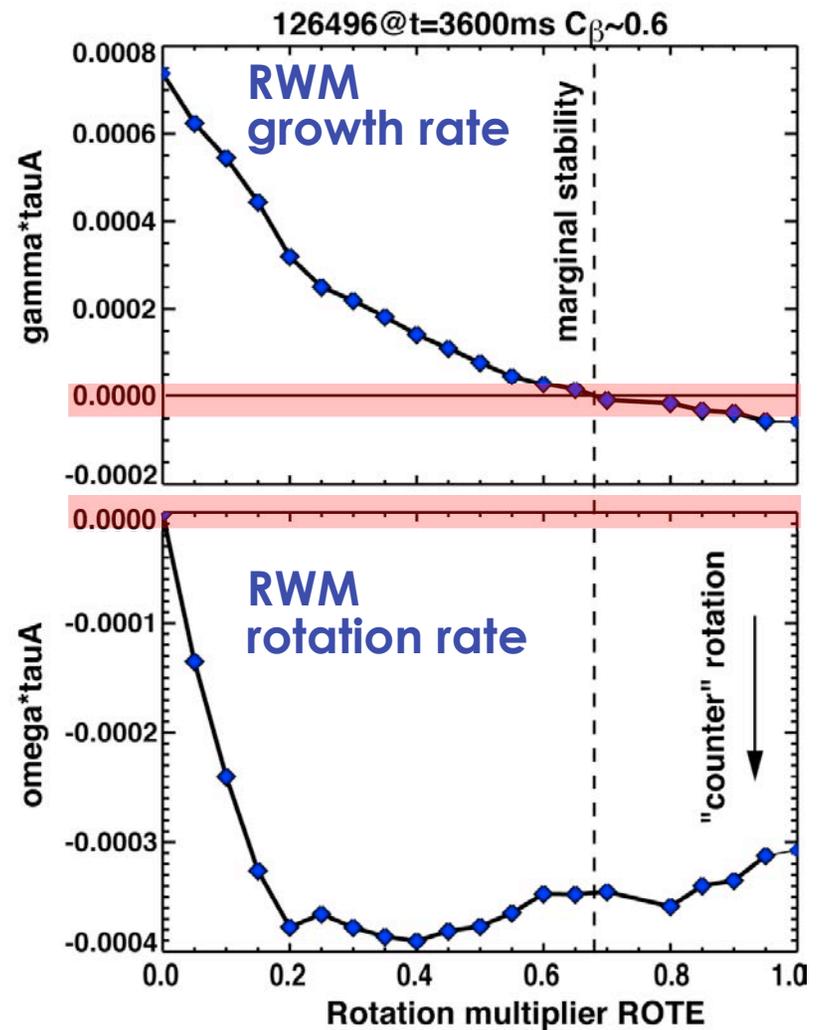
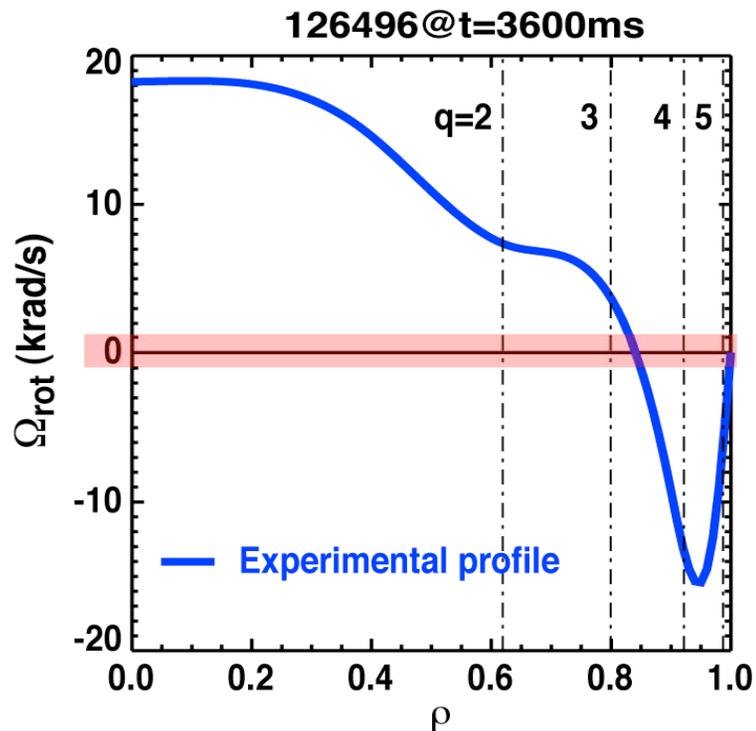
- Marginal stability predicted with 70% of experimental rotation profile for balanced NBI plasmas
  - Kinetic damping model [Bondeson and Chu] implemented in MARS-F



- Sound wave damping model needs at least 300% of experimental rotation profile for marginal stability

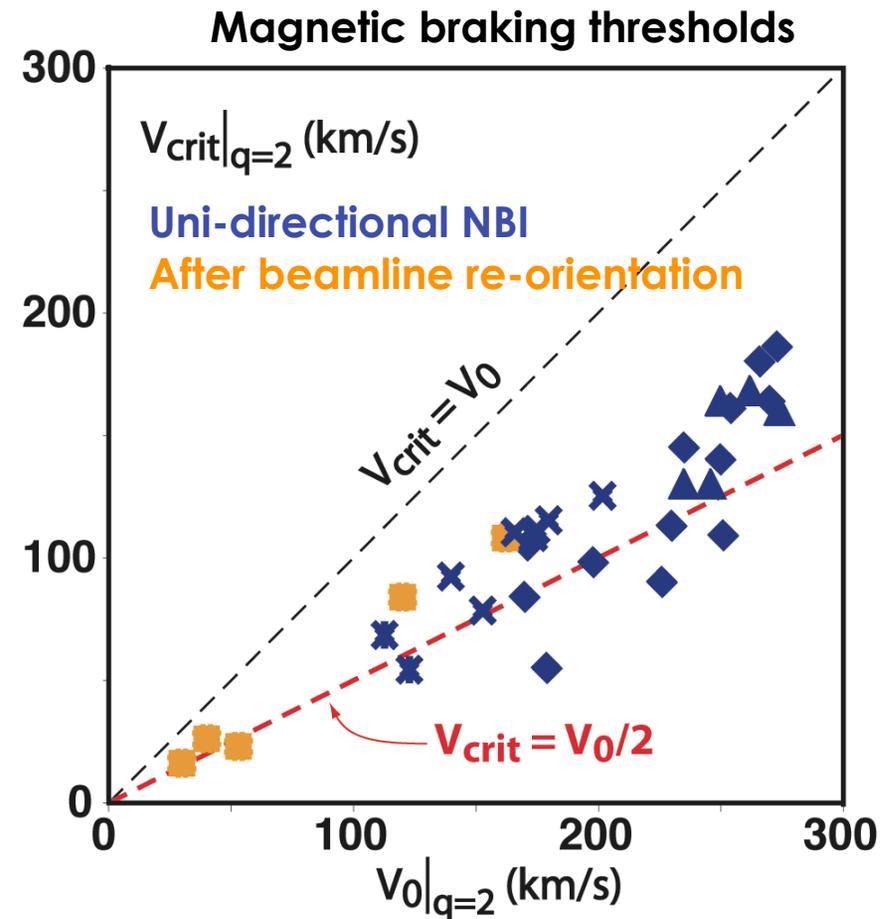
# MARS-F With Kinetic Damping Model Suggests Importance of Plasma Rotation Near the Edge

- **Experimental rotation profile is scaled to find marginal stability**
  - RWM growth rate  $\gamma_{RWM}$  and mode rotation frequency  $\omega_{RWM}$  are normalized to growth rate without rotation
- **RWM rotates in direction of plasma edge**



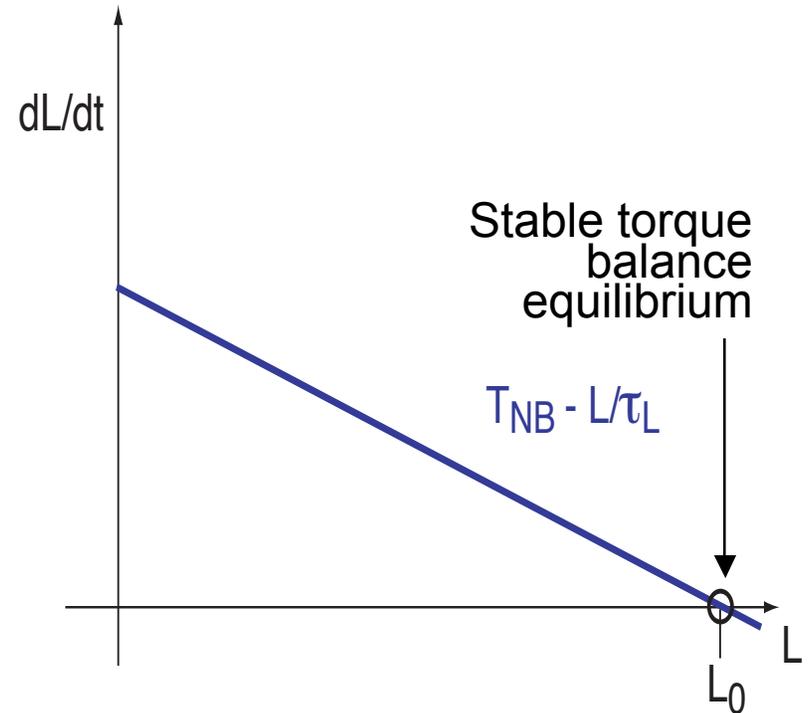
# High Rotation Threshold Measured With Magnetic Braking Is Consistent With Torque-balance Equilibrium Bifurcation

- Increasing static resonant error field ( $n=m/q$ ) leads to bifurcation in torque-balance equilibrium of plasma
  - Rotation must jump from a high value to essentially locked
- “Induction motor” model of error field-driven reconnection [Fitzpatrick]:
  - Plasma rotation at critical point,  $V_{\text{crit}} \sim 1/2$  of unperturbed rotation,  $V_0$
- Lower neutral beam torque gives lower  $V_0$ , therefore a lower  $V_{\text{crit}}$  at entrance to “forbidden band of rotation”



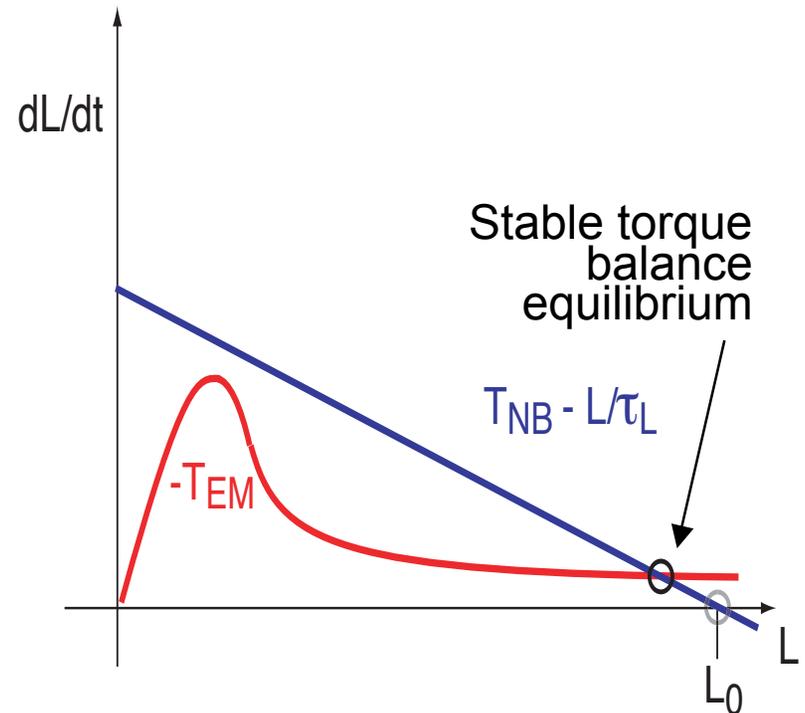
# "Forbidden Band" of Rotation Results in a Higher Effective Rotation Threshold for RWM Onset

- With no error field, torque balance requires NB torque = viscous torque



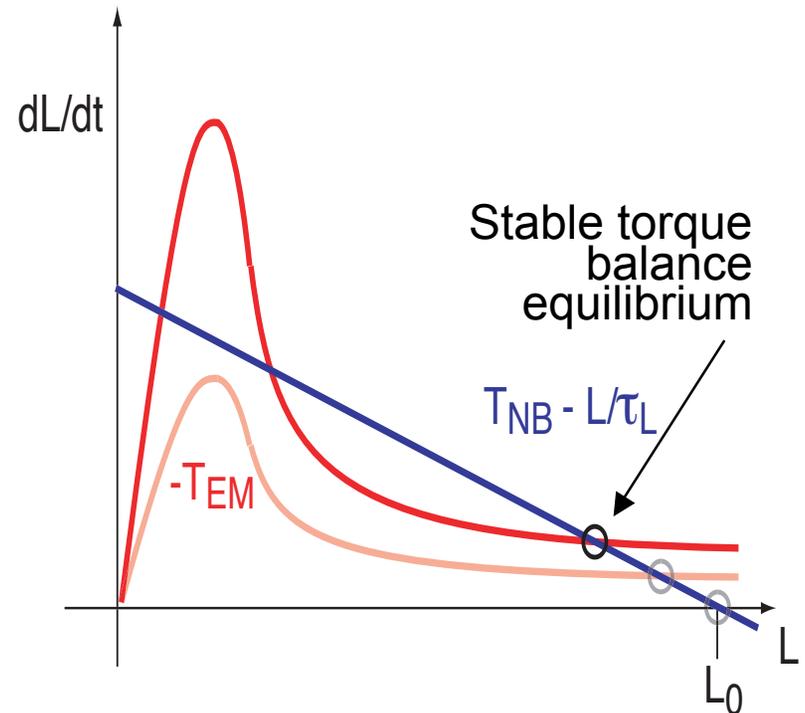
# "Forbidden Band" of Rotation Results in a Higher Effective Rotation Threshold for RWM Onset

- With uncorrected error field, resonant field amplification by stable RWM leads to large electromagnetic torque



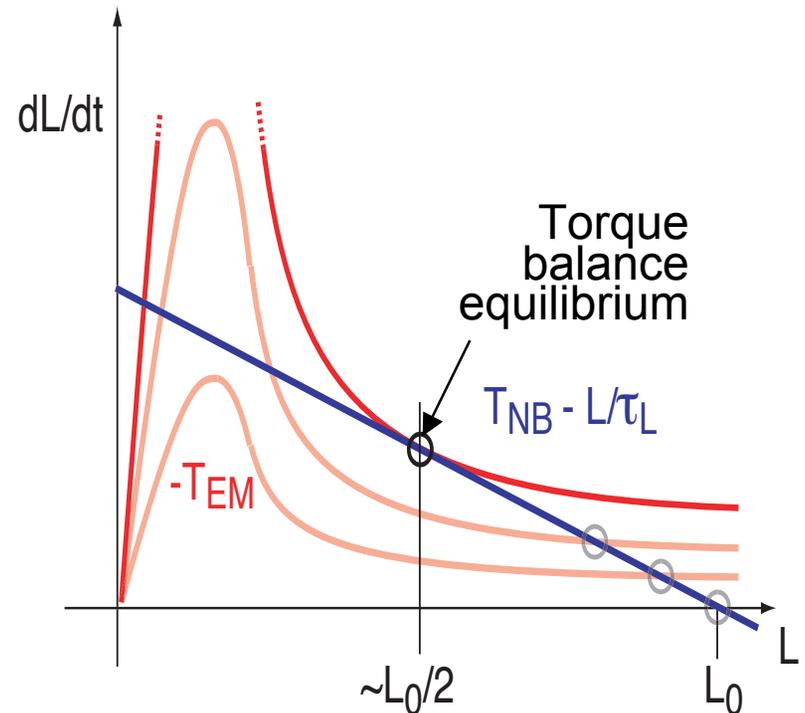
# "Forbidden Band" of Rotation Results in a Higher Effective Rotation Threshold for RWM Onset

- With uncorrected error field, resonant field amplification by stable RWM leads to large electromagnetic torque increasing with beta above no-wall limit



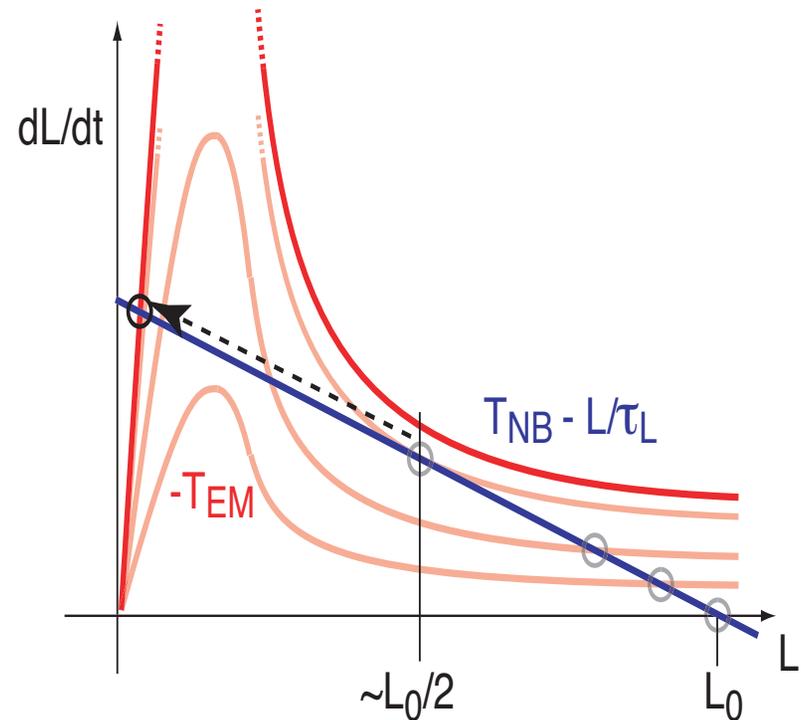
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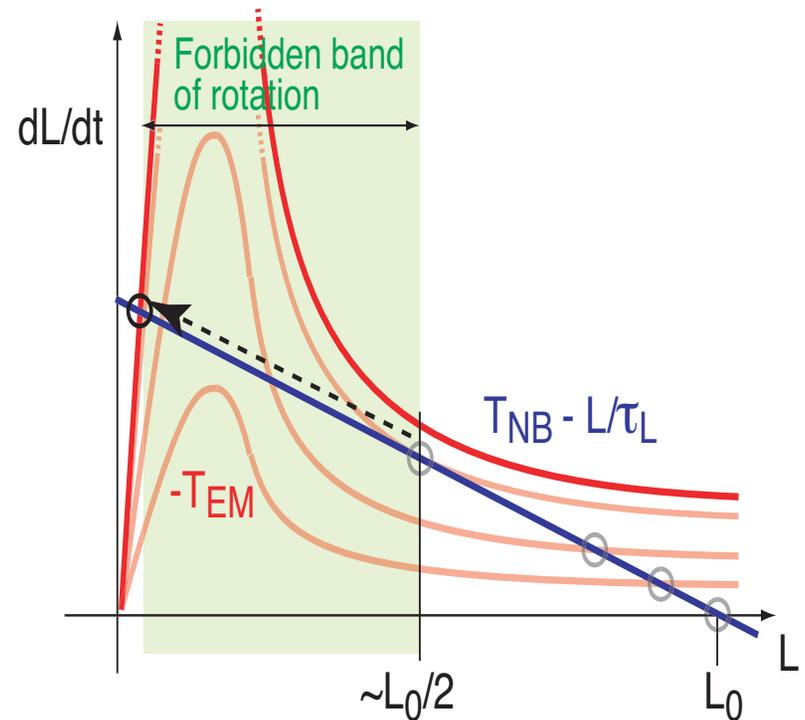
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- As perturbation amplitude increases, torque balance jumps to low-rotation branch



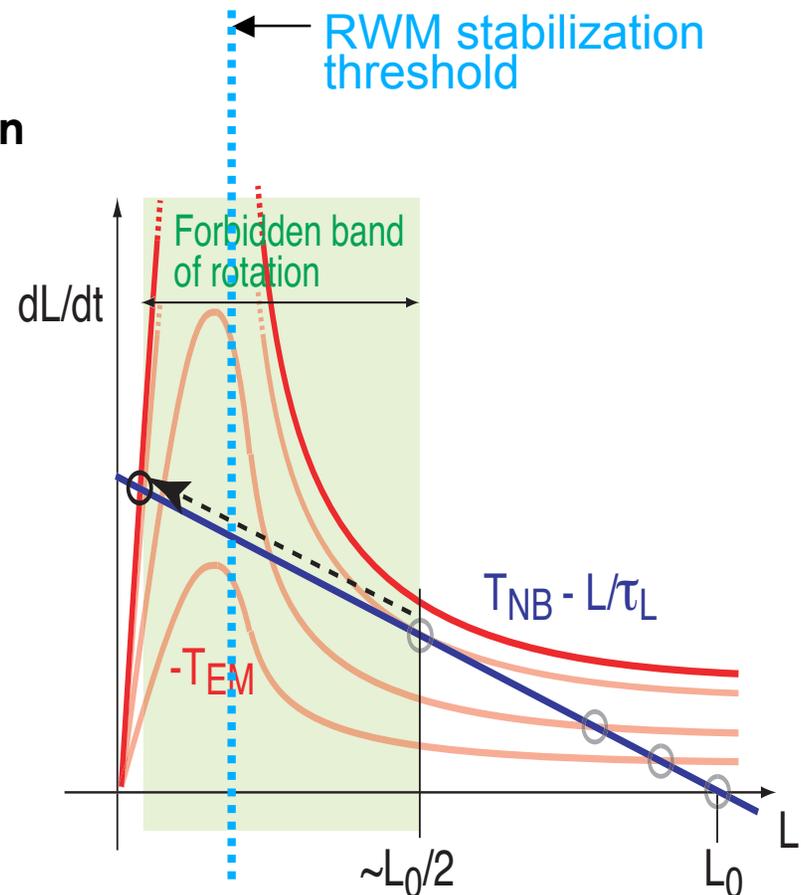
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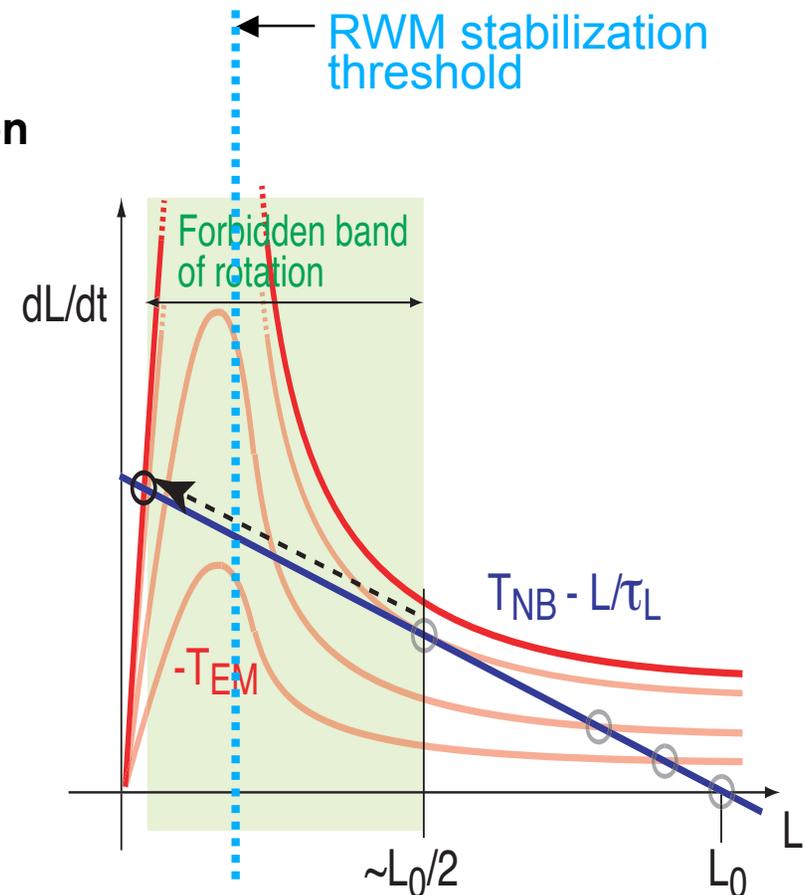
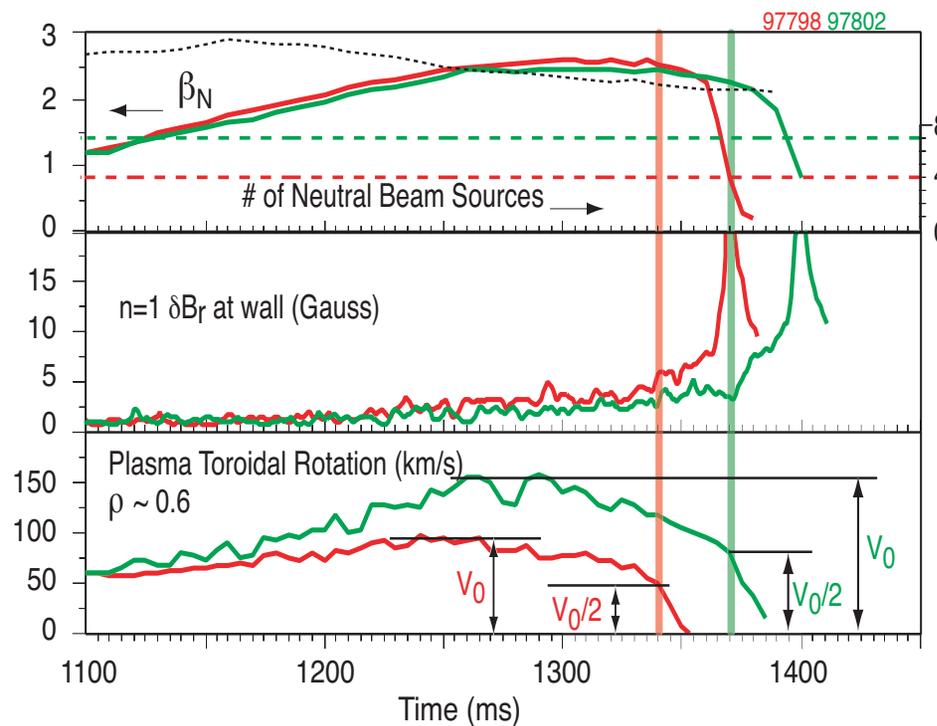
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- With large non-axisymmetric field, bifurcation of rotation occurs above RWM threshold

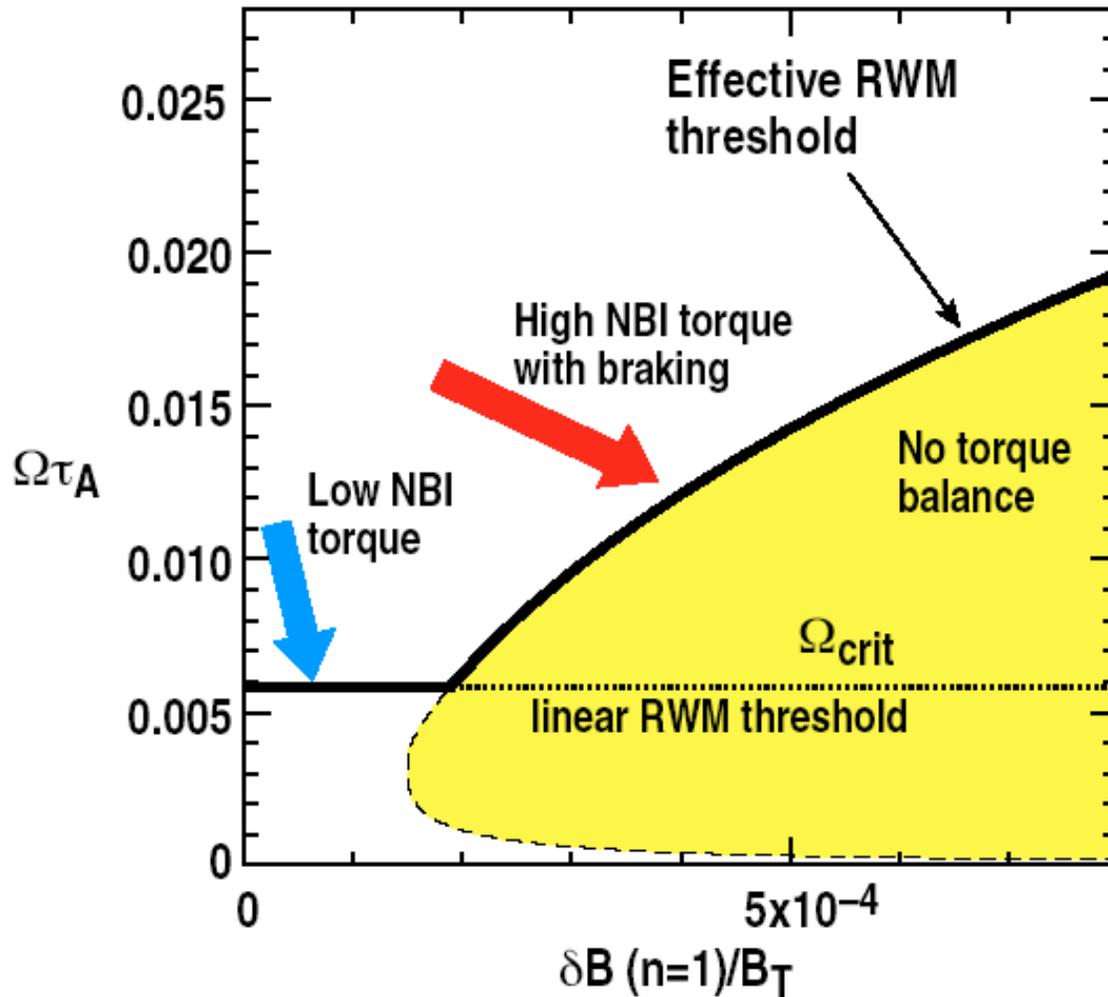


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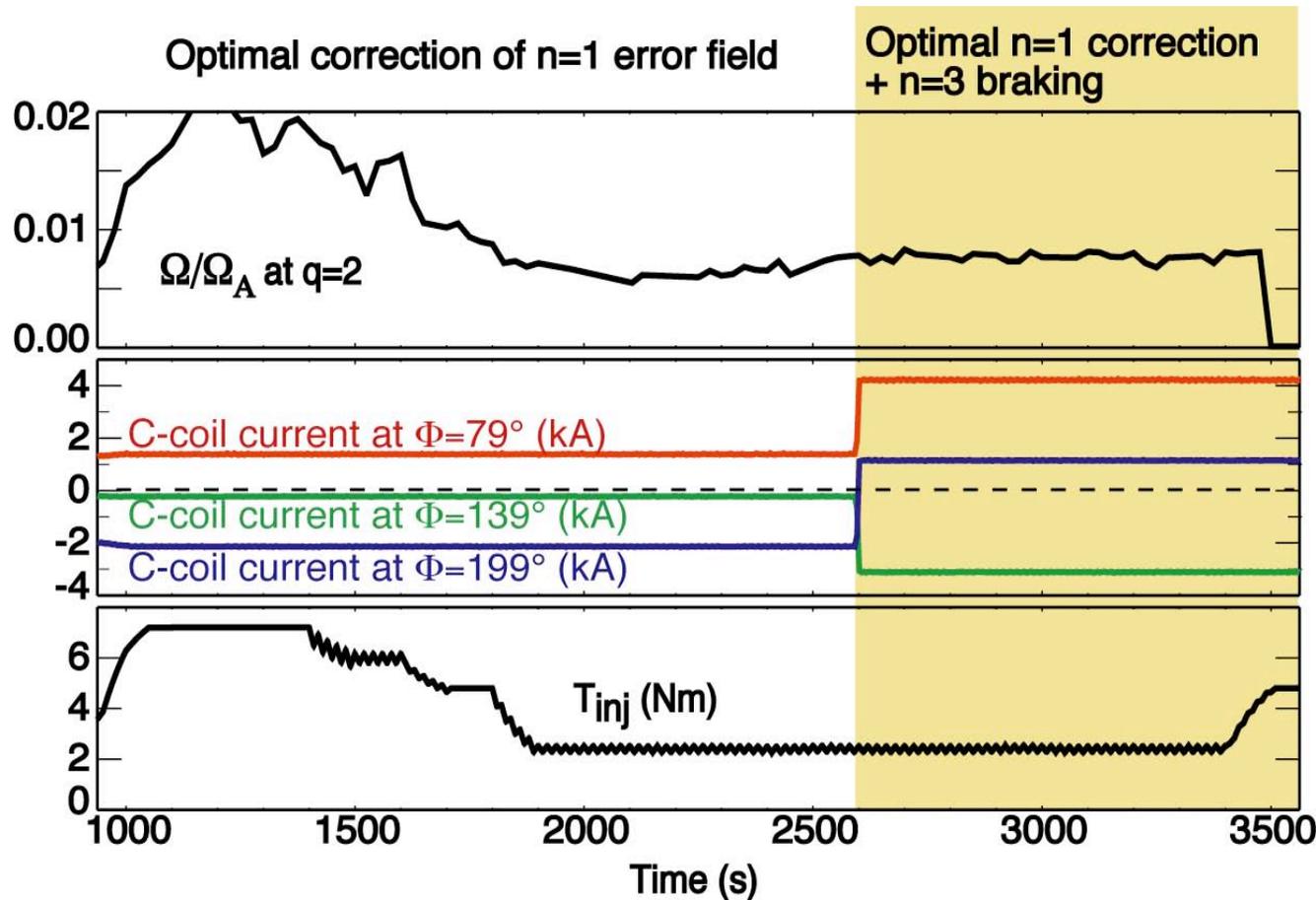


# Recent Model by Fitzpatrick Includes RWM Dispersion Relation With Neoclassical Poloidal Viscosity



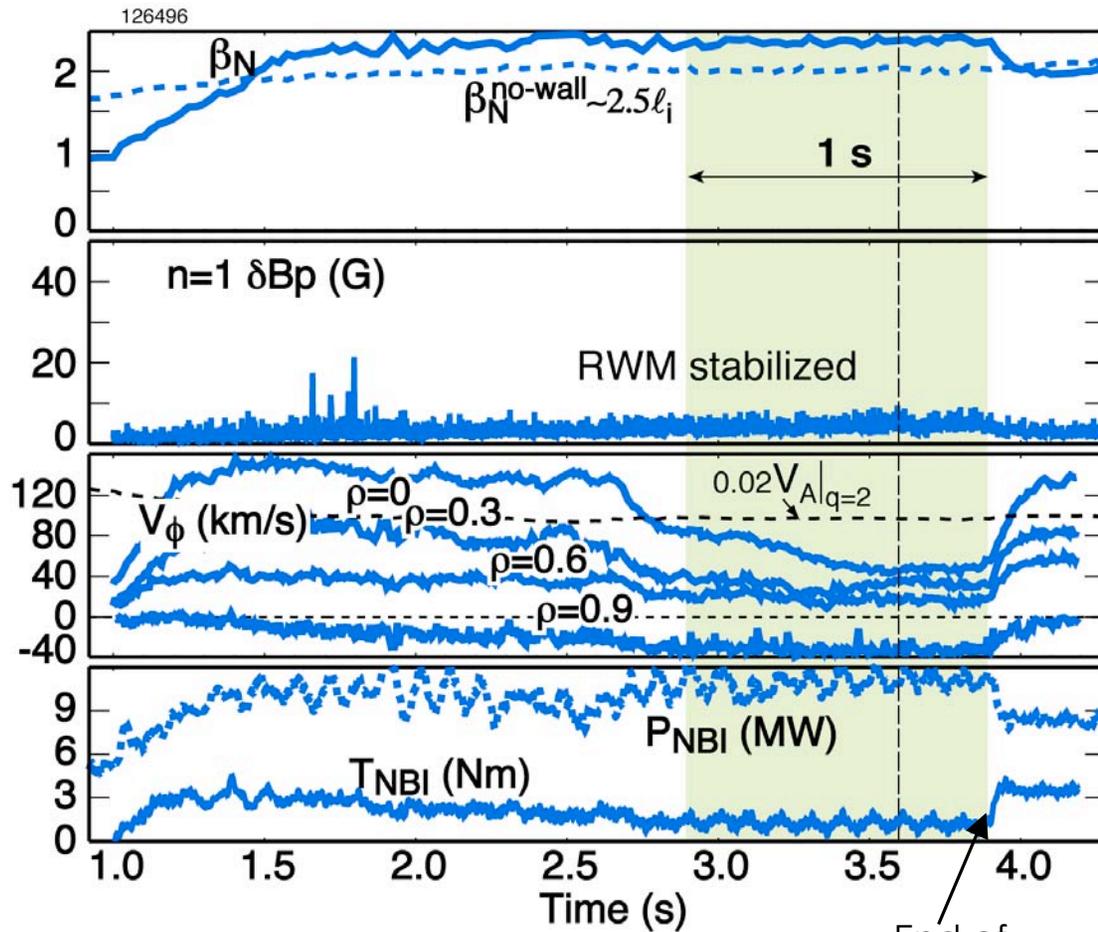
- “True” critical rotation for RWM is seen only when resonant error field is small
- Resonant surface is just outside plasma

# Offset Rotation, Not Bifurcation, Observed With Non-resonant $n=3$ Braking and $\sim$ Balanced Injection

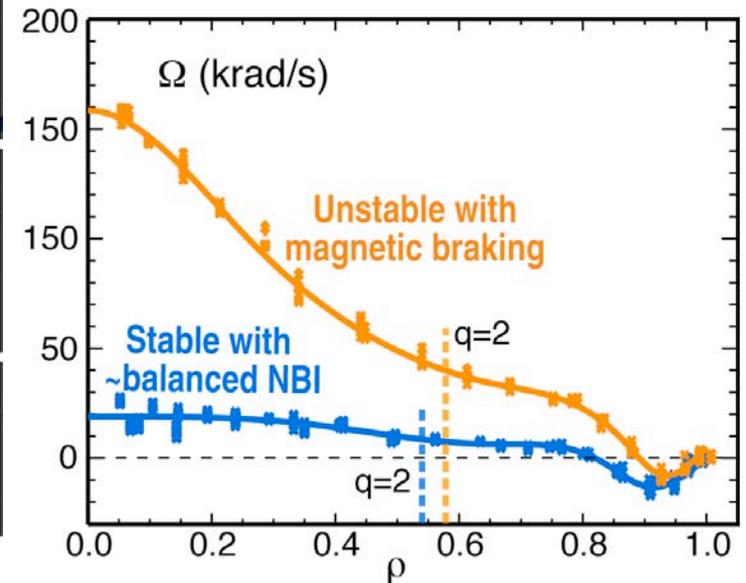


- $I_{n=3} > 3$  kA has little effect on plasma rotation

# With Optimal Error Field Correction, RWM Stabilization at Very Slow Plasma Rotation Sustained for >300 Wall Times



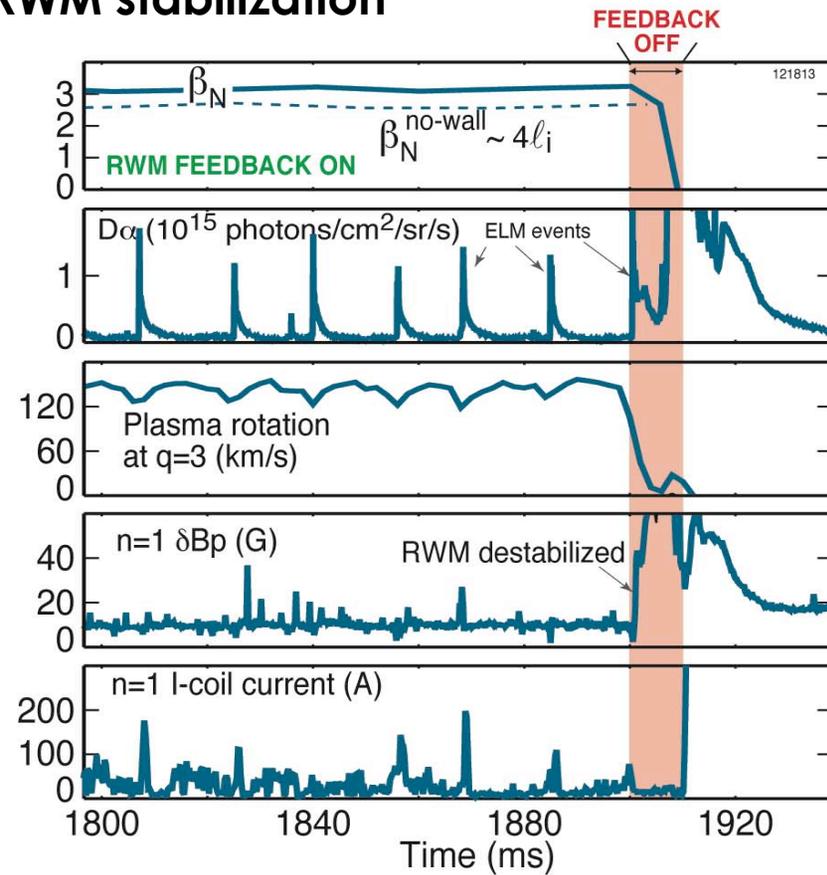
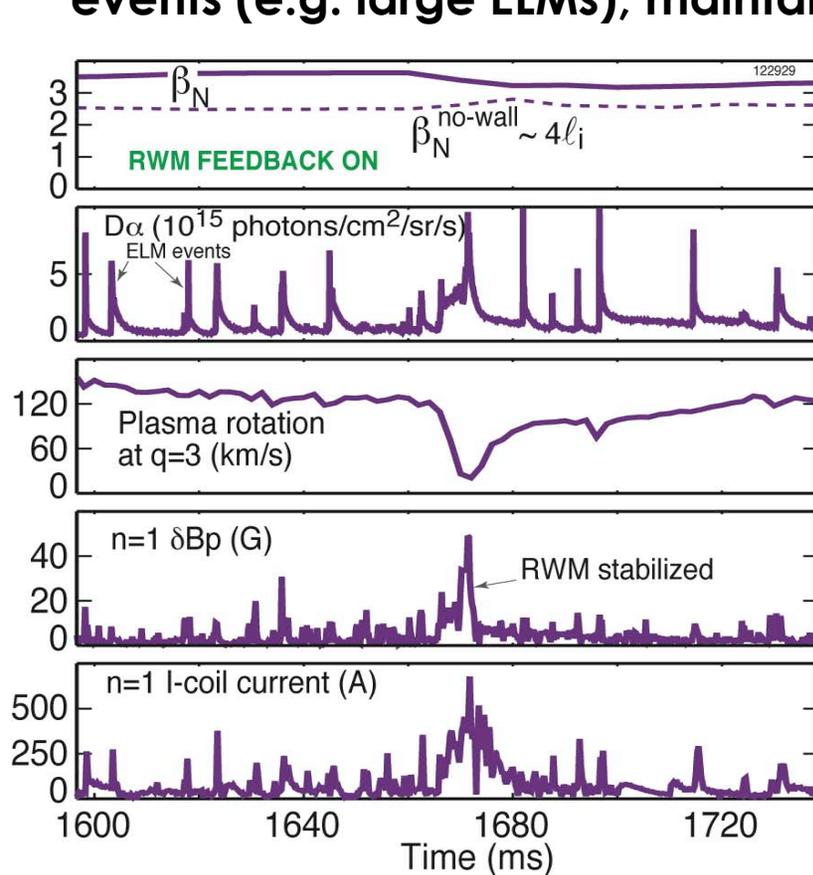
- Plasma rotation at  $q=2$   $\sim 0.35\% \Omega_A$  just above  $\Omega_{crit}$  is sufficient to sustain  $\beta_N$  above no-wall limit



End of counter NBI

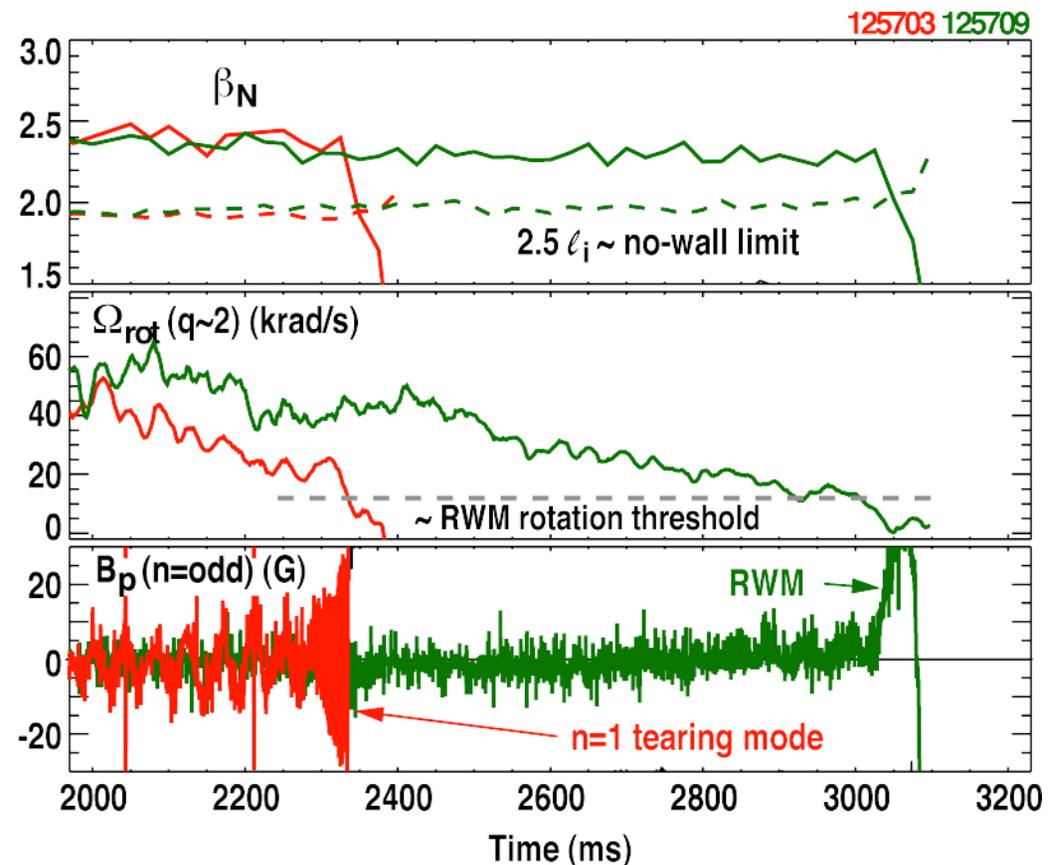
# In High Performance Plasmas (Rapid Rotation) Active RWM Feedback Is Required

- In DIII-D, high rotation is maintained with large, slow-varying  $n=1$  currents in external coils for error field correction
- Smaller, faster-varying  $n=1$  currents in internal coils respond to transient events (e.g. large ELMs), maintain RWM stabilization



# RWM Feedback at Slow Rotation More Difficult Than Anticipated

- First attempts of RWM feedback not yet conclusive
- Onset of 2/1 tearing mode frequently observed near RWM onset
  - High susceptibility to tearing in the vicinity of an ideal MHD stability limit
  - High susceptibility to penetration of resonant non-axisymmetric fields (RWM at amplitude below detection) at very slow rotation



# RWM Stabilized With Near-balanced Neutral Beam Injection

- **The plasma rotation needed for RWM stabilization is much slower than previously thought  $\rightarrow \Omega\tau_A \sim 0.3\%$  at  $q=2$** 
  - Achieved with neutral beam line re-orientation in DIII-D:
    - Balanced neutral beam injection  $\rightarrow$  lower injected torque and plasma rotation with minimized non-axisymmetric fields
  - Such a slow rotation should be achievable in ITER
- **Resonant magnetic braking experiments overestimate the critical rotation**
  - Induction motor model of error field driven reconnection can explain observation of higher apparent thresholds
  - Non-resonant braking cannot slow rotation below RWM low threshold, consistent with NTV theory
- **Ideal MHD with dissipation (MARS-F with kinetic model) is consistent with experimental observations**
  - Edge plasma rotation may be crucial
- **Even with sufficient rotation, active RWM feedback is still needed**
  - System requirements for ITER could be reduced